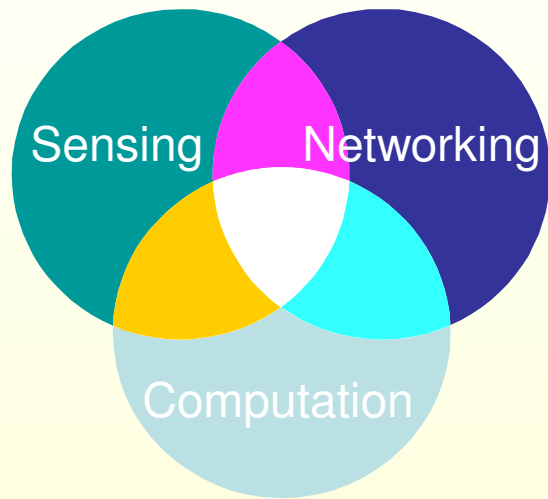
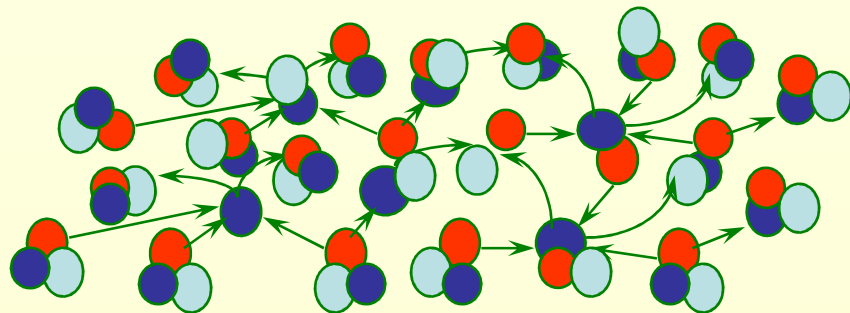


CS321: Sensor Tasking and Control



Leonidas Guibas
Computer Science Dept.
Stanford University



Sensor Deployment/Tasking

- How do we make good use of sensor nodes:
 - where should nodes be deployed?
 - which nodes should sense?
 - which nodes should communicate?

Sensing and Communication Costs



Adequacy/Quality of Information Obtained

We often need to predict the `value` of a sensor reading before we make it ...

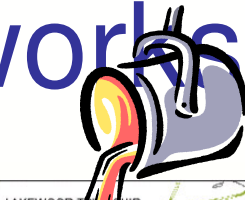
Papers

- Andreas Krause and Carlos Guestrin; **Near-Optimal Nonmyopic Value of Information in Graphical Models**; 21st Conference on **Uncertainty in Artificial Intelligence** (UAI 2005), Edinburgh, July 2005.
- Carlos Guestrin, Andreas Krause and Ajit Singh; **Near-Optimal Sensor Placements in Gaussian Processes**; 22nd International Conference on **Machine Learning** (ICML 2005), Bonn, August 2005.
- Andreas Krause, Carlos Guestrin, Anupam Gupta, Jon Kleinberg; **Near-optimal Sensor Placements: Maximizing Information while Minimizing Communication Cost**; Fifth International Conference on **Information Processing in Sensor Networks** (IPSN'06), April 2006.
- Andreas Krause and Carlos Guestrin; **Near-optimal Observation Selection Using Submodular Functions**; survey paper for the Nectar track in the 22nd Conference on **Artificial Intelligence** (AAAI), Vancouver, July 2007.
- Jure Leskovec, Andreas Krause, Carlos Guestrin, Christos Faloutsos, Jeanne VanBriesen and Natalie Glance; **Cost-Effective Outbreak Detection in Networks**; 13th ACM SIGKDD International Conference on **Knowledge Discovery and Data Mining** (KDD), San Jose, August 2007.

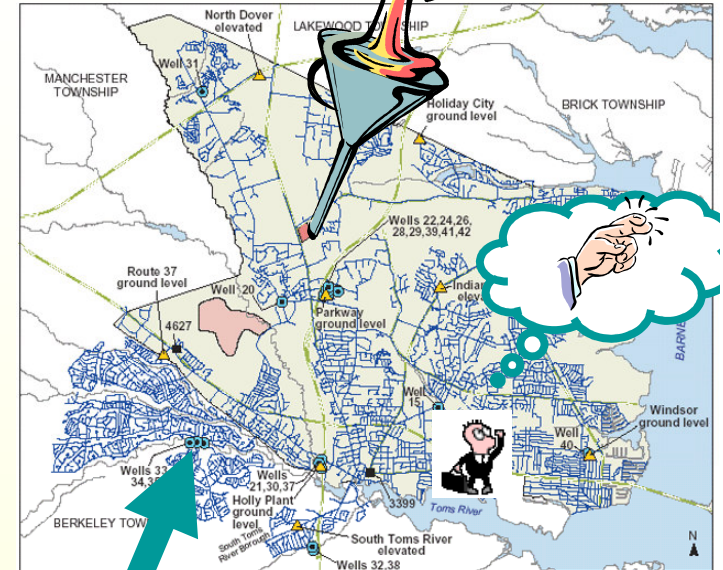
Sensor Placement/Tasking Examples

Water Distribution Networks

Chlorine



- **Water distribution in a city**
→ very **complex system**
- **Pathogens in water can affect thousands** (or millions) of people
- Currently: **Add chlorine** to the source and **hope for best**

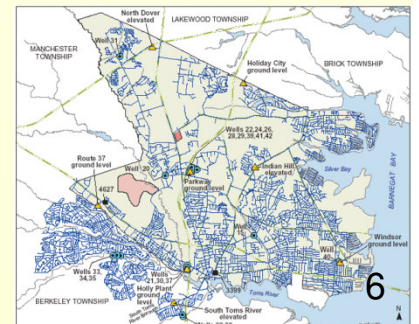


Barnegat Bay, NJ

ATTACK!
could deliberately
introduce pathogen

Sensing the Waterways

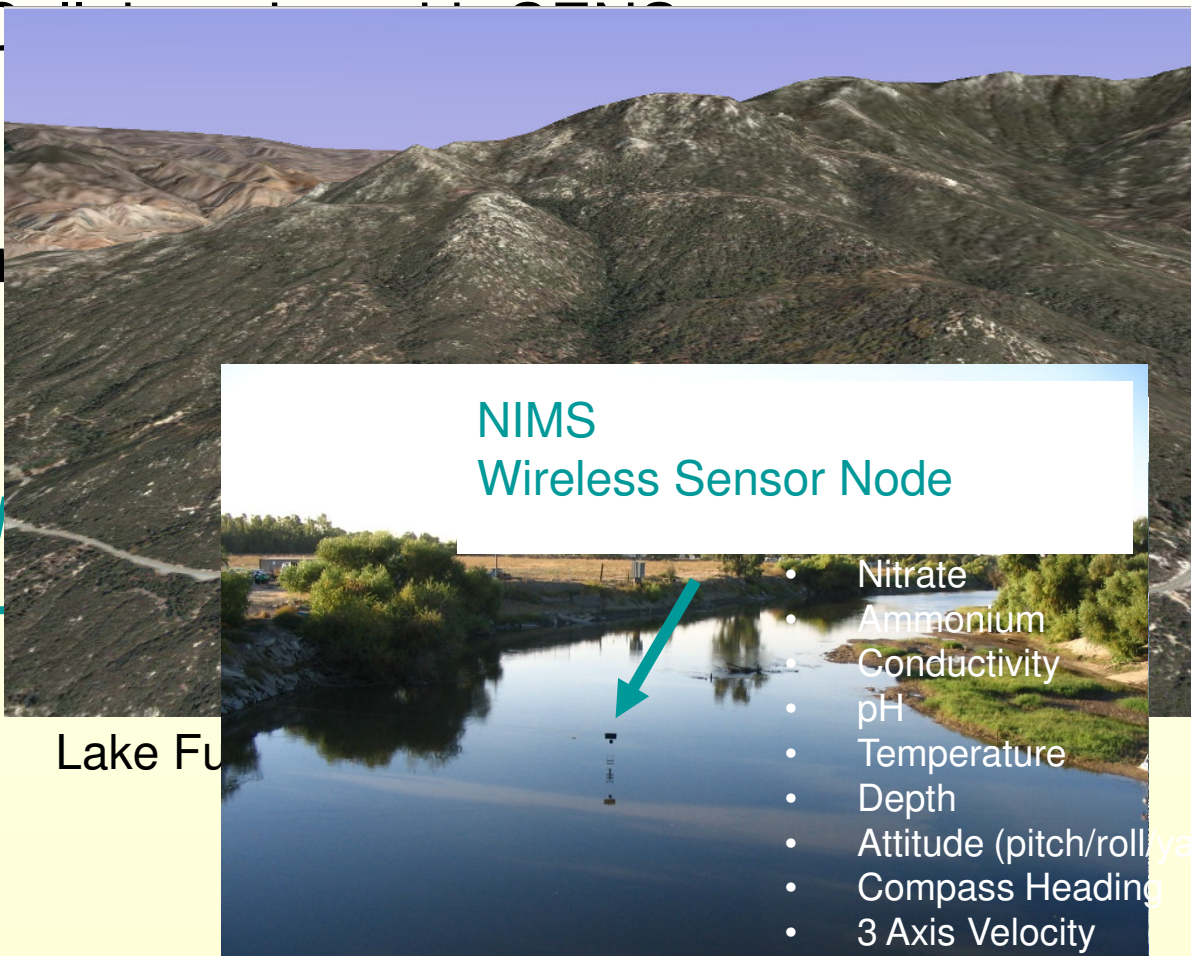
- Sensors in pipes (or taps) could detect pathogens **quickly**
 - minimize population affected, ...
- **1 Sensor: \$5,000** (just for chlorine)
- Local government not willing to spend much money
 - **Must be smart about where to place sensors**
- **Battle of the Water Sensor Networks** (competition Oct. 2006)
 - Get **model of a city**
 - **Simulator** of water flow provided by the **EPA**
 - Competition for **best placements**



Monitoring Algae Biomass in Lakes and Rivers

- Algae levels too high → Monitor biomass

- C



Lake Fu

NIMS
Wireless Sensor Node

- Nitrate
- Ammonium
- Conductivity
- pH
- Temperature
- Depth
- Attitude (pitch/roll/yaw)
- Compass Heading
- 3 Axis Velocity

Chair Sensor Placement

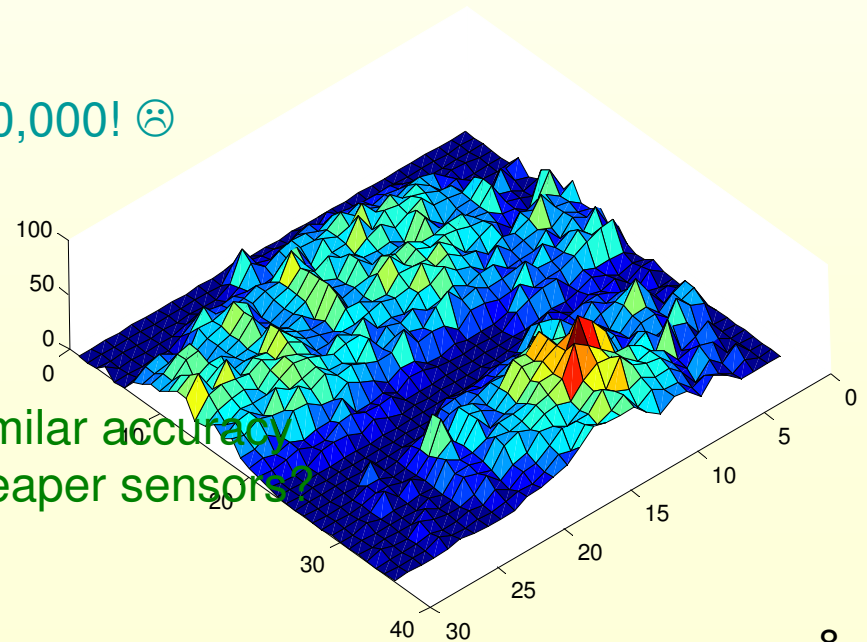
- Help elderly stay active/healthy by activity recognition using a pressure sensing chair



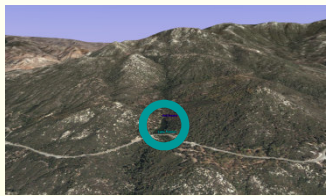
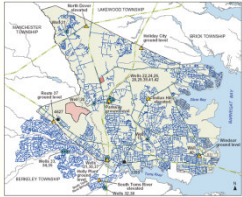
Equipped with
1 sensor per cm^2 ! 😊

Costs \$10,000! 😞

Can we get similar accuracy
with fewer, cheaper sensors?



Fundamental Question: Sensor Placement



Where should we place sensors to monitor spatial phenomena?

- pathogen distribution
- algae biomass
- temperature and light field
- rear-end pressure
- ...

PART I:

Near-Optimal Sensor Placement:

Maximizing **Information**

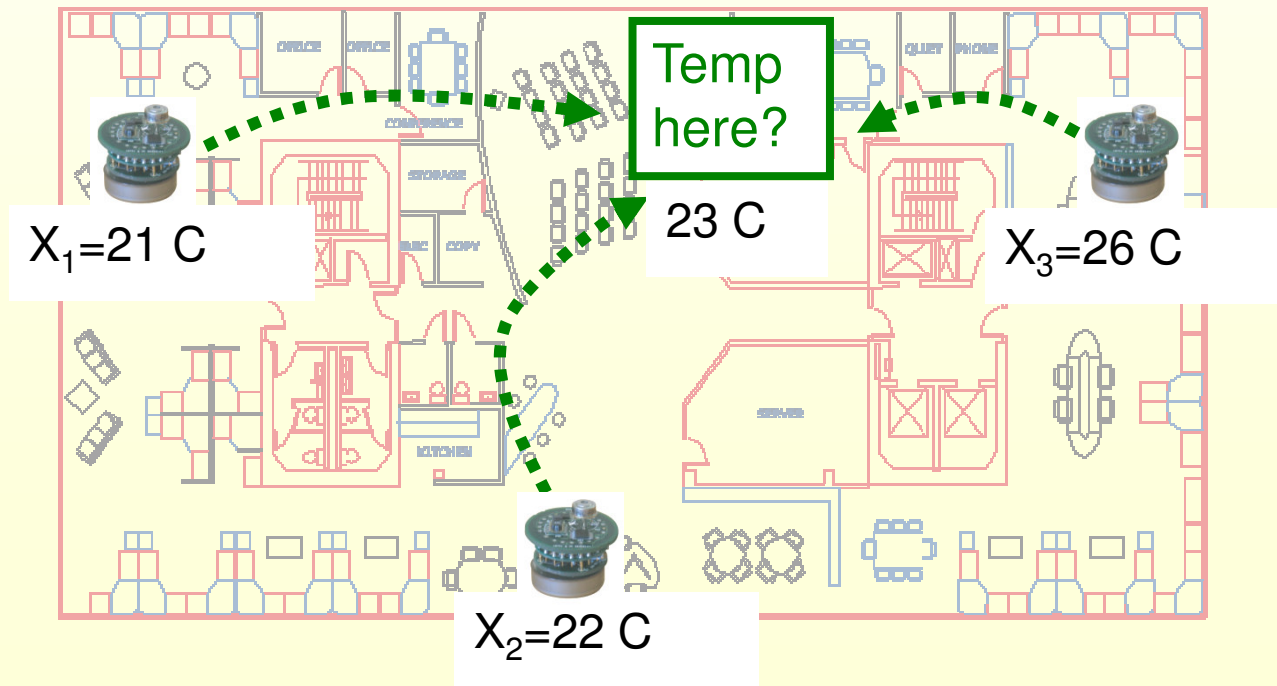
while

Minimizing **Communication Cost**

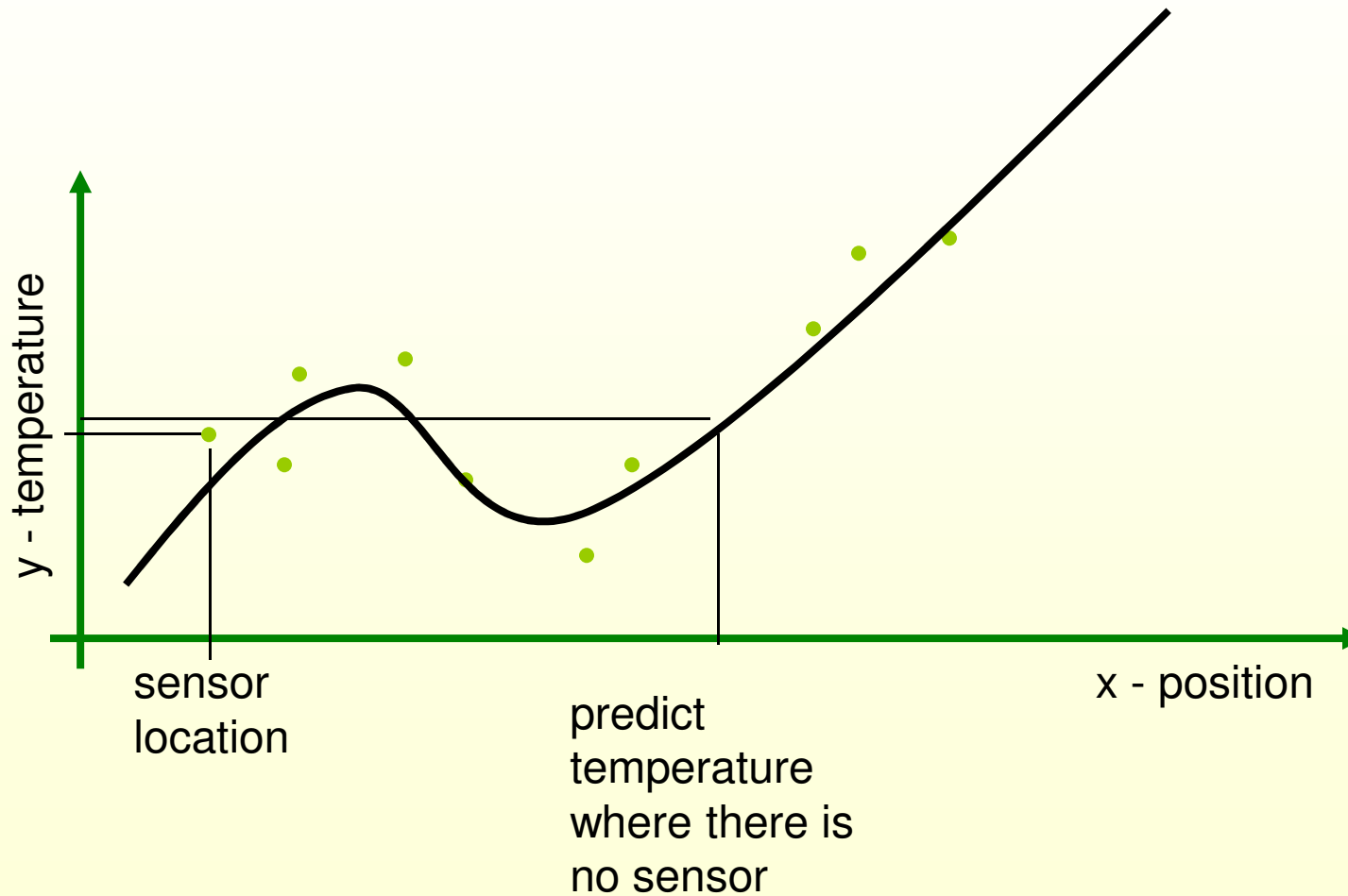
First question in presentation:
How do we use sensors to monitor
a spatial phenomena?

Predicting Spatial Phenomena from Sensor Readings

- Can only measure where we have sensors
- **Multiple sensors** can be used to predict phenomena at **uninstrumented** locations

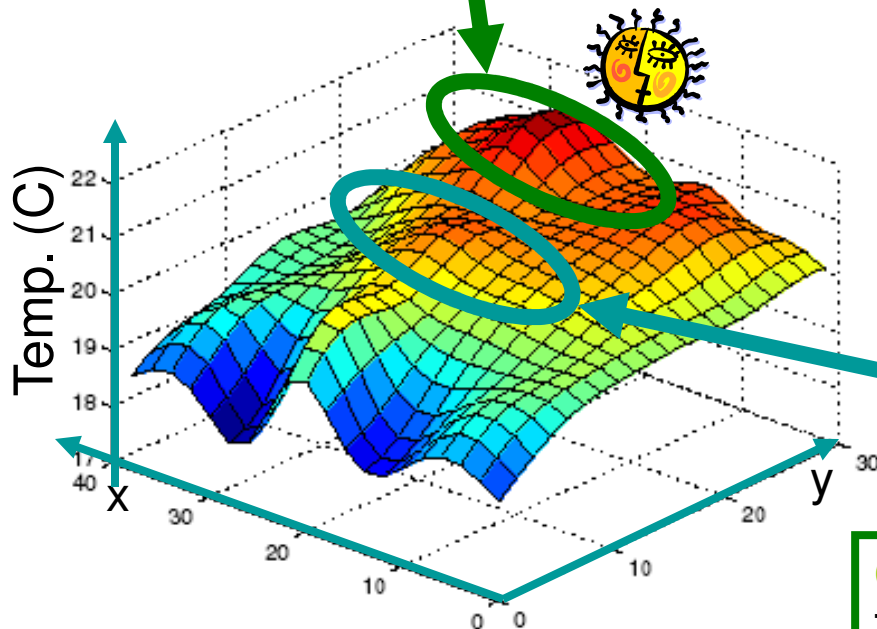


Prediction is a Regression Problem

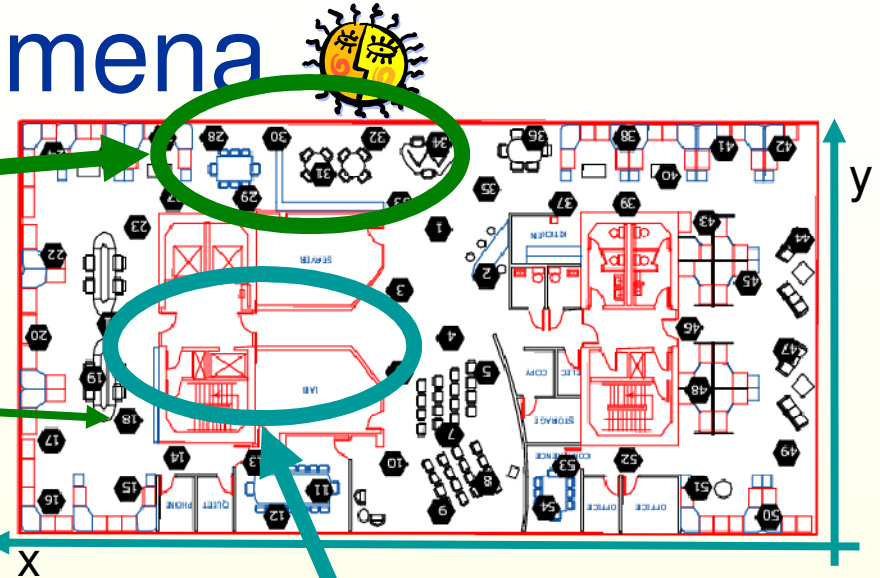


Regression Models for Spatial Phenomena

Real deployment
of temperature sensors
many sensors around →
trust estimate here
measurements from 52 sensors
(black dots)



Predicted temperature
throughout the space

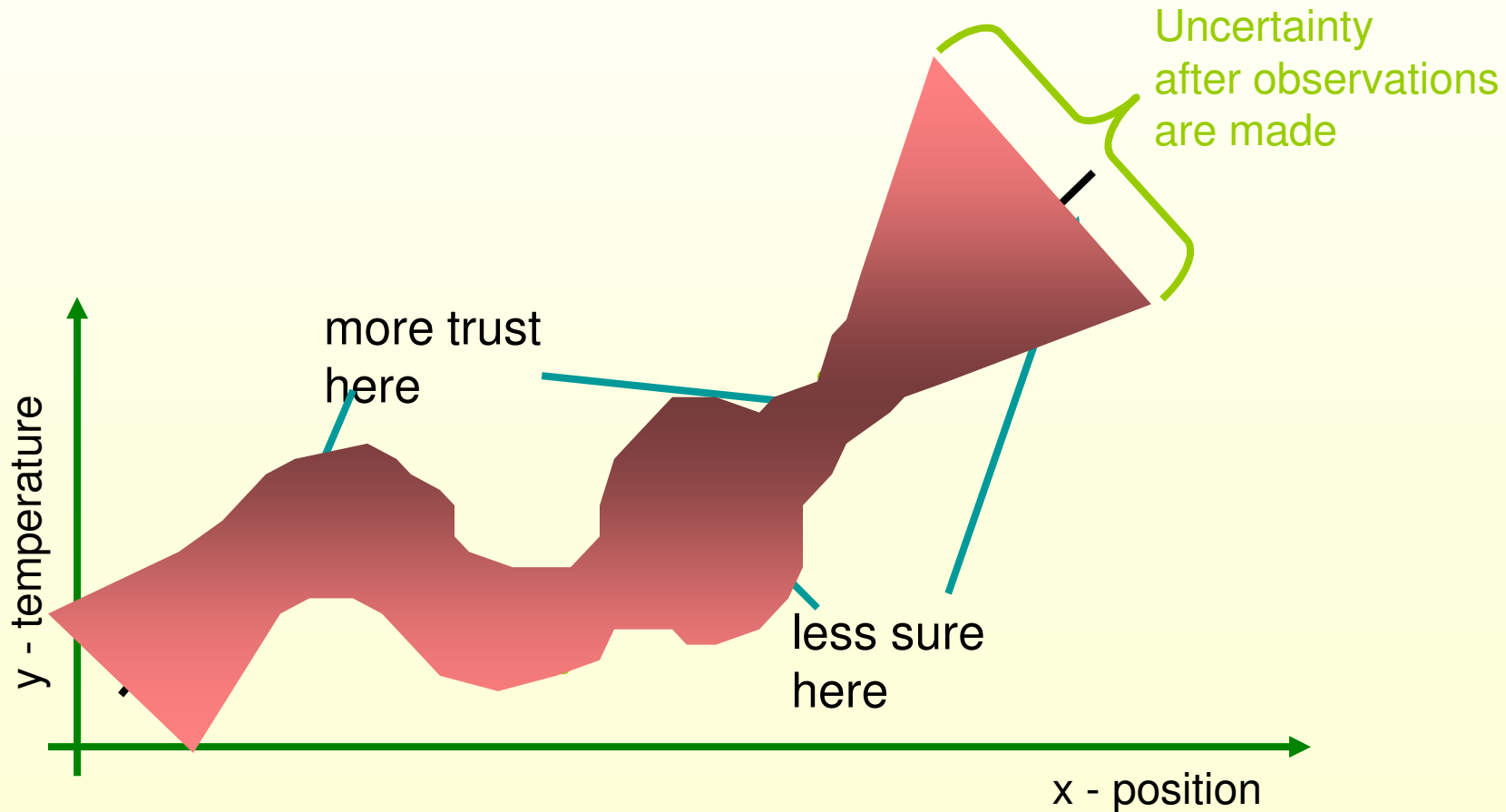


few sensors around →
don't trust estimate

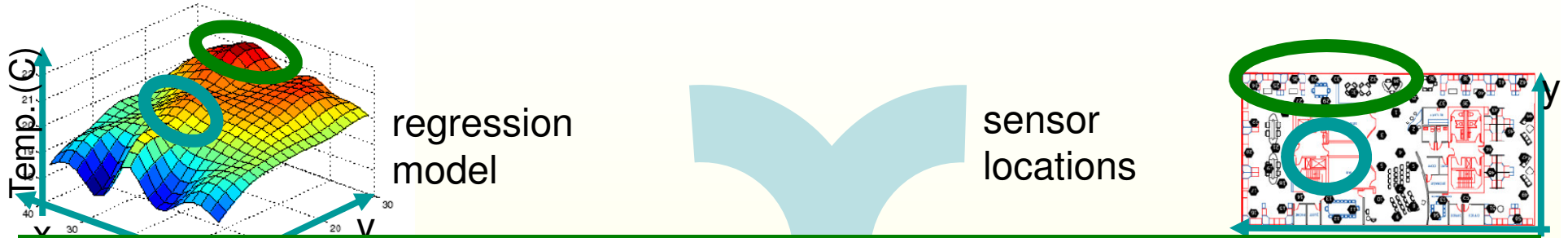
Good sensor placements:
Trust estimate everywhere!

Uncertainty about Prediction – Intuition

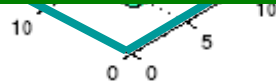
trusting estimate \leftrightarrow low uncertainty about prediction



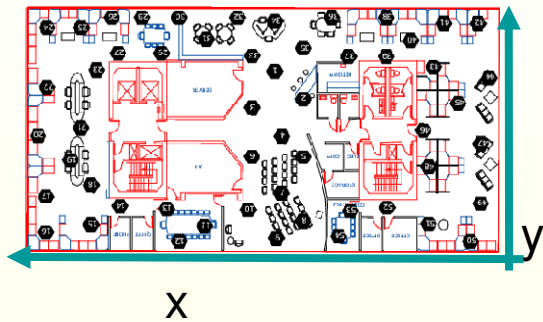
Probabilistic Models for Spatial Phenomena



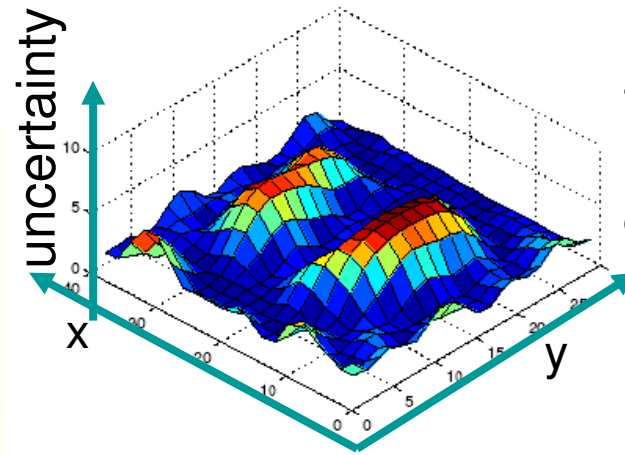
- Modeling uncertainty is fundamental!
- Many rich probabilistic models
 - gaussian processes, a *non-parametric* model [O'Hagan '78]
 - Learned from pilot data or computed from expert model (e.g., EPA)
- Learning model is well-understood → **focus on optimizing sensor locations**



Information Quality



sensor placement A

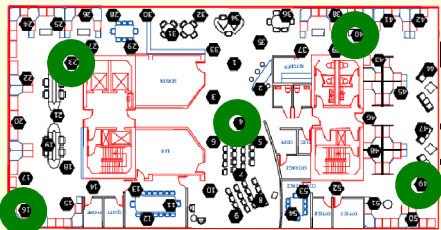


information quality $I(A)$

uncertainty in prediction
after placing sensors

● Pick locations **A** with **highest information quality**

● lowest “uncertainty” after placing sensors

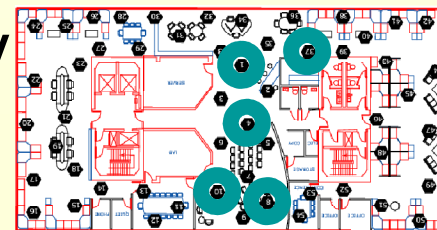


placement A

$I(A) = 10$

and in terms of entropy

on



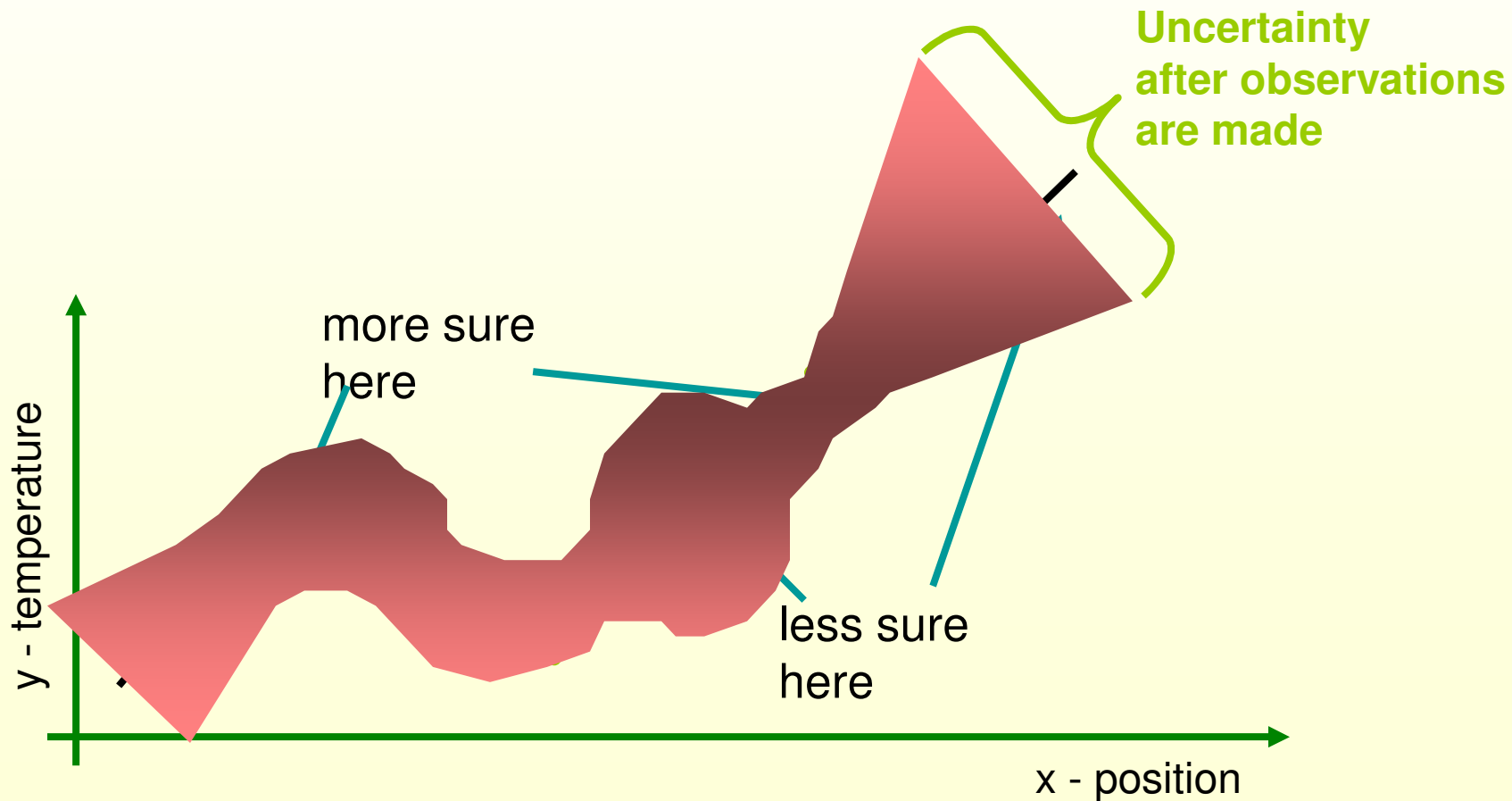
placement B

$I(B) = 4$

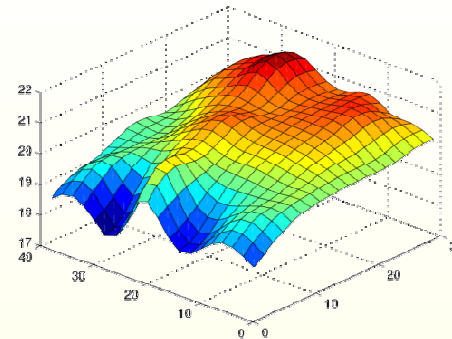
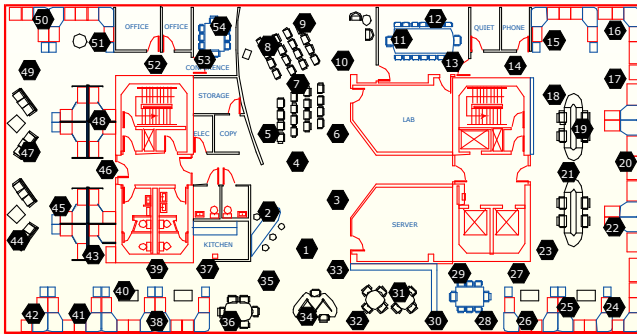
rior

Gaussian Processes (GP) - Intuition

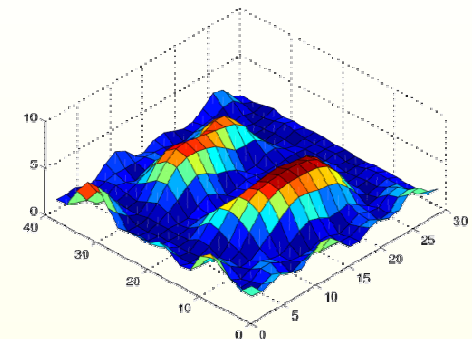
**GP – Non-parametric; represents uncertainty;
complex correlation functions (kernels)**



Gaussian Processes



Posterior
mean temperature



Posterior
variance

Kernel function:

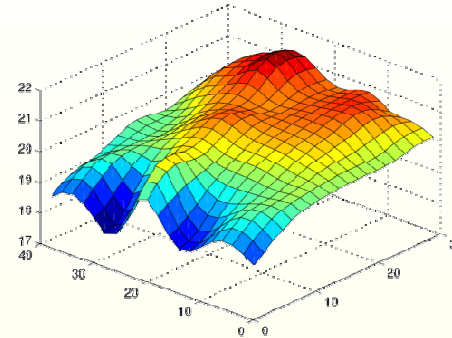
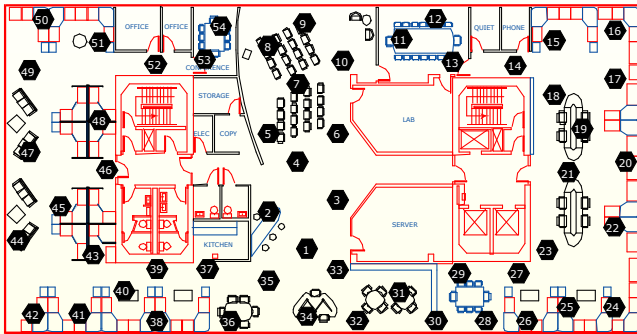
$$\sigma_{ij} = K(x_i, x_j)$$

Prediction after observing
set of sensors A :

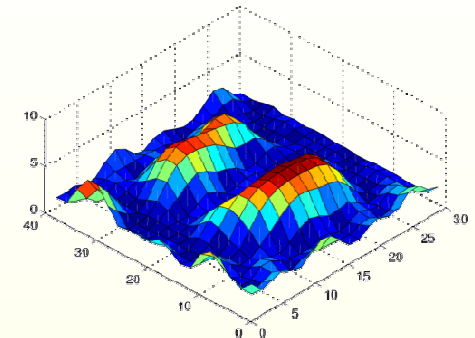
$$\mu_{Y|A} = \mu_Y + \Sigma_{YA} \Sigma_A^{-1} (x_A - \mu_A)$$

$$\sigma_{Y|A} = \sigma_Y + \Sigma_{YA} \Sigma_A^{-1} \Sigma_{AY}$$

Gaussian Processes for Sensor Placement



Posterior
mean temperature



Posterior
variance

Goal:
Find sensor placement with least
uncertainty after observations

Problem is still NP-complete ☹️
Need approximation

Sensor Placements

- Consider **myopically** selecting

$$H(A_1) + H(A_2 | \{A_1\}) + \dots + H(A_k | \{A_1 \dots A_{k-1}\})$$

most uncertain
 This is exactly the joint entropy
 $H(\mathbf{A}) = H(\{A_i\}_{i=1}^k)$

most uncertain
 given $A_1 \dots A_{k-1}$

- This can be seen as an attempt to maximize

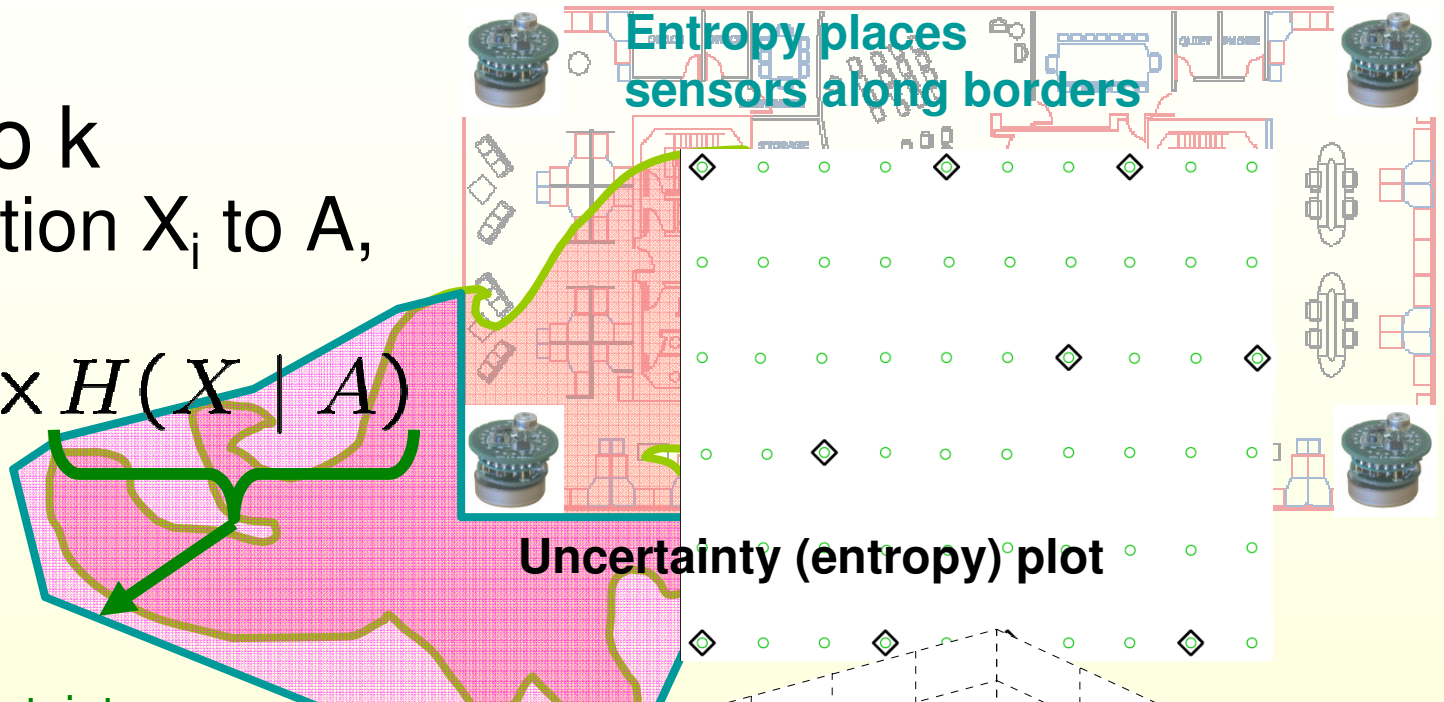
$$\max_{\mathbf{A} \subset \mathcal{S}} H(\mathbf{A}) \text{ subject to } |\mathbf{A}| \leq k$$

Entropy Criterion *(c.f., [Cressie '91])*

- $A \leftarrow \emptyset$
- For $i = 1$ to k
 - Add location X_i to A ,
s.t.:

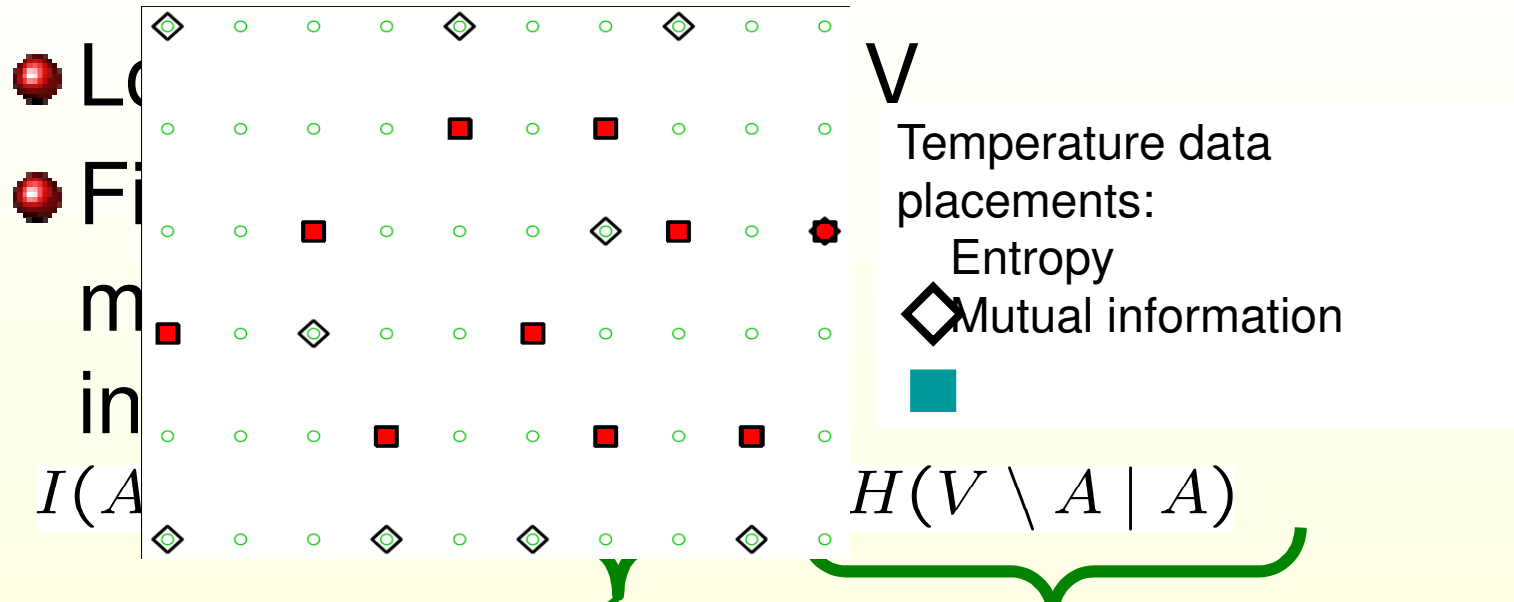
$$X_i = \operatorname{argmax}_X H(X | A)$$

“Wasted”
information
observed by
Entropy



Entropy criterion wastes information [O'Hagan '78],
Indirect, doesn't consider sensing region –
No formal guarantees 😞

Objective Function: Mutual Information



Intuitive criterion – Locations that are both different and informative
Formal guarantees 😊

High uncertainty
 given A –
X is different

Low uncertainty
 given rest –
X is informative

The Placement Problem

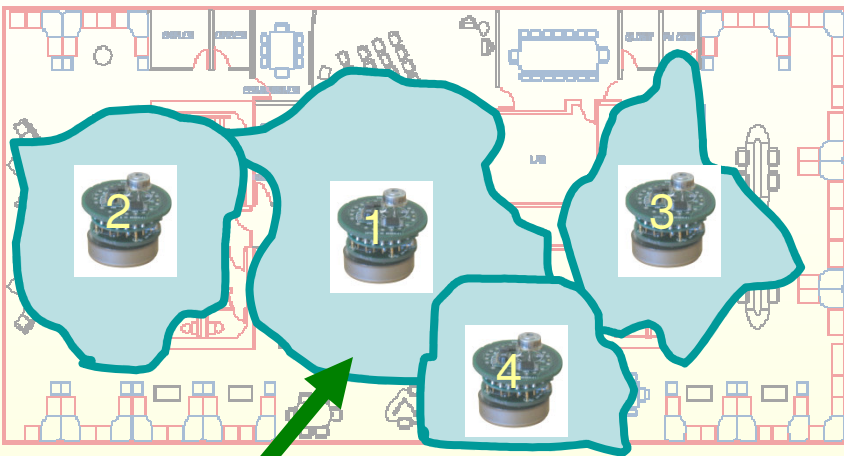
- Let V be set of locations we can choose from
- For subset of locations $A \subseteq V$, let
 - $I(A)$ be **information quality** of placement A

• Want to optimize
 $\max_A I(A)$ subject to $|A| \leq k$

- A well-studied problem: *c.f.* [Lindley '56, O'Hagan '78, Sacks et al. '89, Cressie '91, Rasmussen '96, Atkinson '96, Flaherty et al. '05,...]
- **NP-hard** → most **existing methods are heuristics with no quality guarantees**
- **Let's look at one such heuristic...**

Simple Greedy Algorithm

Greedy:



area where
sensor provides
“information”

- First pick most informative location:

$$X_1 = \operatorname{argmax}_X I(X)$$

- Then, pick most **improvement** given previous one:

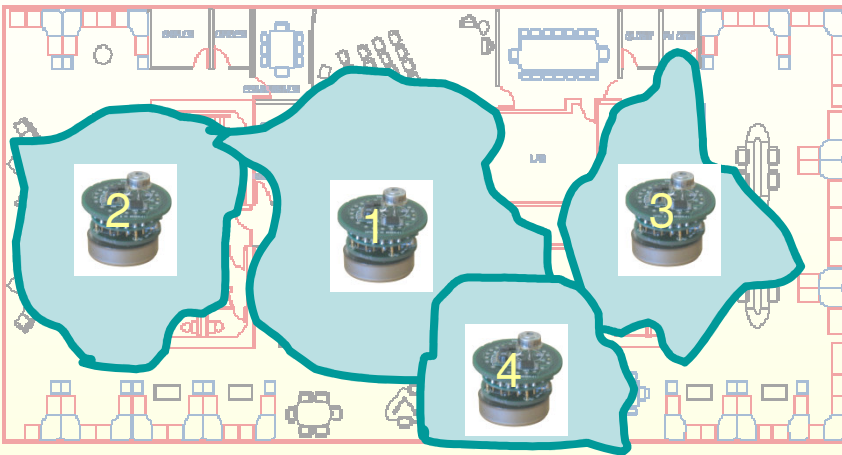
$$X_2 = \operatorname{argmax}_X I(X \cup X_1) - I(X_1)$$

- And so on...

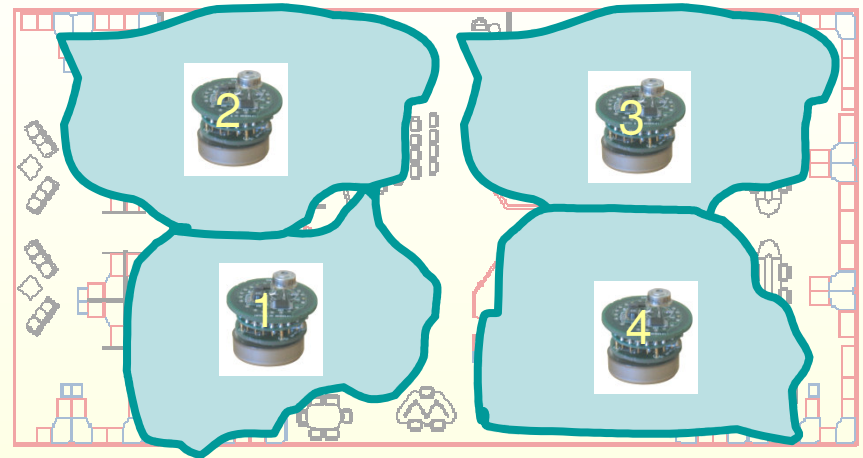
$$X_3 = \operatorname{argmax}_X I(X \cup X_1 \cup X_2) - I(X_1 \cup X_2)$$

Greedy Algorithms are Generally Suboptimal

Greedy:

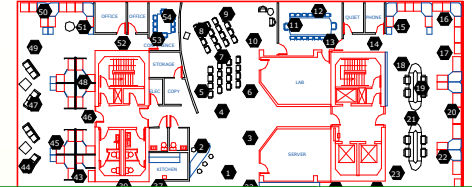
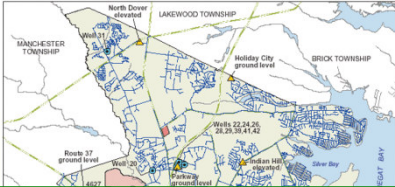


Optimal:



- **Greedy** algorithm provides **suboptimal** solution 😞
- But greedy **doesn't look that bad...** 😊

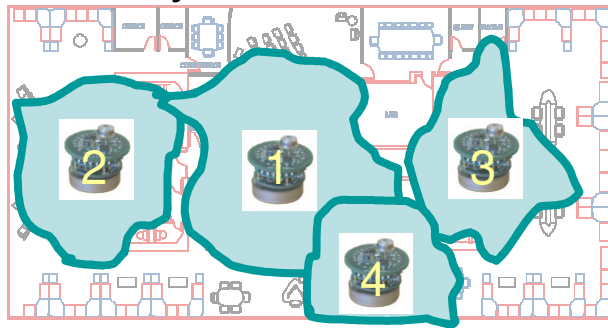
Greedy is Pretty Good!



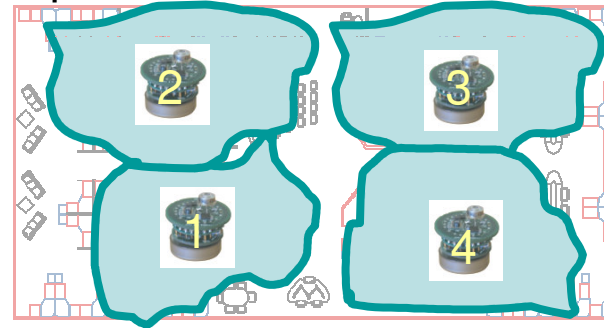
simple greedy algorithm works rather well!

Why ????

Greedy:



Optimal:



- Greedy behaves **well in the first few steps**
- By the time it becomes “**suboptimal**”, there **isn't much information** to be had...

Key Observation: Law of Diminishing Returns

Placement A = $\{S_1, S_2\}$

Placement B = $\{S_1, \dots, S_5\}$



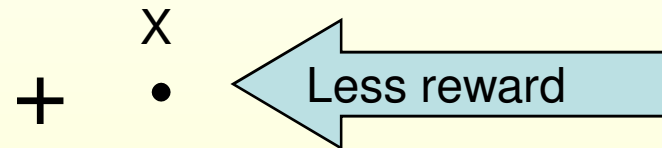
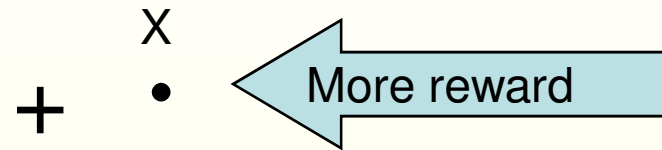
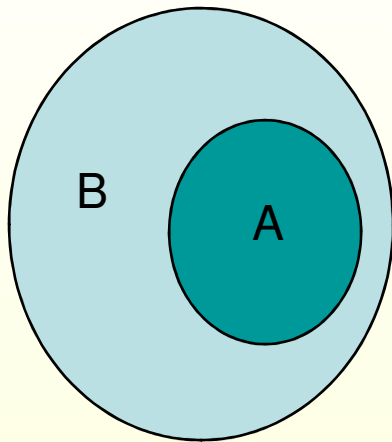
Adding S' will help a lot!



New sensor S'

Adding S' doesn't help much

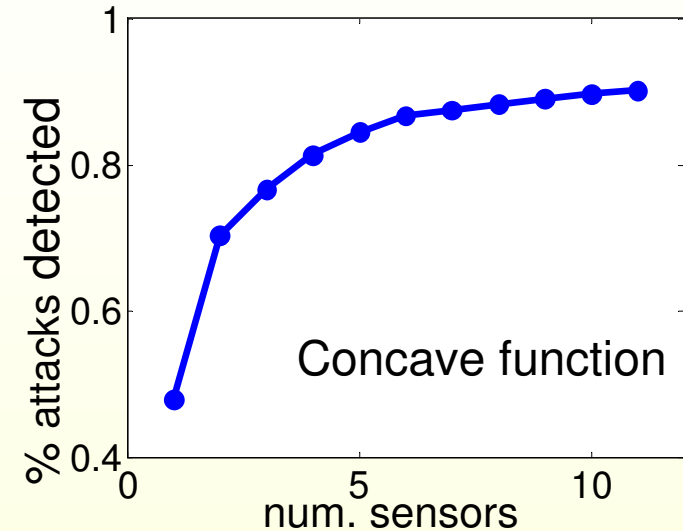
Submodular Functions: Functions on Sets



$$F(A \cup X) - F(A) \geq F(B \cup X) - F(B)$$
$$A \subseteq B$$

Submodularity and Sensor Placement

Many sensor placement objectives are submodular!!! :-)



If $I(A)$ is a submodular function

Concave behavior: ↘ improvement provided by last sensor

diminishing returns → improvement small 😊

Sensor Placement for Information Quality

- **Theorem: Greedy** algorithm provides **constant factor approximation**: placing k sensors:

$$I(A_{\text{greedy}}) \geq (1 - 1/e) \max_{A:|A|=k} I(A)$$

Result of the algorithm

Constant factor
~63%

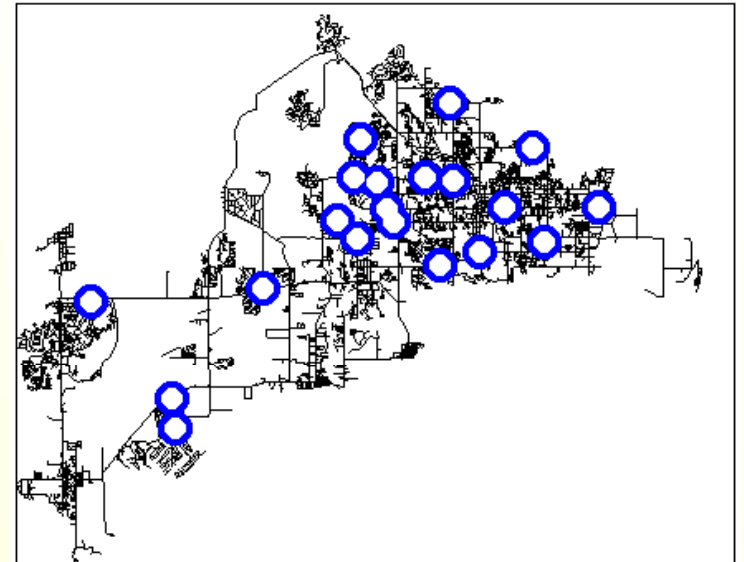
Optimal solution

Example: Water Networks Competition

- 12,527 junctions
- 3.6 million contamination events

- Place 20 sensors to
 - maximize detection likelihood
 - minimize detection time
 - minimize population affected

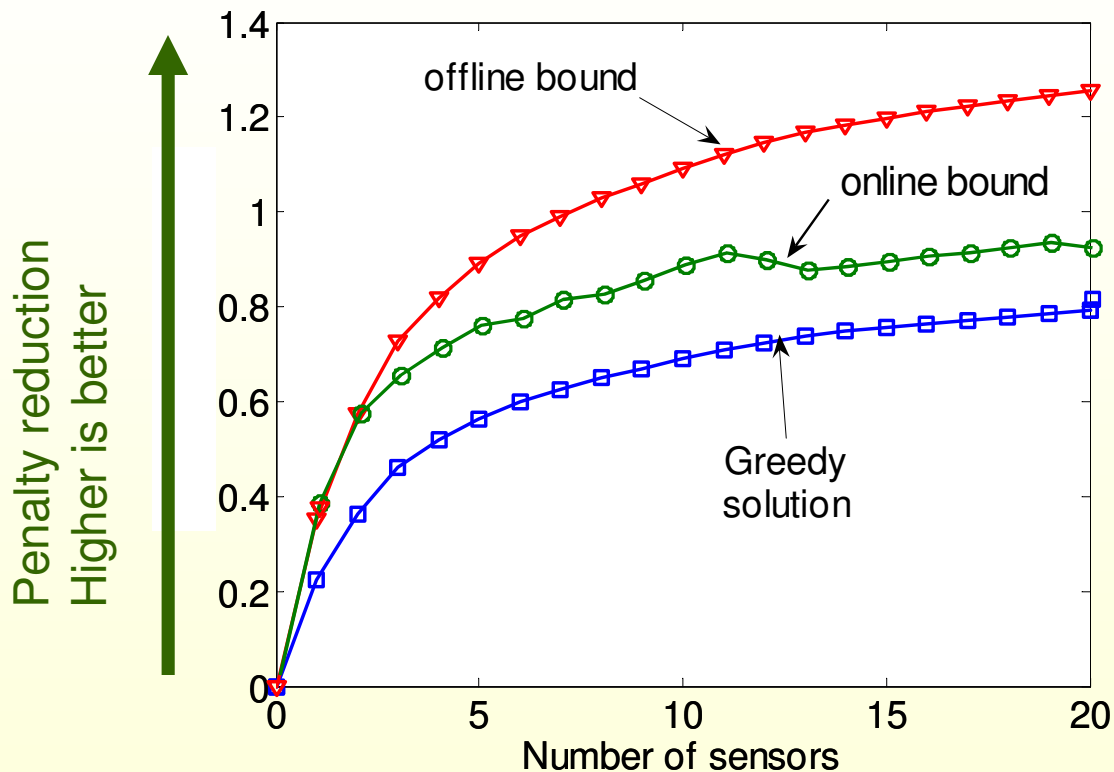
in expectation over all possible contaminations



Observation:

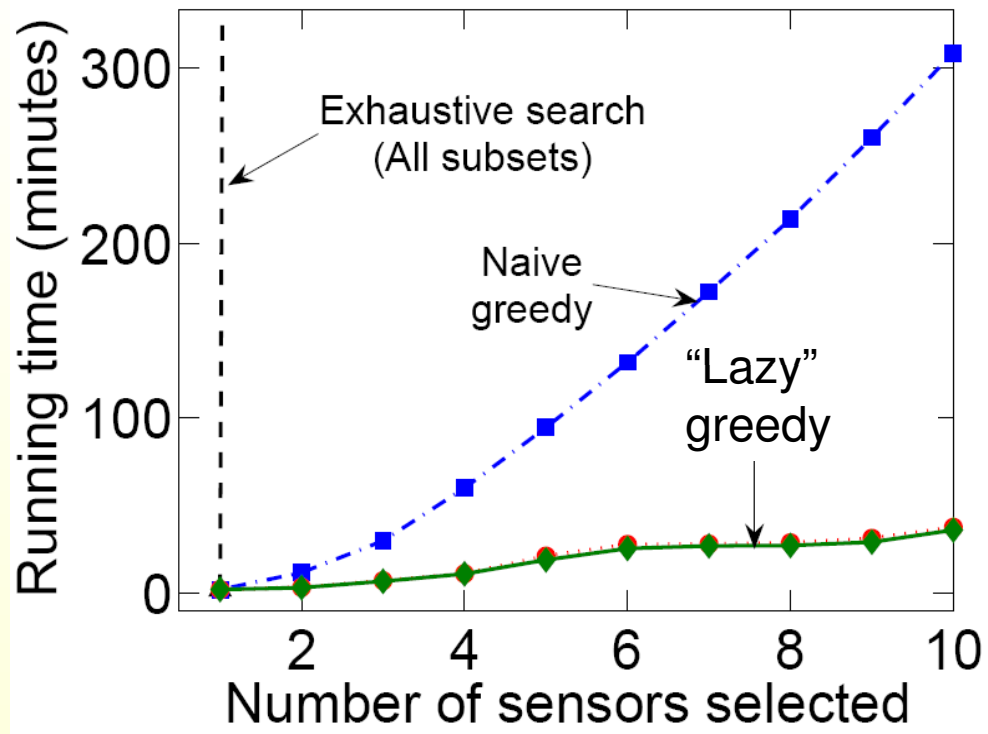
All these objectives are submodular! 😊

Bounds on Optimal Solution



- Submodularity allows us to obtain **online** bounds on the performance of **any** algorithm
 - Use to evaluate quality of heuristic (e.g., simulated annealing)
 - Use in branch and bound algorithms

Speeding Up Algorithms



- Submodularity allows to **speed up** algorithms using **“lazy evaluations”**

Results of BWSN [Ostfeld et al]

- Multi-criterion optimization
 - “everybody is a winner”
- [Ostfeld et al ‘07]: count number of non-dominated solutions

Author	#non-dom. (out of 30)
Krause et. al.	26
Berry et. al.	21
Dorini et. al.	20
Wu and Walski	19
Ostfeld and Salomons	14
Propato and Piller	12
Eliades and Polycarpou	11
Huang et. al.	7
Guan et. al.	4
Ghimire and Barkdoll	3
Trachtman	2
Gueli	2
Preis and Ostfeld	1

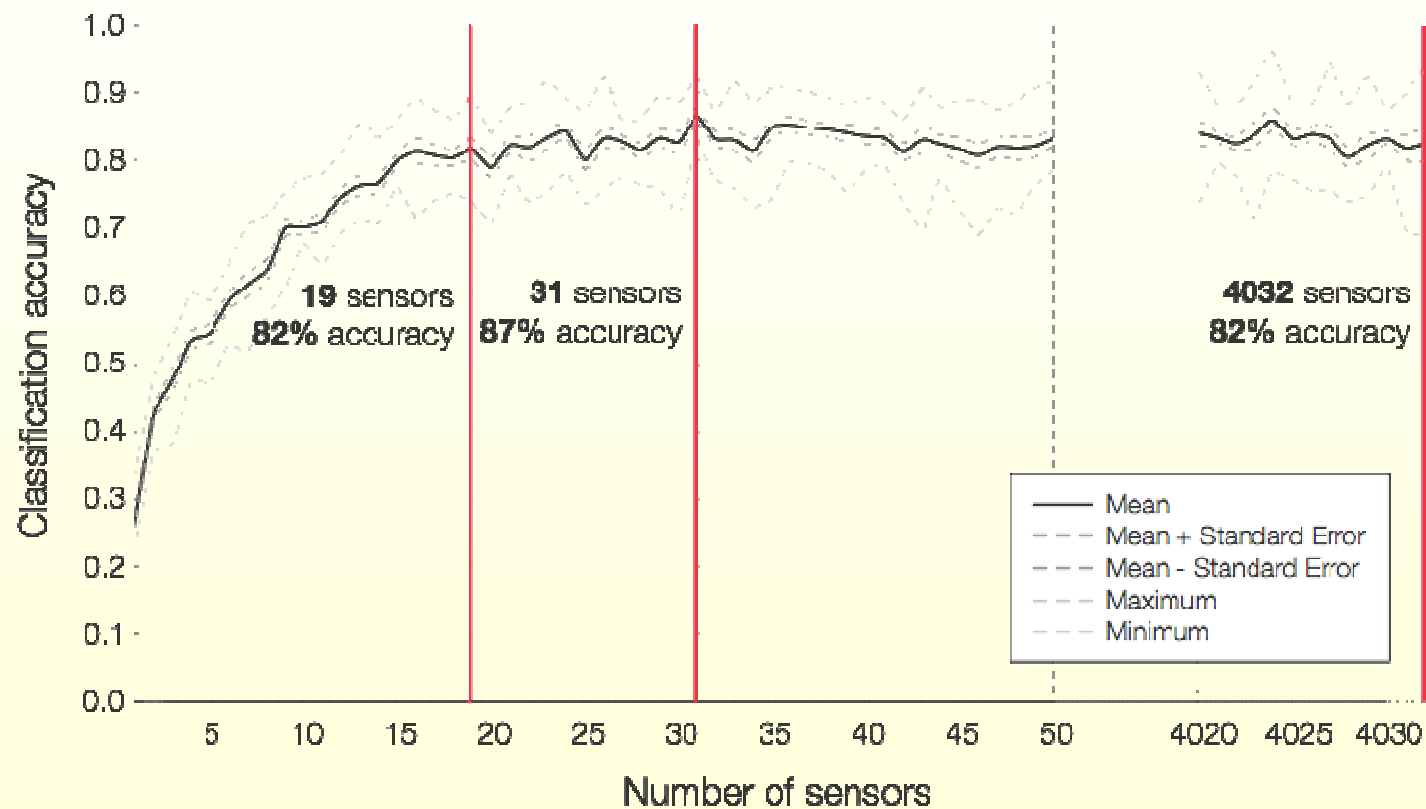
Smart Chair Prototype

[Mutlu, Krause, Forlizzi, Guestrin, Hodgins '07]

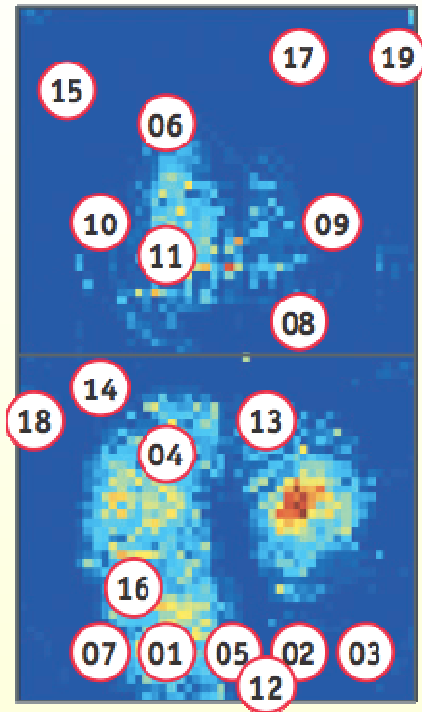
- 20 naive participants
- Robust generalization
Up to 87% accuracy in classifying 10 postures with new subjects
- Low cost
Using 19 pressure sensors instead of 4032. Reducing sensor cost from \$3K to ~\$100
- 10 Hz real-time performance
On a standard desktop computer



Near-Optimal Placement on Chair



Selected placements



Near-optimal placements shown on high-resolution pressure map



Near-optimal placements on the prototype

Summary thus far: **Optimizing information quality**

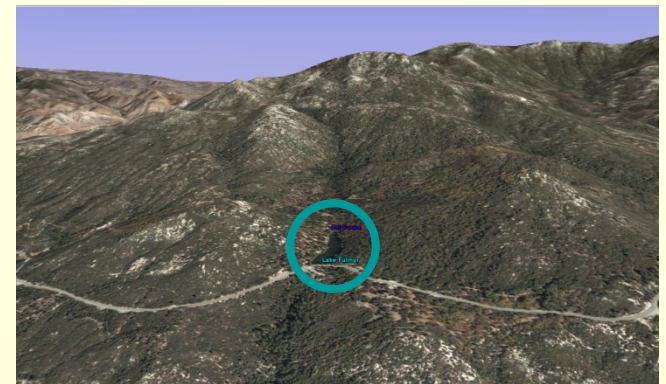
- **Greedy** algorithm for sensor placement is provably **near optimal**
 - **simple and effective** approach for finding **highly informative** sensor placements
 - **works very well on real data!**
- **Submodular functions are key in placing sensors in order to optimize information** 😊

Wireless Sensor Nodes

- In many applications, nodes use wireless links for **communication**
- No cables
 - huge cost savings
 - ease of deployment
 - simpler maintenance
 - enables mobility
 - allows us to go where no one has gone before... 😊



CMU's Intelligent Workplace



Lake Fulmor

PART II:

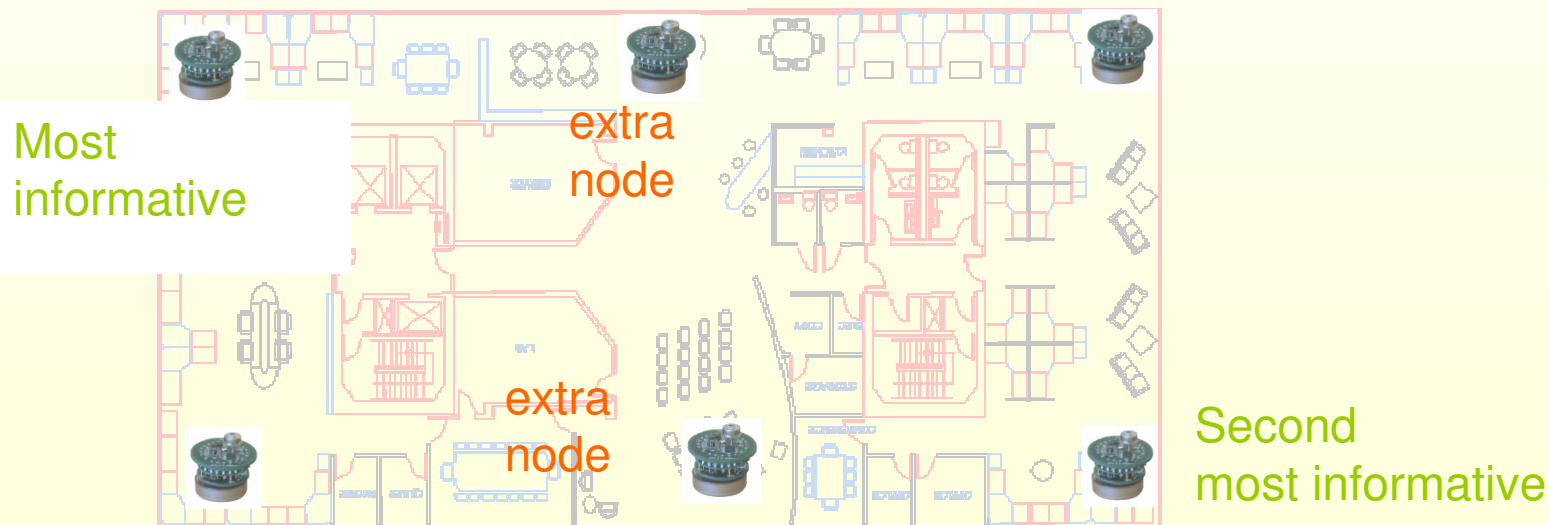
Near-Optimal Sensor Placement:

Maximizing **Information** while

Minimizing **Communication Cost**

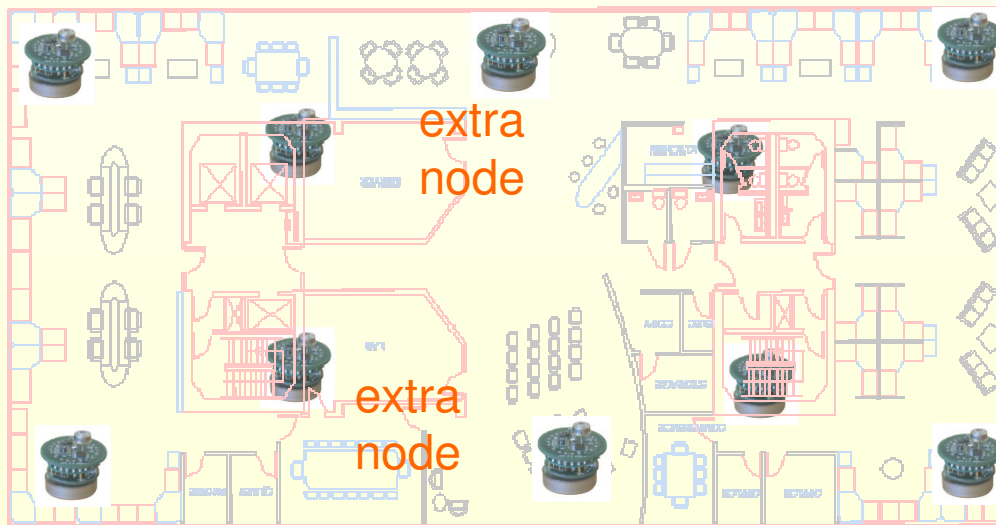
What About the Greedy Algorithm When Communication Matters?

- **Greedy-connect**: a simple heuristic
 - greedy obtains near-optimal **information quality**
 - usually selects nodes that are “far apart”
 - add **extra nodes** to guarantee **communication**



What if we used simple greedy algorithm when comm. matters?

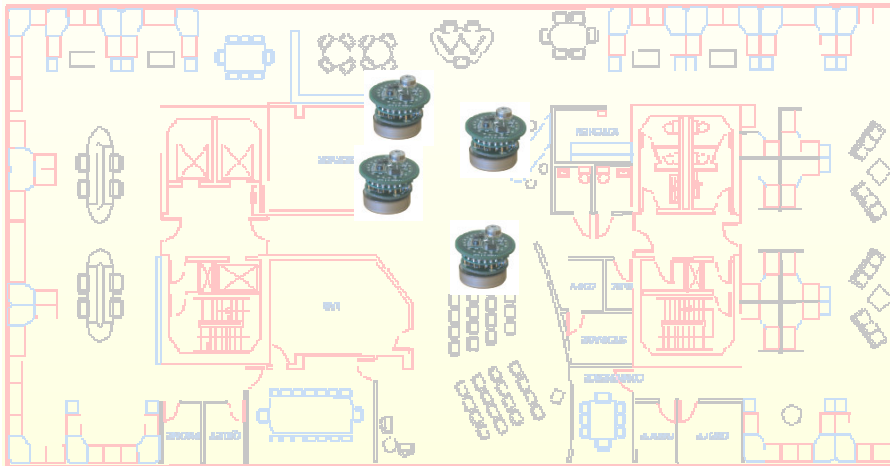
- **Greedy-connect**: a simple heuristic
 - greedy obtains near-optimal **information quality**
 - usually selects nodes that are “far apart”
 - add **extra nodes** to guarantee **communication**



But, there might be a only **slightly less** informative, but **much less** costly solution!

Trade-off: Information vs. Communication Cost

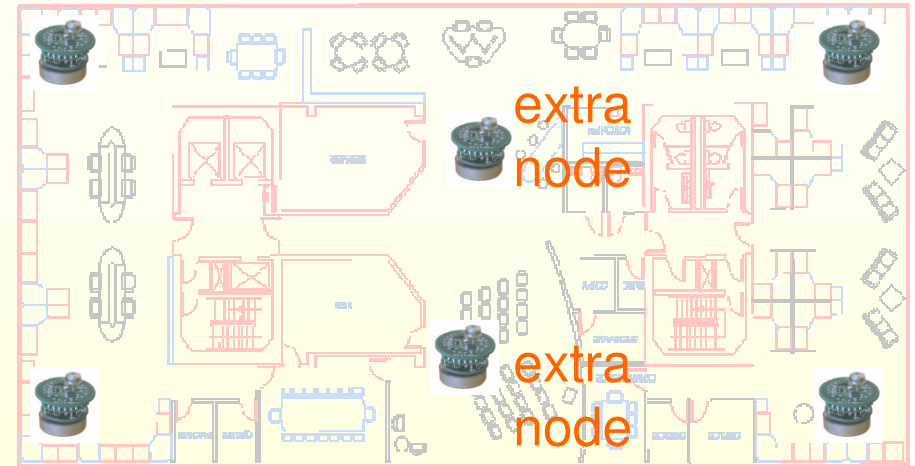
The “closer” the sensors:



efficient communication! 😊

worse information quality! ☹️

The “farther” the sensors:



better information quality! 😊

worse communication! ☹️

The pSPIEL Algorithm

[Krause, G., Gupta, Kleinberg '06]

- **pSPIEL**: Efficient, randomized algorithm
(**p**added **S**ensor **P**lacem**e**nts at **I**nformative and
cost-**E**ffective **L**ocations)
- In expectation, **both** information quality and
communication cost will be **close to optimum**
- Built a system on **real sensor nodes** for sensor
placement using pSPIEL
- Evaluated the method on **real-world sensor
placement** problems

The Placement Problem

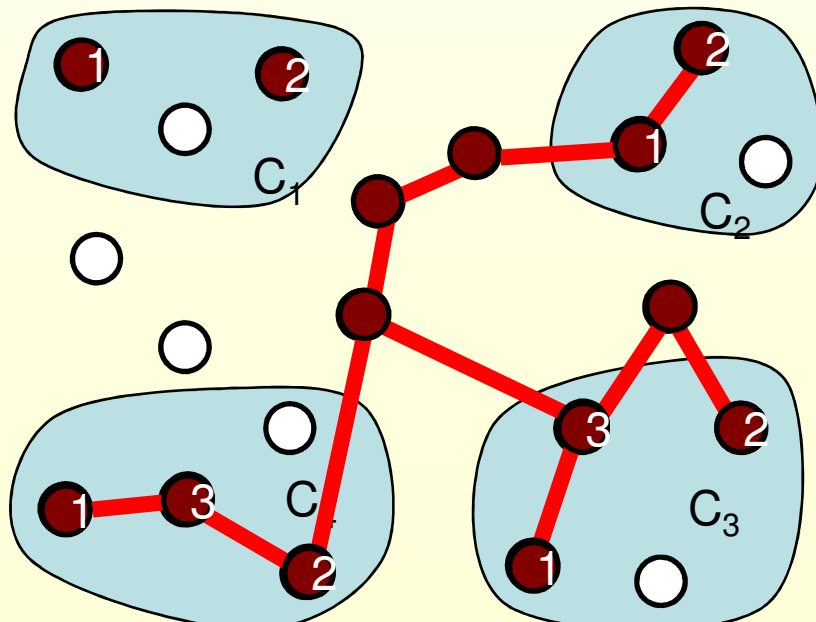
- Let V be set of locations to choose from
- For subset of locations $A \subseteq V$, let
 - $I(A)$ be **information quality** and
 - $C(A)$ be **communication cost** of placement A

- Want to optimize
 $\min C(A)$ subject to $I(A) \geq Q$

- $Q > 0$ is information quota

Our approach: *pSPIEL*

- **Decompose** sensing region into small, well-separated clusters
- Solve cardinality constrained problem **per cluster**
- **Combine** solutions using k-MST algorithm



Guarantees for Sensor Placement

Theorem:

pSPIEL finds a tree T with

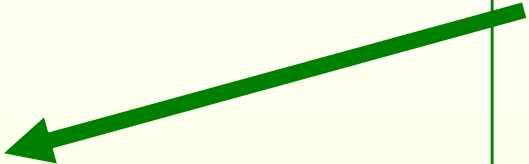
info. quality

$$I(T) \geq \Omega(1) \text{OPT}_{\text{quality}},$$

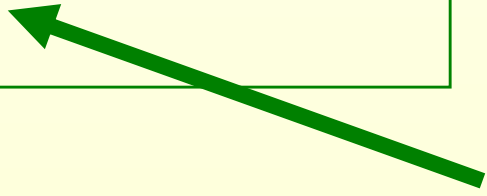
comm. cost

$$C(T) \leq O(\log |V|) \text{OPT}_{\text{cost}}$$

const.
factor
approx.
info.



log
factor
approx.
comm.
cost

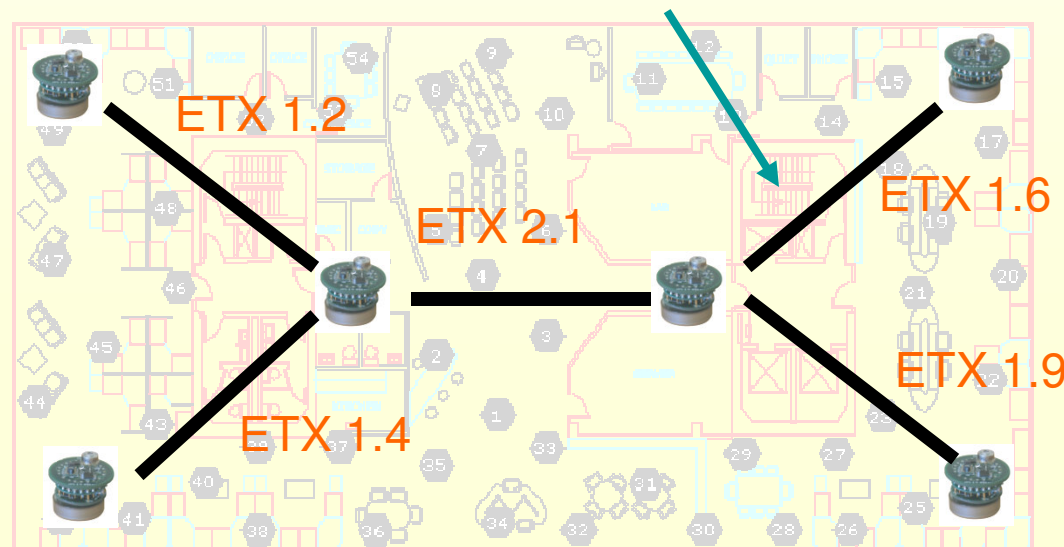


Summary of the Approach

- ❑ Use small, short-term “bootstrap” deployment to **collect** some **data** or obtain **expert model** (e.g., from the EPA)
- ❑ **Learn/Compute models** for **information quality** and **communication cost**
- ❑ **Optimize tradeoff** between information quality and communication cost using ***pSPIEL***
- ❑ **Deploy sensors**
- ❑ If desired, collect more data and continue with step 2

Communication Cost: a Simple Definition

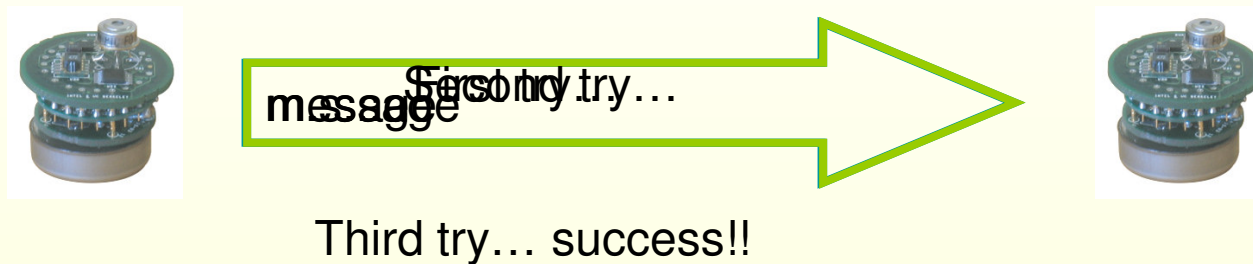
- Message loss requires retransmission
- This depletes the sensor's battery quickly
- **Communication cost for two sensors** means **expected number of transmissions (ETX)**
- **Communication cost for placement** is sum of all ETXs along routing tree



Total cost = 8.2

How to Compute ETX

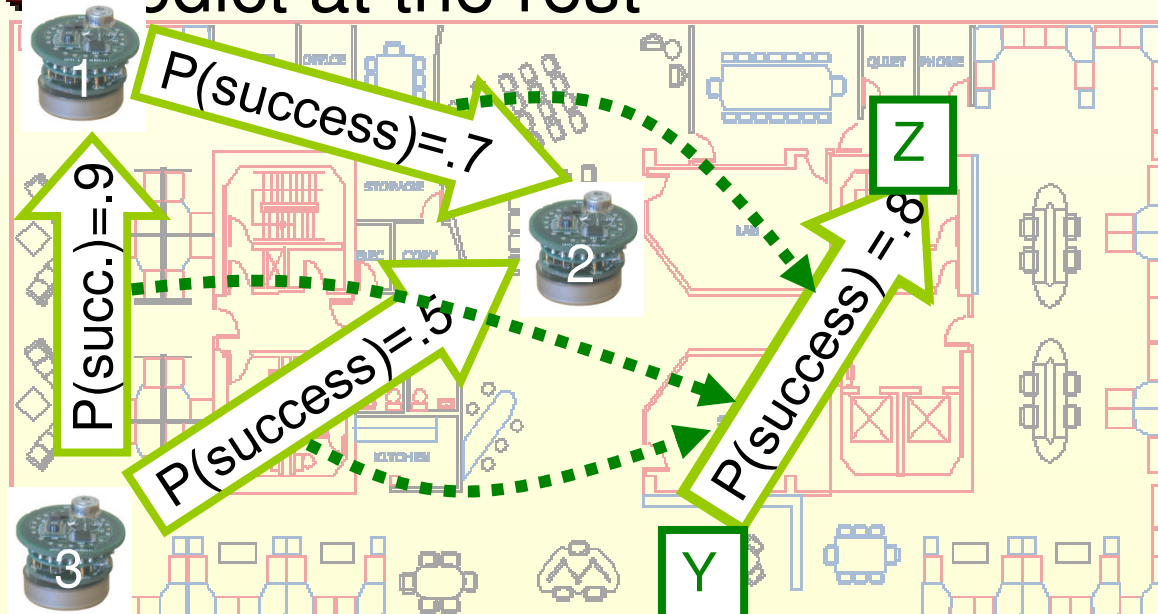
- Pick two sensors and collect transmission logs



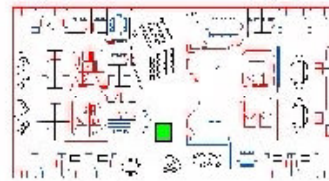
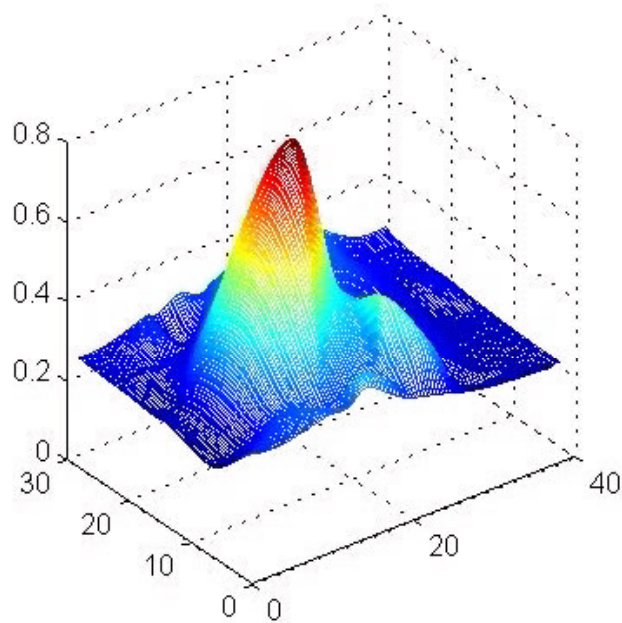
- If we do this long enough, we estimate e.g.
 $P(\text{success}) = 1/3$, and hence $ETX = 1/(1/3) = 3$

Predicting Communication Cost

- Must answer: **If I were to place sensors at Y and Z, what would the link quality be?**
- **A regression problem:**
 - Measure link qualities for some locations
 - Predict at the rest

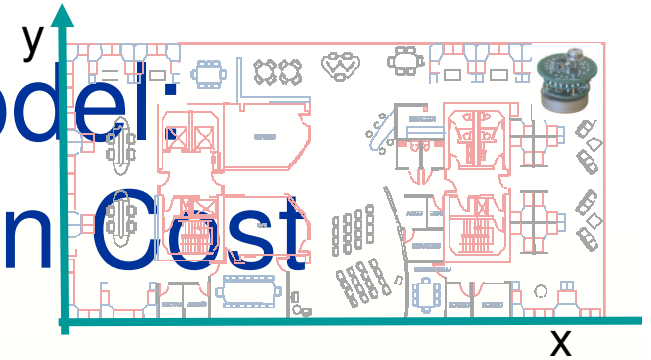


Interpolated Real Link Quality Data

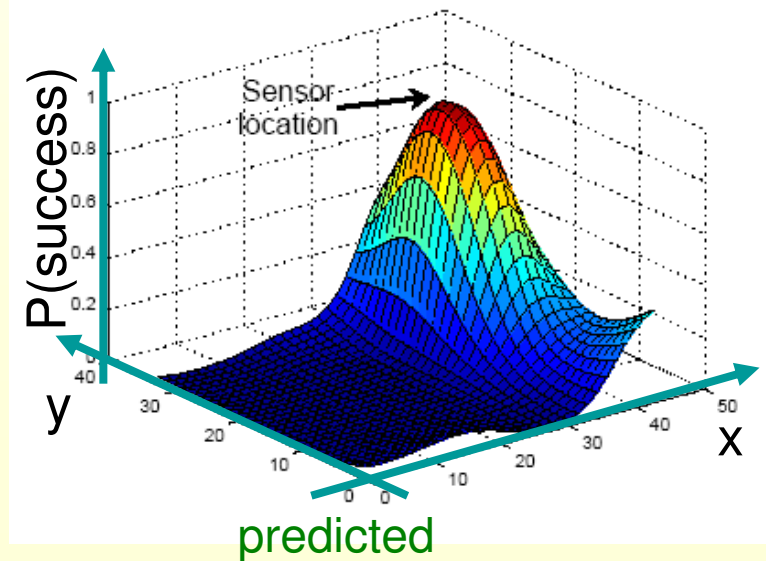
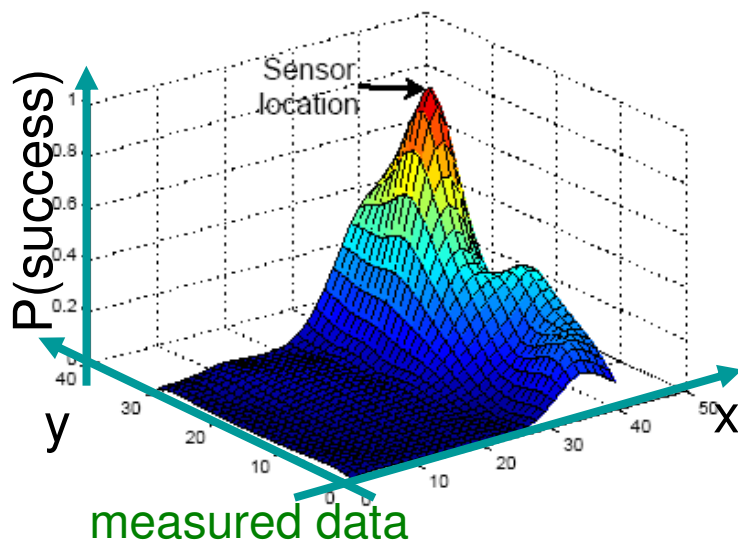


- Complex surface
- Looks very little like $1/r^2$
 - a typical assumption
- Observe
 - “corridor” effect
 - external interference
 - ...
- How can we model this phenomena?

Learned Model Communication Cost



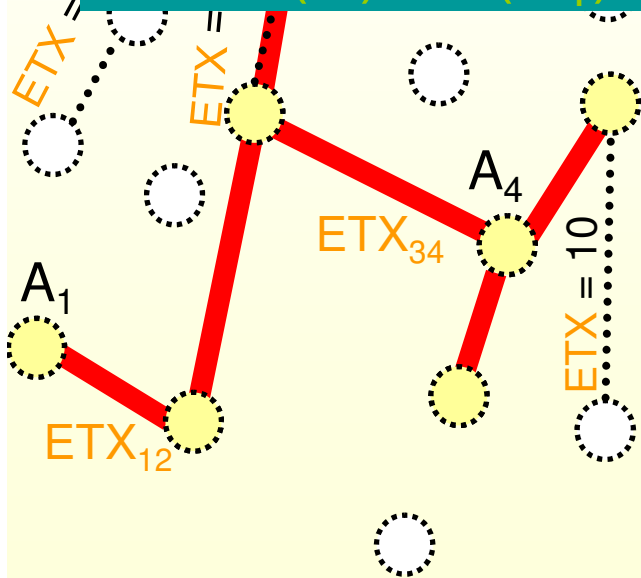
- Complex data
- Represent using probabilistic model
 - extension of non-parametric Gaussian process used for temperature
 - main difference: link qualities in $[0,1]$



Minimizing Communication Cost While Maximizing Information Quality

First: **simplified** case, where each sensor provides **independent information**:

$$I(A) = I(A_1) + I(A_2) + I(A_3) + I(A_4) + \dots$$



$$\min_A C(A)$$

$$C(A) =$$

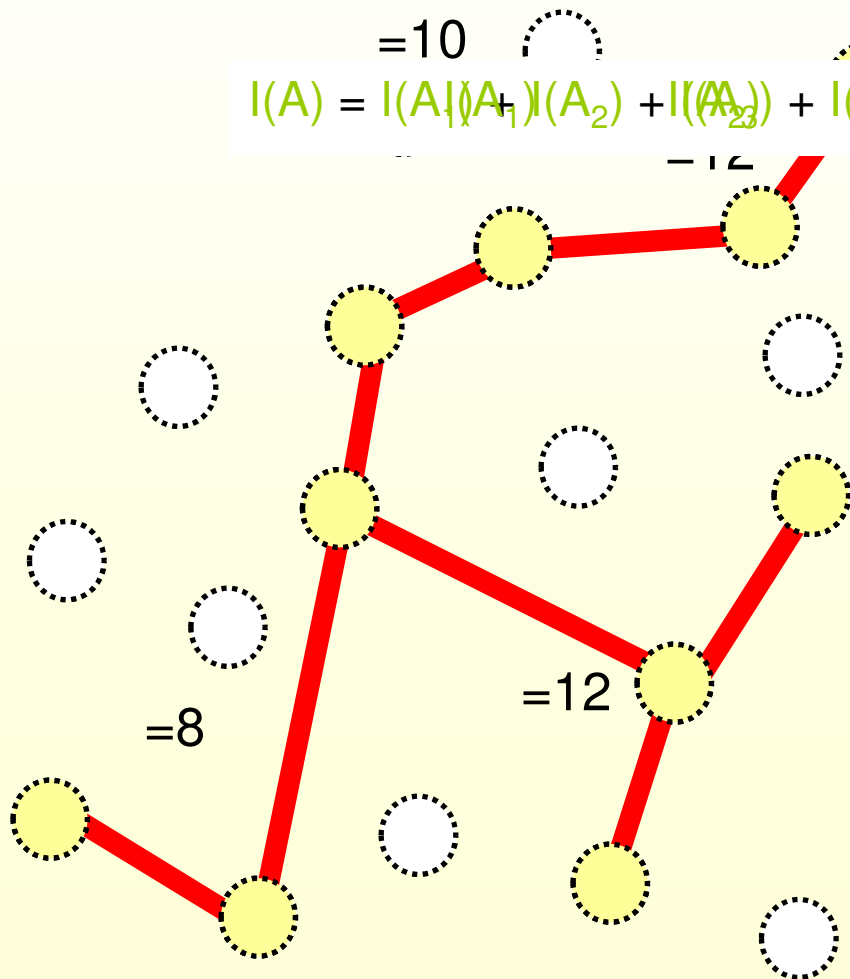
locations are informative:

$$I(A) \geq Q \quad + \quad + \quad + \dots$$

$$I(A) = I($$

$$\cup \quad \cup \quad \cup \dots)$$

Quota Minimum Steiner Tree (Q-MST) Problem



$$I(A) = I(A_1) + I(A_2) + I(A_3) + \dots + I(A_4)$$

Problem:

Find the cheapest tree that collects that least Q reward:

$$+ + + \dots \geq Q$$

Perhaps could use to solve our problem!!! 😊

NP-hard... 😞

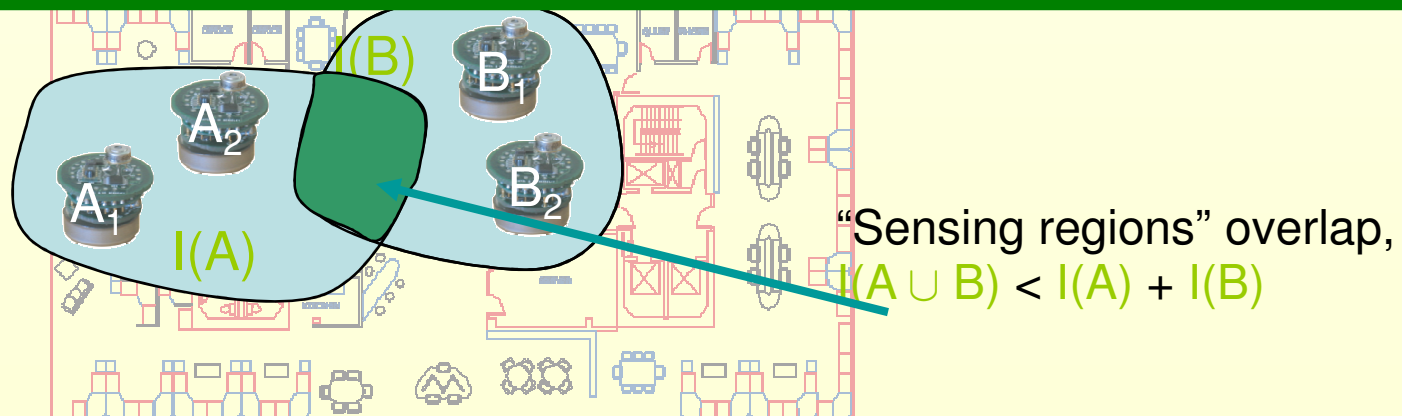
but very well studied [Blum, Garg, ...]

Constant factor 2 approximation algorithm available! 😊

Getting Closer...

- Q-MST algorithm works if $I(A)$ is *modular*, i.e., if A and B disjoint, $I(A \cup B) = I(A) + I(B)$
- **Makes no sense** for sensor placement!
 - Close by sensors are **not** independent

- For sensor placement, I is *submodular*
 $I(A \cup B) \leq I(A) + I(B)$



Must Solve a New Problem

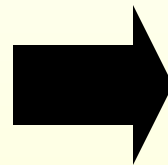
insight: our sensor problem has additional structure! ☺

● Want to optimize

● min $C(A)$ subject to $I(A) > Q$

if sensors provide
independent information

$$I(A) = I(A_1) + I(A_2) + I(A_3) + \dots$$



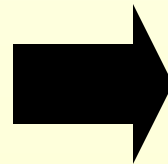
a modular problem

solve with Q-MST ☺

but info not independent ☹

sensors provide
submodular information

$$I(A_1 \cup A_2) \leq I(A_1) + I(A_2)$$



a new open problem!

submodular steiner tree

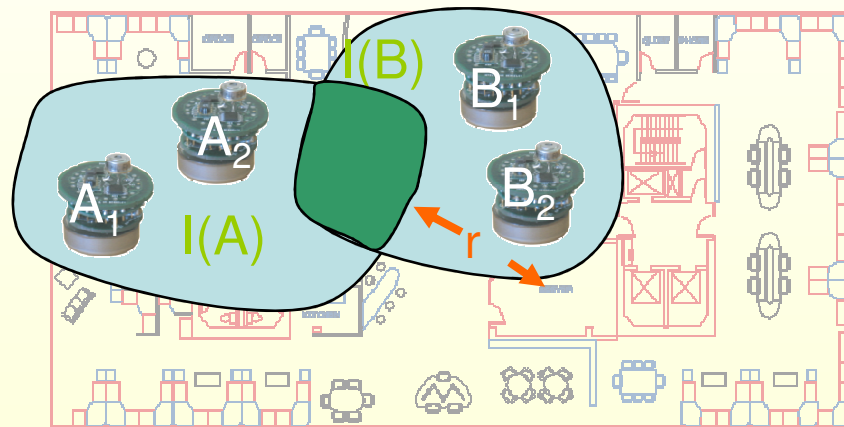
strictly harder than Q-MST

generalizes existing problems

e.g., group steiner

Independence via Separability

- If A, B are placements closeby, then $I(A \cup B) < I(A) + I(B)$
- If A, B are placements, at least r apart, then $I(A \cup B) \approx I(A) + I(B)$

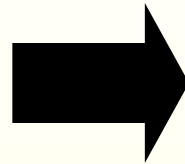


- Sensors that are **far apart** are **approximately independent**
 - We showed **locality is empirically valid**

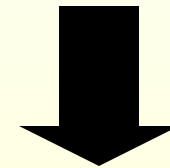
Outline: pSPIEL

submodular
steiner tree
with locality

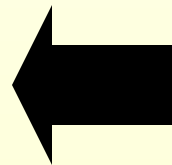
$$I(A_1 \cup A_2) \leq I(A_1) + I(A_2)$$



approximate by a modular problem:
for nodes A
sum of rewards $A \approx I(A)$



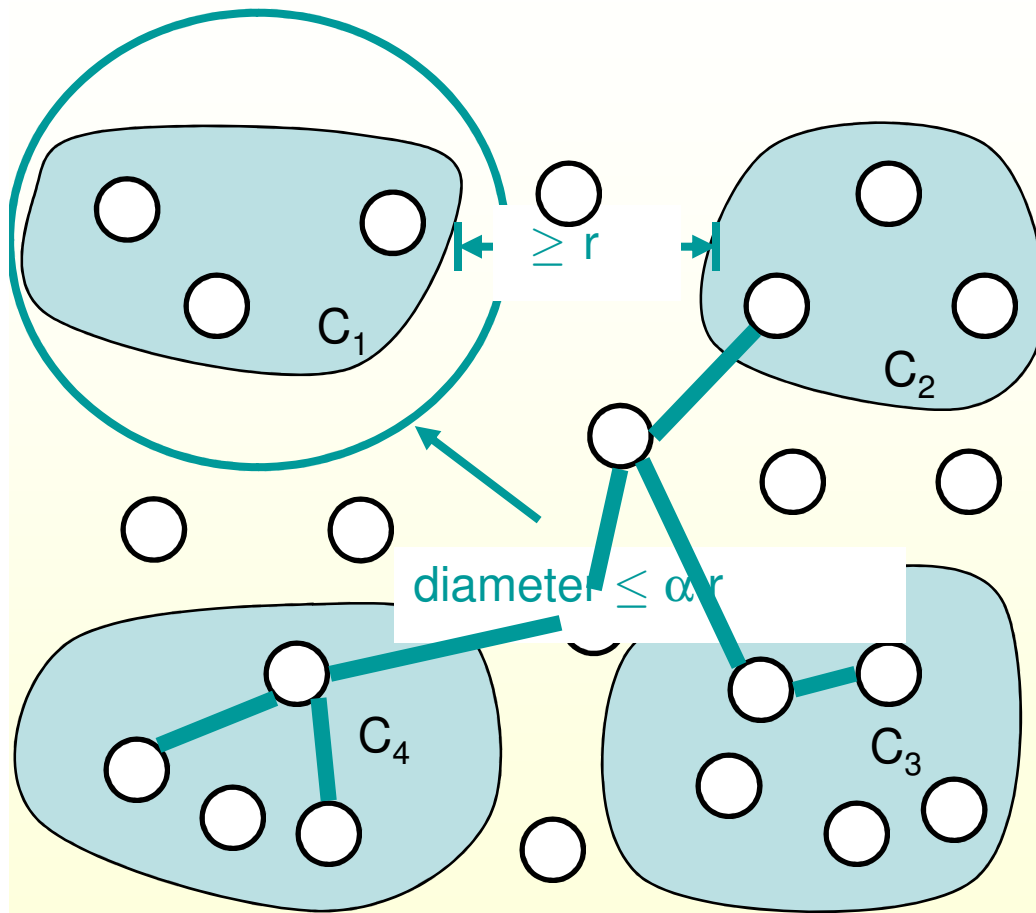
obtain solution of
original problem
(prove it's good)



solve modular approximation
with Q-MST

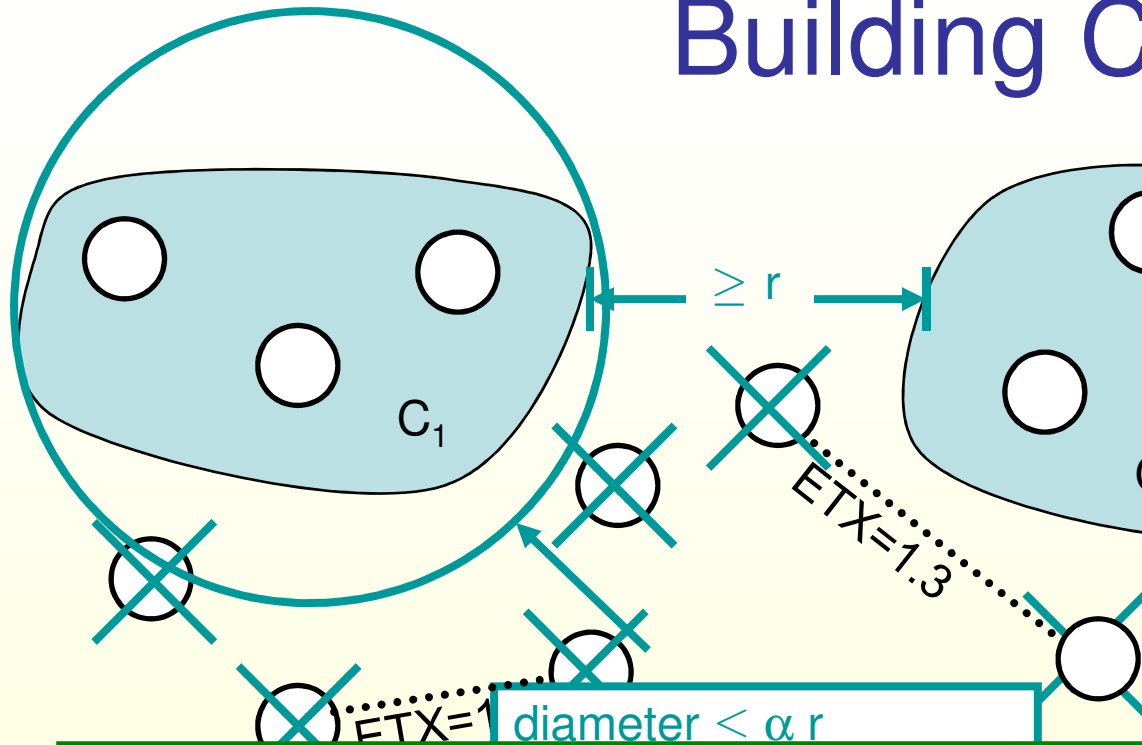
use off-the-shelf
Q-MST solver

Overview: pSPIEL



- Build **clusters** over possible sensor locations
 - well-separated
 - not too large
- **Throw away** locations **not in clusters**
- **Information additive between clusters!** 😊
 - **separability or locality!!!**
- Use Q-MST to decide **which nodes** to use from **each cluster** and **how to connect** them

pSPIEL: Step 1 Building Clusters



● **Throw away locations not in clusters → not allowed to place sensors there**

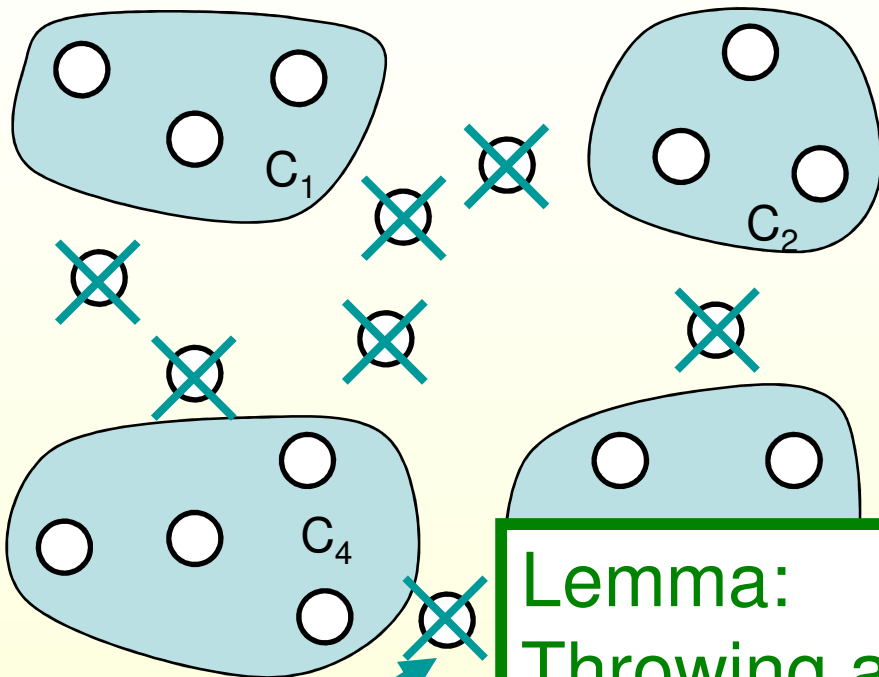
Lemma: [Gupta et al. '03]

Such padded decompositions (small, well-separated clusters) can be found efficiently

Throw away at most $\frac{1}{2}$ of the possible locations

pSPIEL: Step 2

Throwing Away Nodes



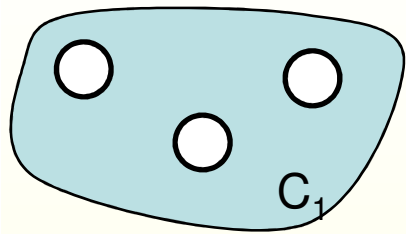
- We throw out unpadded possible sensor locations
- at most $\frac{1}{2}$ of all locations

was this one too good to let go?

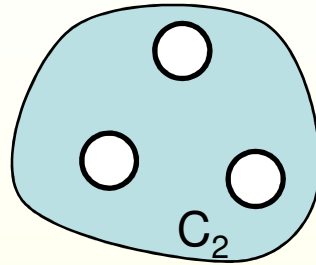
Lemma:
Throwing away non-clustered locations doesn't hurt **information quality** too much in expectation! 😊

proof uses submodularity and an "uncrossing" procedure

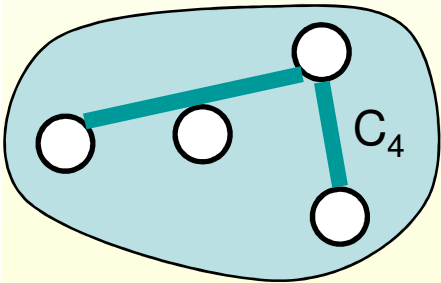
pSPIEL: Well-Separated Small Clusters



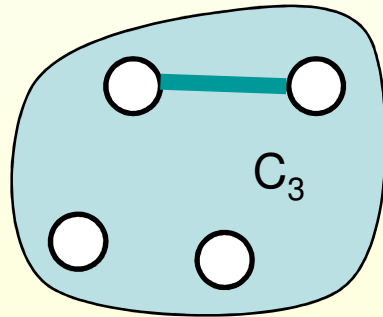
$I(A_2)$



$I(A_3)$



$I(A_4)$



- Under **separability**, clusters are **mostly independent!**

$$I(A_2 \cup A_3 \cup A_4) \approx I(A_2) + I(A_3) + I(A_4)$$

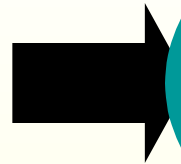
- Diameters are **small**, we **don't care** about **comm. cost within cluster!**

- use greedy-connect in cluster

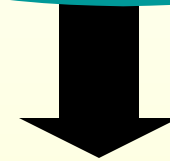
Outline: pSPIEL

submodular
steiner tree
with locality

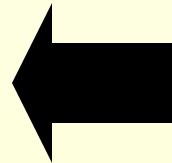
$$I(A_1 \cup A_2) \leq I(A_1) + I(A_2)$$



approximate by a modular problem
(MAG):
for nodes A
sum of rewards $A \approx I(A)$



obtain solution of
original problem
(prove it's good)



solve modular approximation
with Q-MST

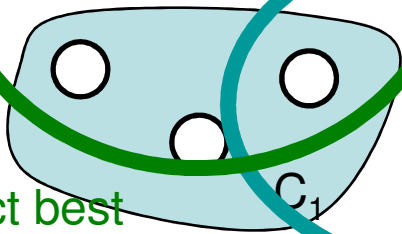
use off-the-shelf
Q-MST solver

pSPIEL: Step 3

Modular Approximation Graph

How do we define weights and rewards?

Consider a cluster:



connect best nodes

most importantly, additive rewards:

greedy chains in clusters

- Order nodes in “order of importance”
 - greedy defines order
- Build a modular approximation graph (MAG)
 - edge weights and node rewards \rightarrow solution in MAG \approx solution of original problem

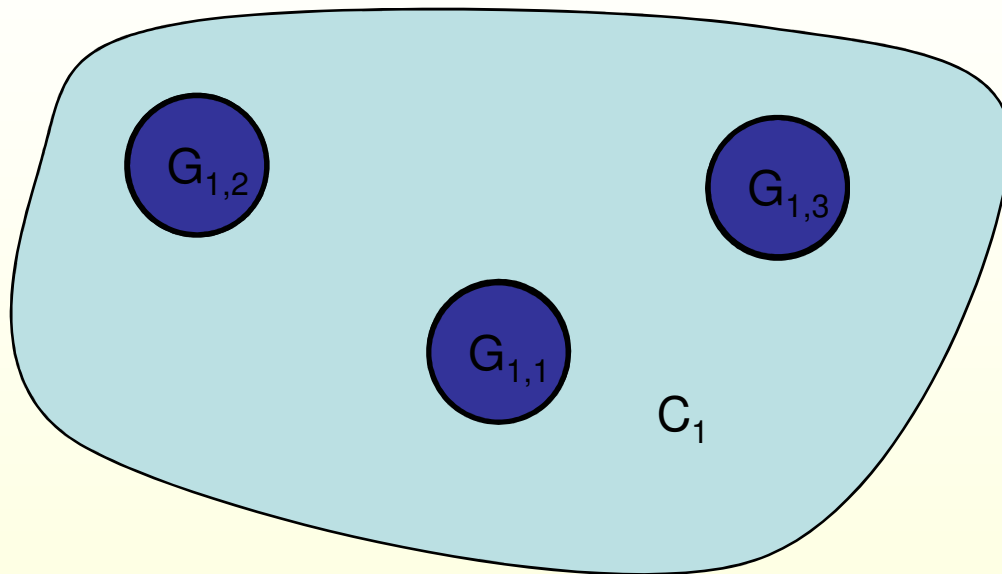
Info: $I(G_{2,1} \cup G_{2,2} \cup G_{3,1} \cup G_{4,1} \cup G_{4,2}) \approx$

+ + + +

Cost: $C(G_{2,1} \cup G_{2,2} \cup G_{3,1} \cup G_{4,1} \cup G_{4,2}) \approx$

+ + +

pSPIEL: Greedy Algorithm within Cluster



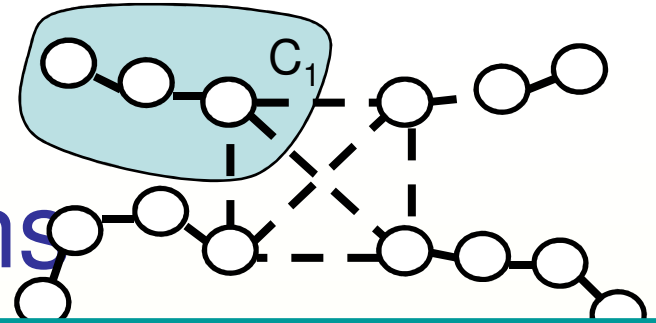
Want to find sets with highest **information quality** in cluster

Run the greedy algorithm in every cluster, i.e., add most informative element

Again Theorem:

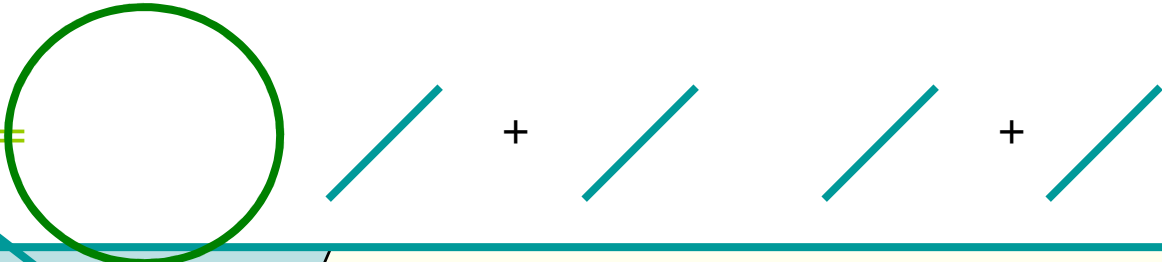
Greedy subsets of size k are at most a constant factor $(1-1/e)$ worse in **Information Quality** than the best such set!
e.g., pick nodes $G_{1,1}$ & $G_{1,2}$ 63% of optimal 2 nodes
in practice, much better

pSPIEL: Step Greedy Chains



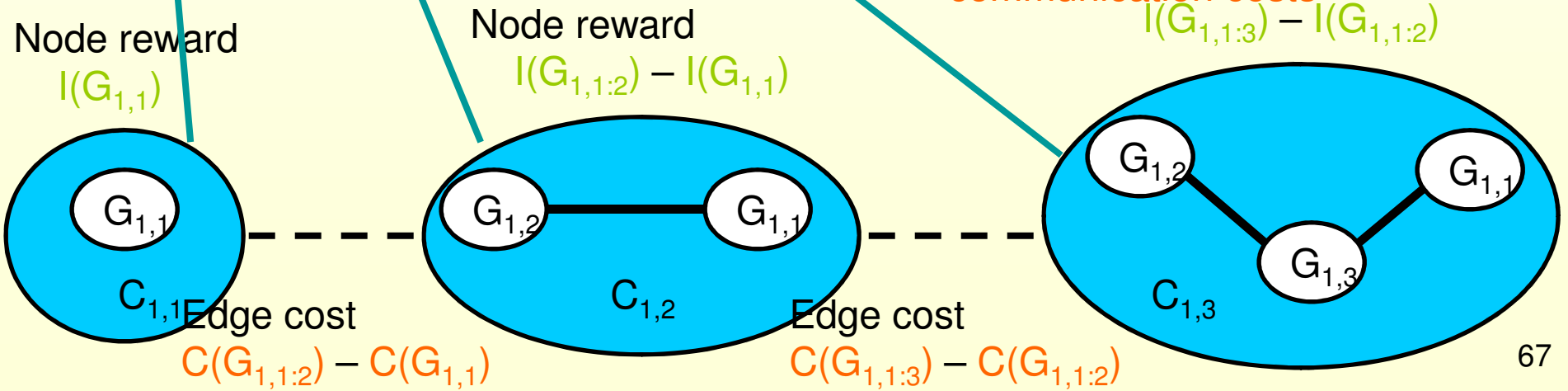
Key property: clusters organized into chain

$$R(C_{1,1}) + R(C_{1,2}) + R(C_{1,3}) =$$



Get a modular functions via telescopic sums

Same trick for communication costs
Node reward $I(G_{1,1:3}) - I(G_{1,1:2})$



pSPIEL: Modular Approximation Graph

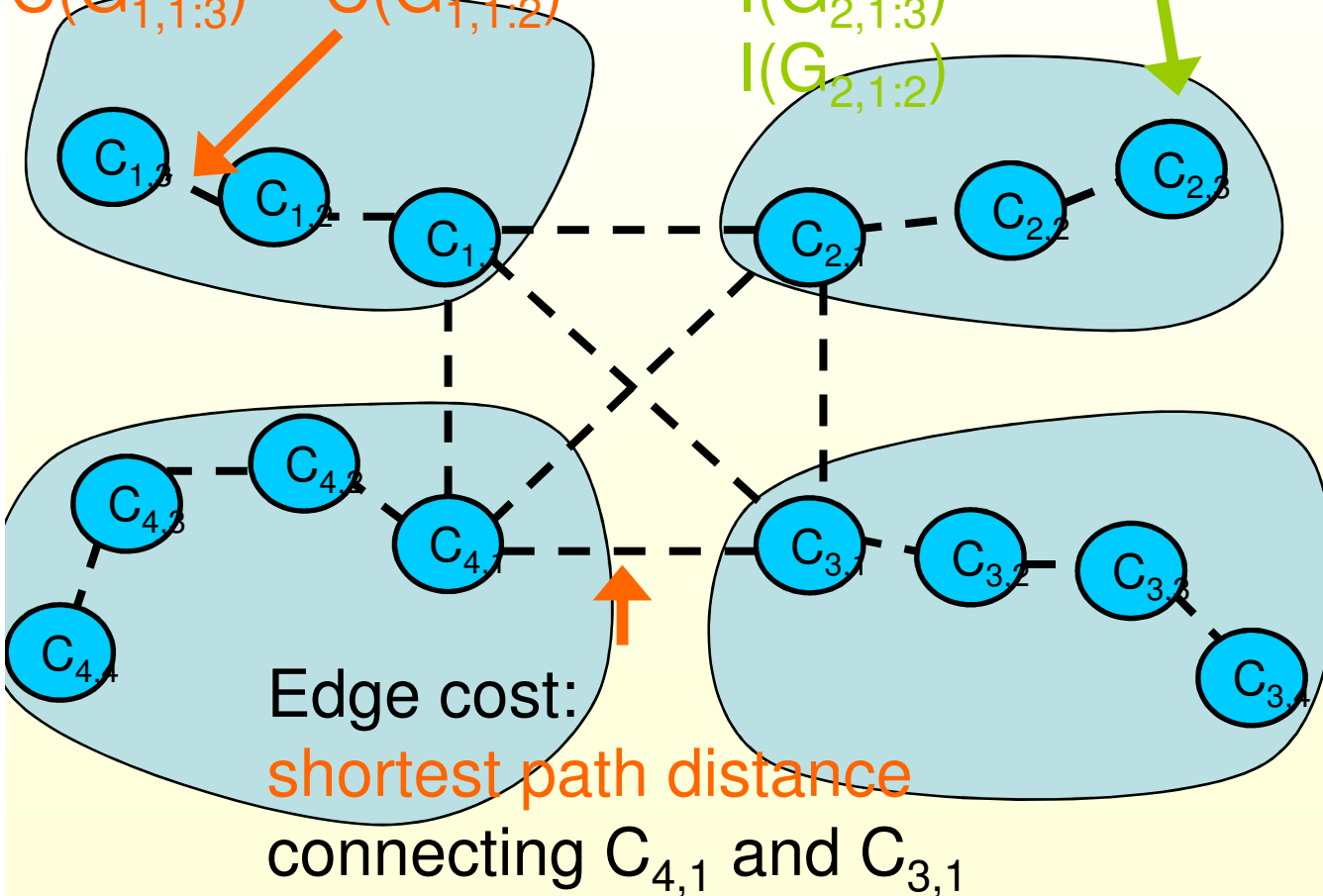
Edge cost:

$$C(G_{1,1:3}) - C(G_{1,1:2})$$

Node reward

$$I(G_{2,1:3}) - I(G_{2,1:2})$$

modular
approximation
graph (MAG)
combines chains

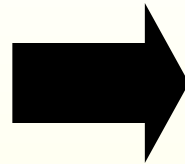


approximates
original
optimization
problem! 😊

Outline: pSPIEL

submodular
steiner tree

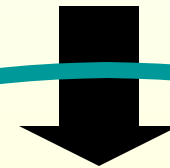
$$I(A_1 \cup A_2) \leq I(A_1) + I(A_2)$$



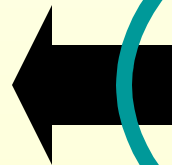
approximate by a modular problem
(MAG):

for nodes A

sum of rewards $A \approx I(A)$



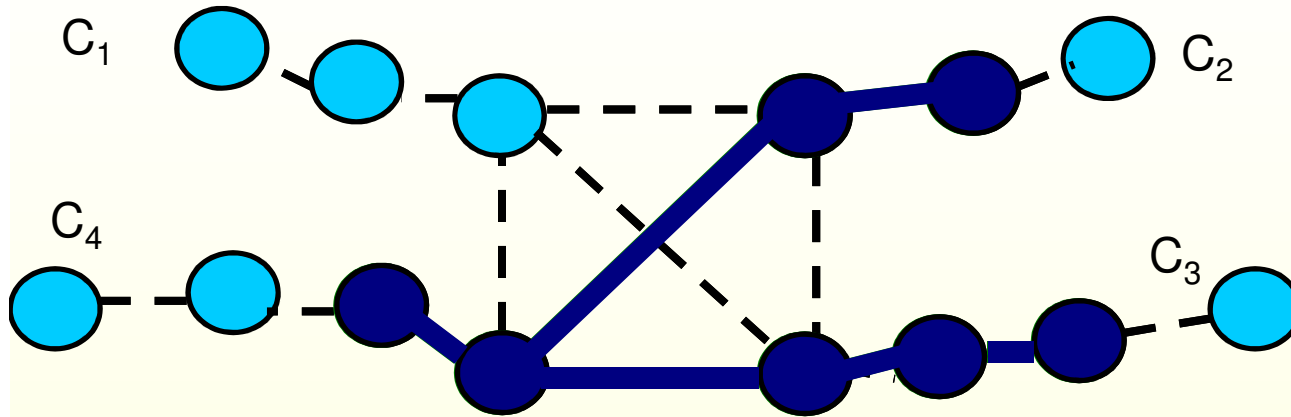
obtain solution of
original problem
(prove it's good)



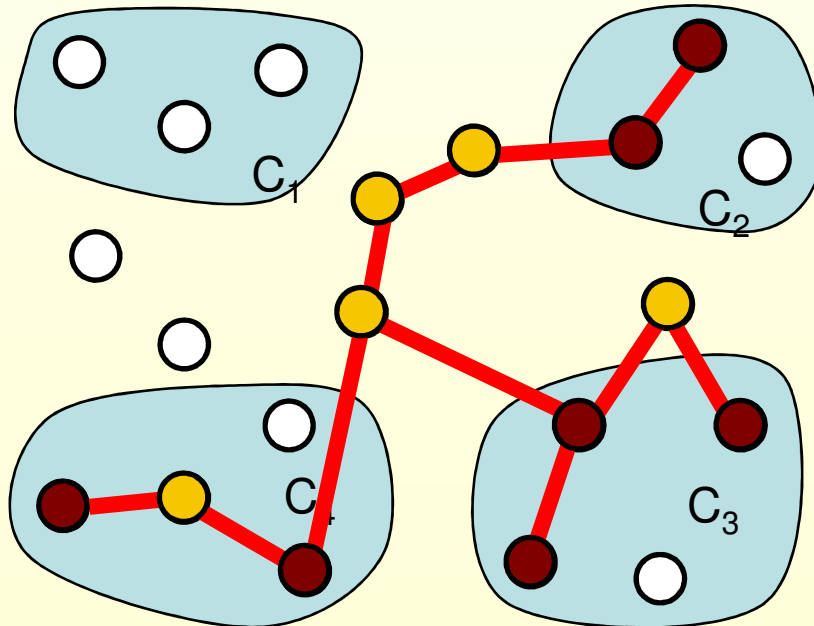
solve modular approximation
with Q-MST

use off-the-shelf
Q-MST solver

pSPIEL: Using Q-MST



tree in MAG \rightarrow solution in original graph

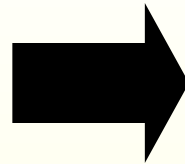


Q-MST on MAG \rightarrow
solution to original
problem! 😊

Outline: pSPIEL

submodular
steiner tree

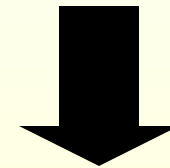
$$I(A_1 \cup A_2) \leq I(A_1) + I(A_2)$$



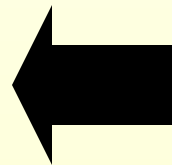
approximate by a modular problem
(MAG):

for nodes A

sum of rewards $A \approx I(A)$



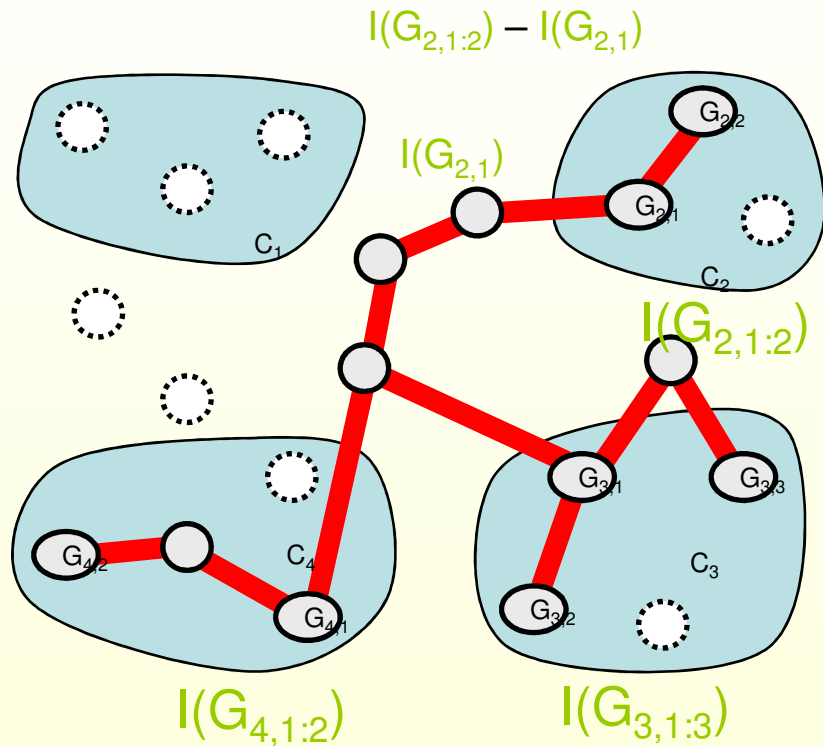
obtain solution of
original problem
(prove it's good)



solve modular approximation
with Q-MST

use off-the-shelf
Q-MST solver

pSPIEL: Solving Sensor Placement Problem



Inside a cluster:

$$I(G_{2,1:2}) = \quad +$$

Total reward by Q-MST:

$$I(G_{2,1:2} \cup G_{3,1:3} \cup G_{4,1:2}) \approx \text{locality!} \geq Q$$

- Want to optimize
 - $\min C(A)$ subject to $I(A) \geq Q$

Proof of $\approx \min C(A)$:
near opt. Q-MST &
small cluster diameter \rightarrow
comm. not too
expensive in cluster

Guarantees for Sensor Placement

Theorem:

pSPIEL finds a tree T with

info. quality

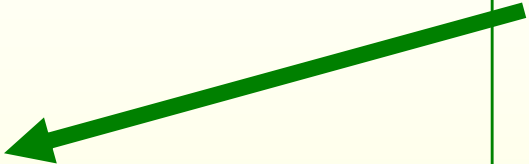
$$I(T) \geq \Omega(1) \text{OPT}_{\text{quality}},$$

comm. cost

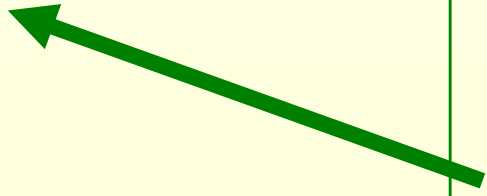
$$C(T) \leq O(r \log |V|) \text{OPT}_{\text{cost}}$$

r depends on locality property

const.
factor
approx.
info.



log
factor
approx.
comm.
cost



Summary of the Approach

1. Use small, short-term “bootstrap” deployment to **collect** some **data** or **expert model** (e.g., from the EPA)
2. **Learn/Compute models** for **information quality** and **communication cost**
3. **Optimize tradeoff** between information quality and communication cost using ***pSPIEL***
4. **Deploy sensors**
5. If desired, collect more data and continue with step 2

Implemented at CMU...

- Implemented on Tmote Sky motes from MotelV
- Collect **measurement** and **link** information and send to base station
- We can now deploy nodes, learn models and come up with placements!

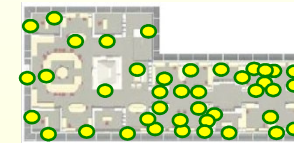
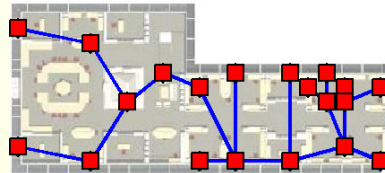


Proof of Concept Study

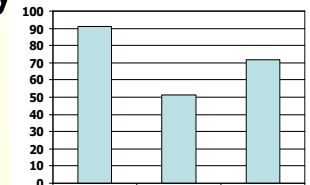
CMU's Intelligent Workplace



● Learned model from short deployment of 46 sensors at the Intelligent Workplace



accuracy



Time

learned GPs for light field & link qualities

deployed 2 sets of sensors: pSPIEL and manually selected locations

evaluated both deployments on 46 locations





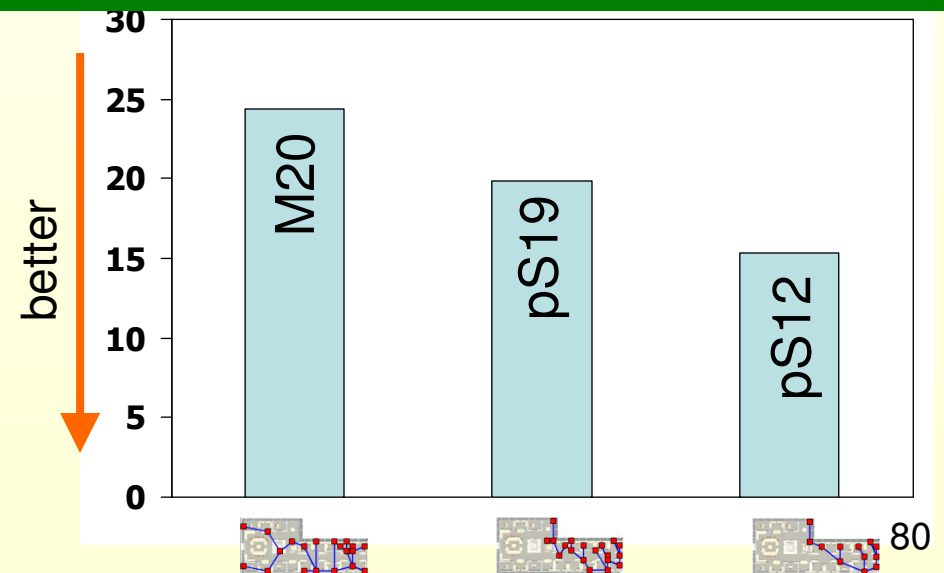
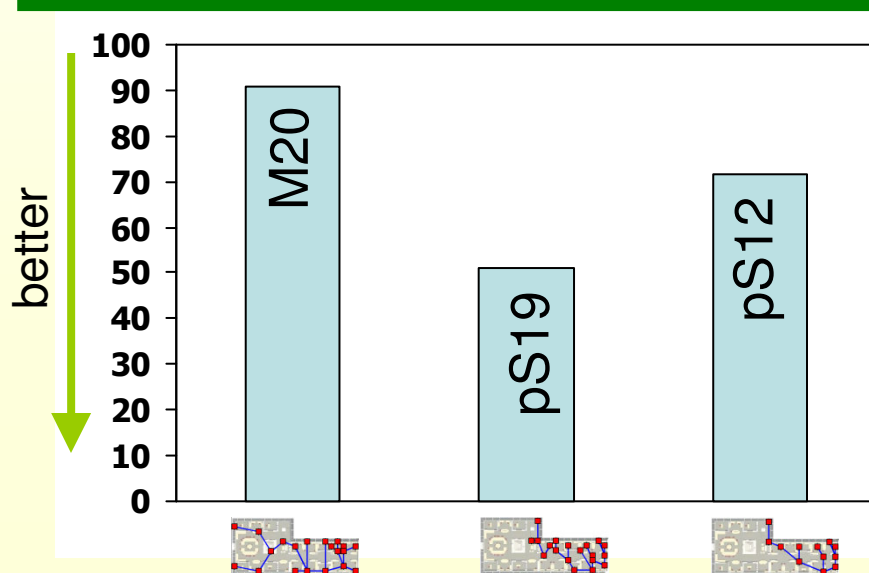


accuracy on
46 locations

Proof of Concept Study



- *pSPIEL* improved solution over intuitive manual placement:
 - 50% better prediction and 20% less comm. cost, or
 - 20% better prediction and 40% less comm. cost
- Poor placements can hurt a lot!
 - Good solution can be unintuitive



Conclusions

- **Unified approach** for deploying wireless sensor networks – **uncertainty is fundamental**
 - models for phenomena, link qualities, and optimization alg.
- ***pSPIEL***: Efficient, randomized algorithm **optimizes tradeoff**: info. quality and comm. cost with **strong guarantees**
 - Proved both **info. quality** and **comm. cost** close to optimum
- Built a **complete system** on Tmote Sky motes, deployed sensors, evaluated placements
- ***pSPIEL* significantly outperforms** alternative methods

Conclusions

- **Submodular functions are cool!**

- Design very effective algorithms, exploit this problem structure
- Simple setting → Greedy algorithm
- Constraints (comm., adversary, path,...) → Beyond greedy, but still exploit submodular fns

- **Not just sensor placement**

- Observation selection, feature selection, experimental design, ...

- **Algorithms actually work on real world problems! :-)**

- Real sensor deployment, water distribution competition, built smart chair,...

The End