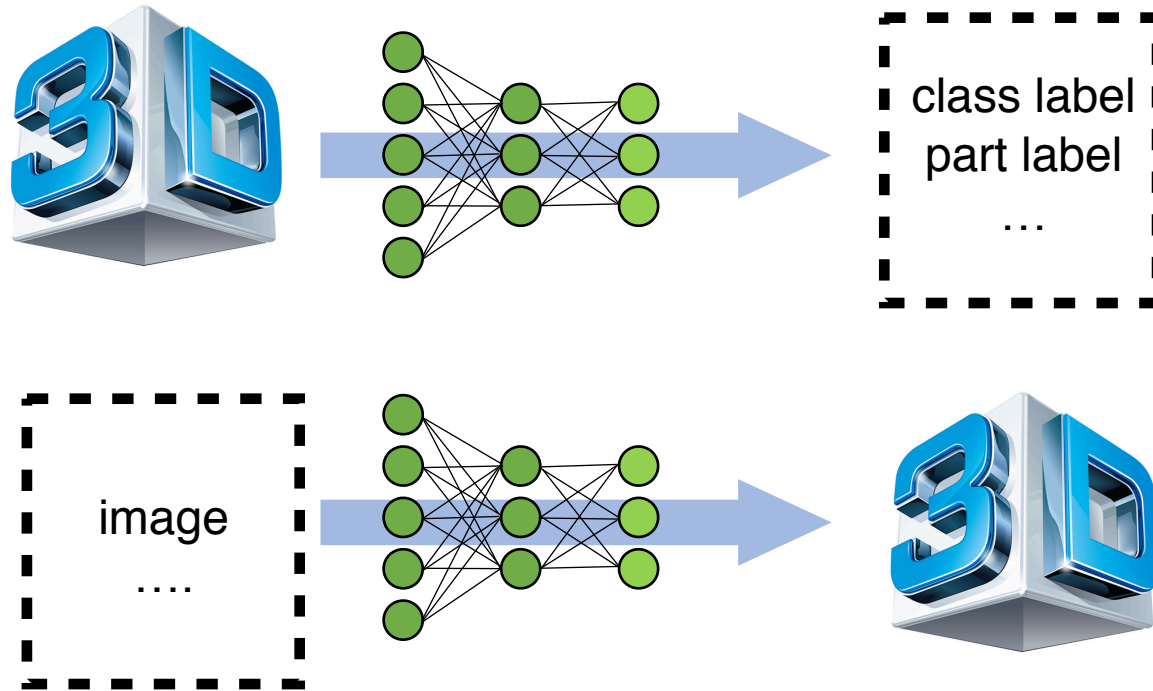


CS468: 3D Deep Learning on Point Cloud Data



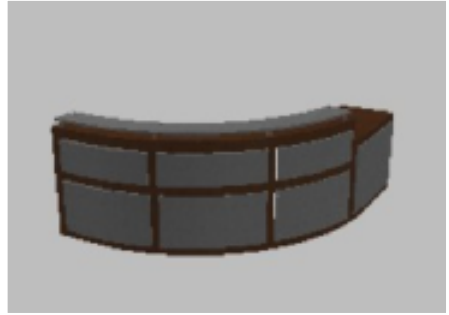
Hao Su
Stanford
University

May 10, 2017

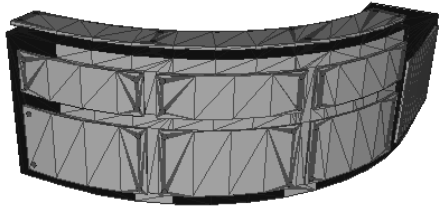
Agenda

- **Point cloud generation**
- Point cloud analysis

Pipeline



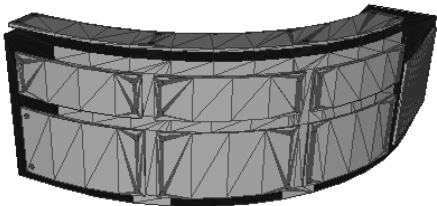
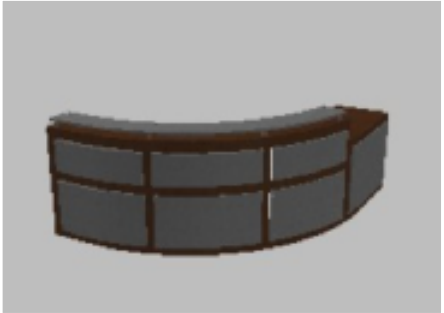
render



Pipeline

2K object categories
200K shapes
~10M image/point set pairs

render



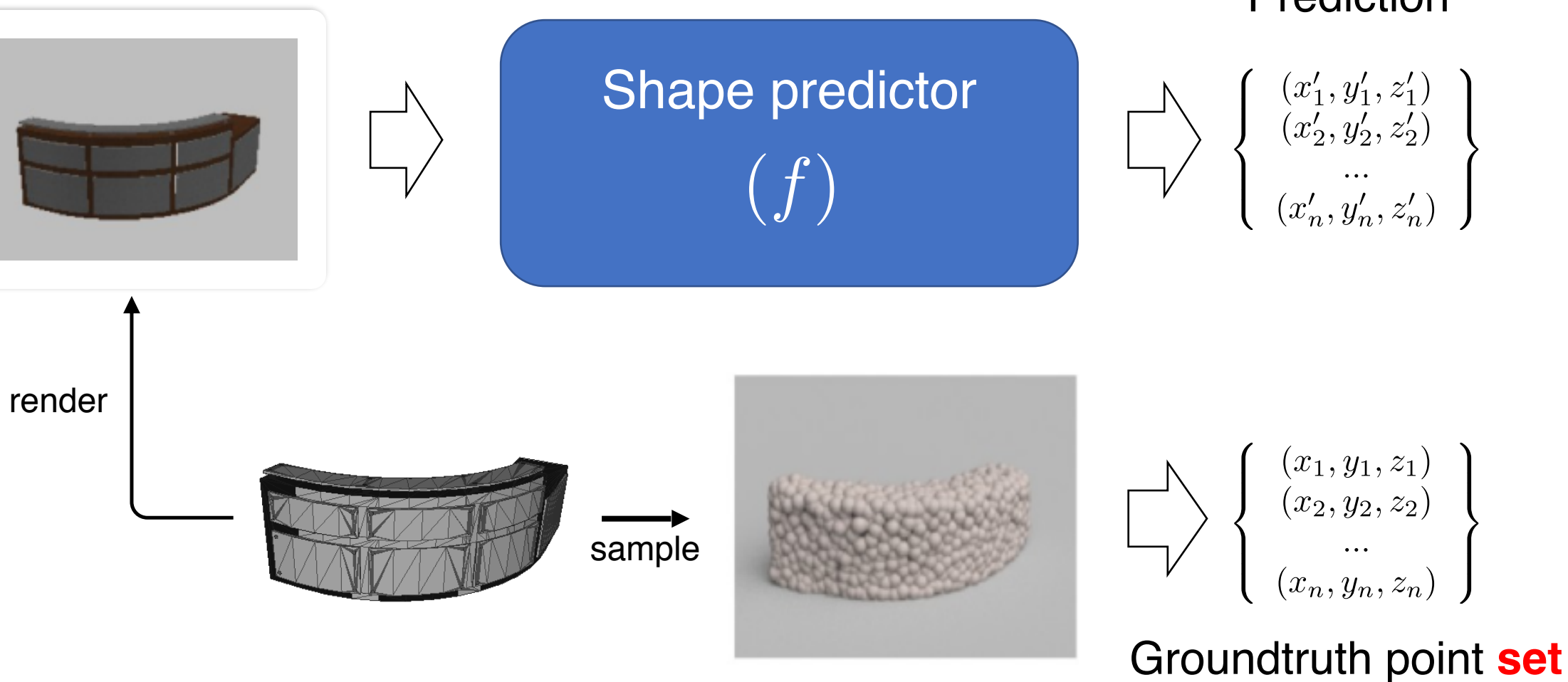
sample



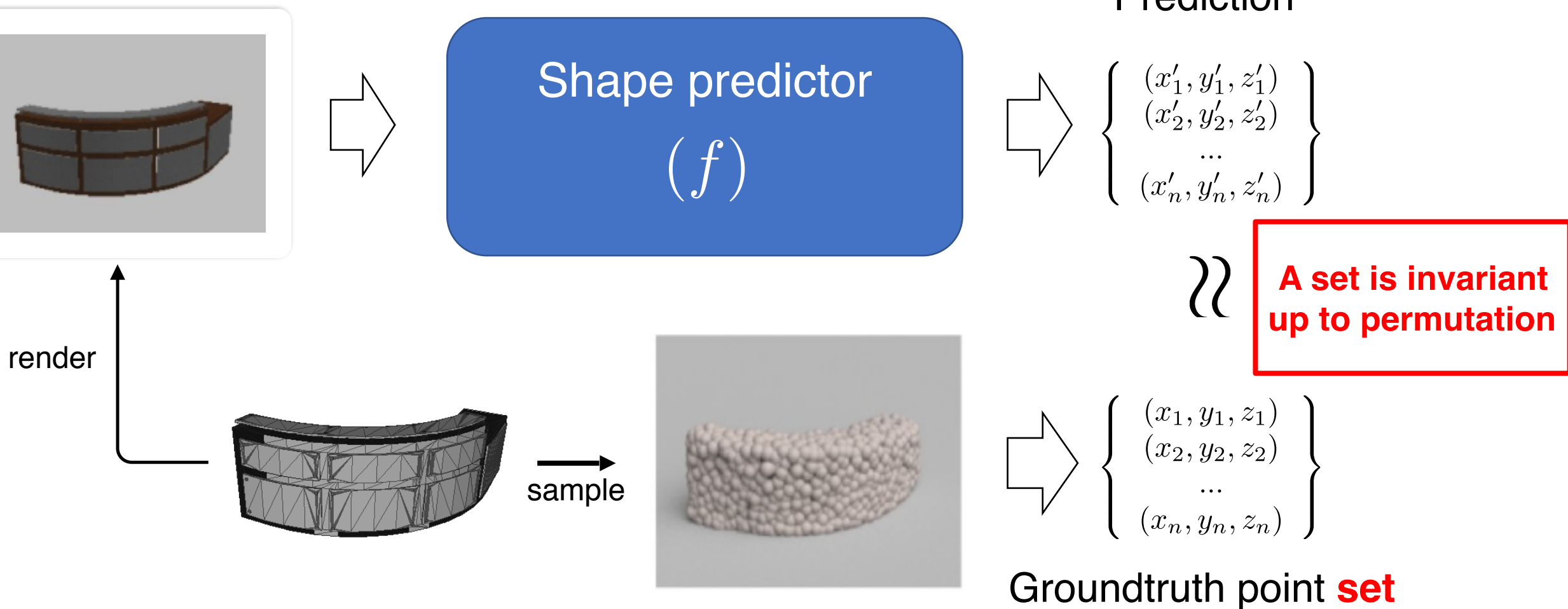
$$\left\{ \begin{array}{c} (x_1, y_1, z_1) \\ (x_2, y_2, z_2) \\ \dots \\ (x_n, y_n, z_n) \end{array} \right\}$$

Groundtruth point **set**

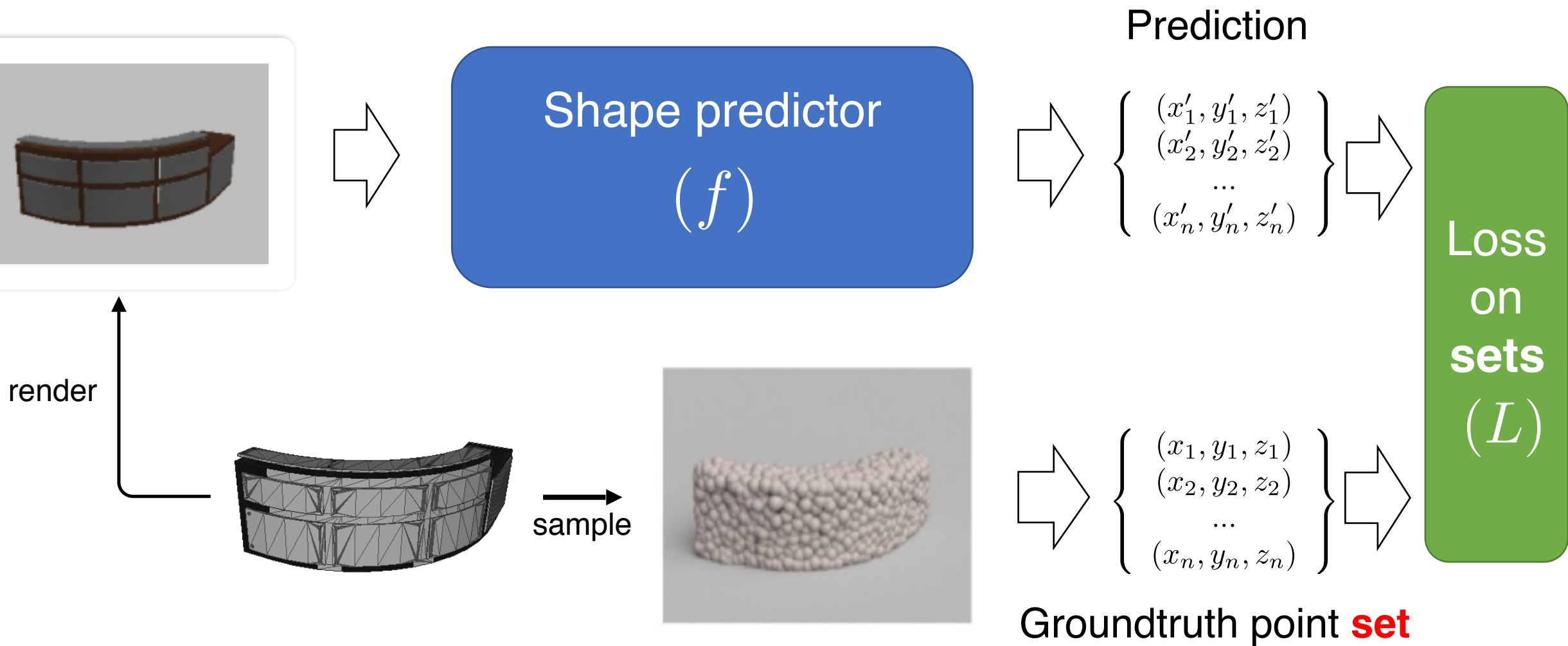
Pipeline



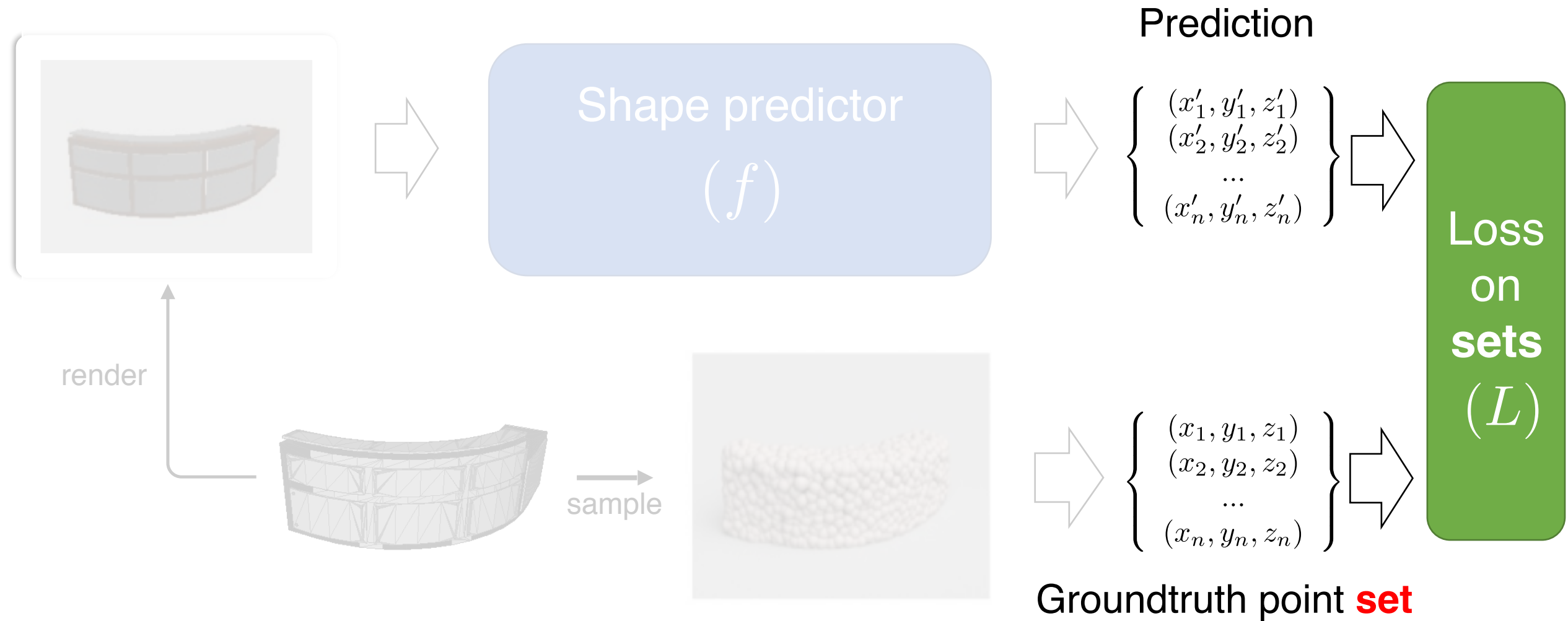
Pipeline



Pipeline

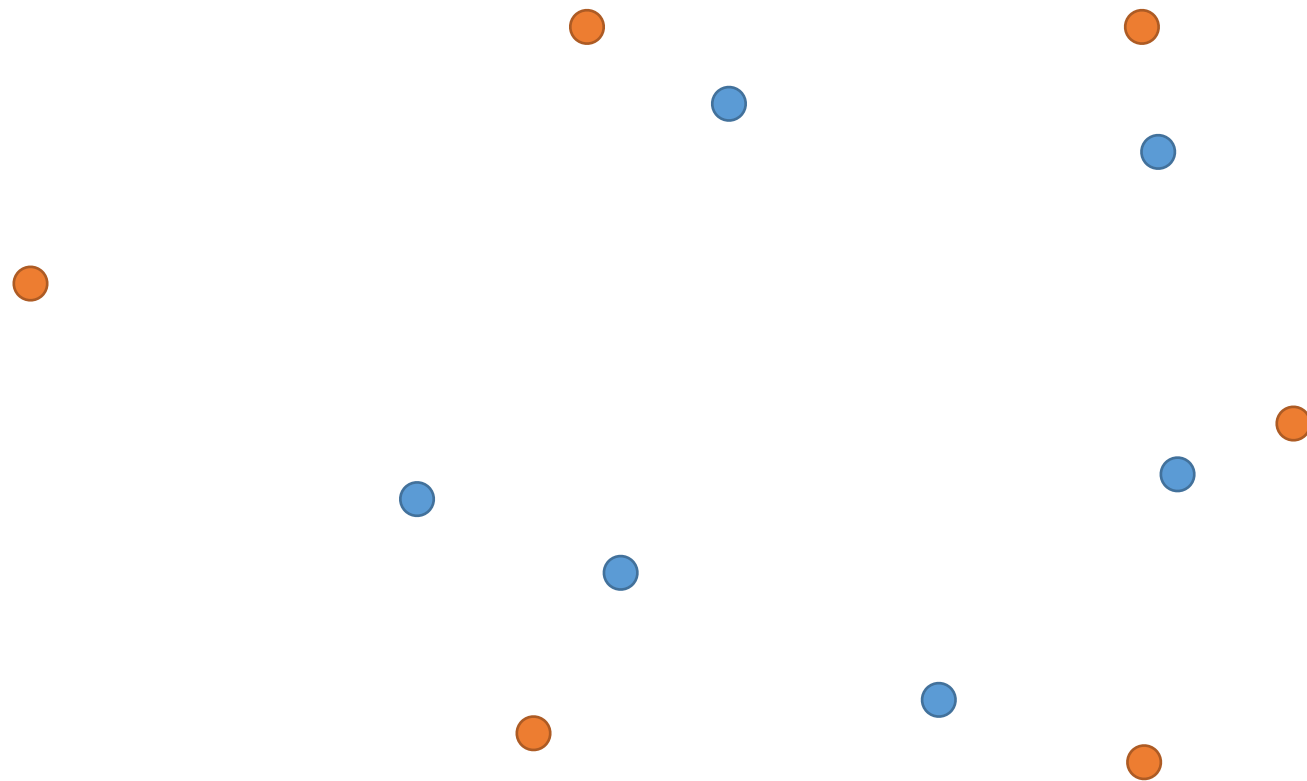


Pipeline



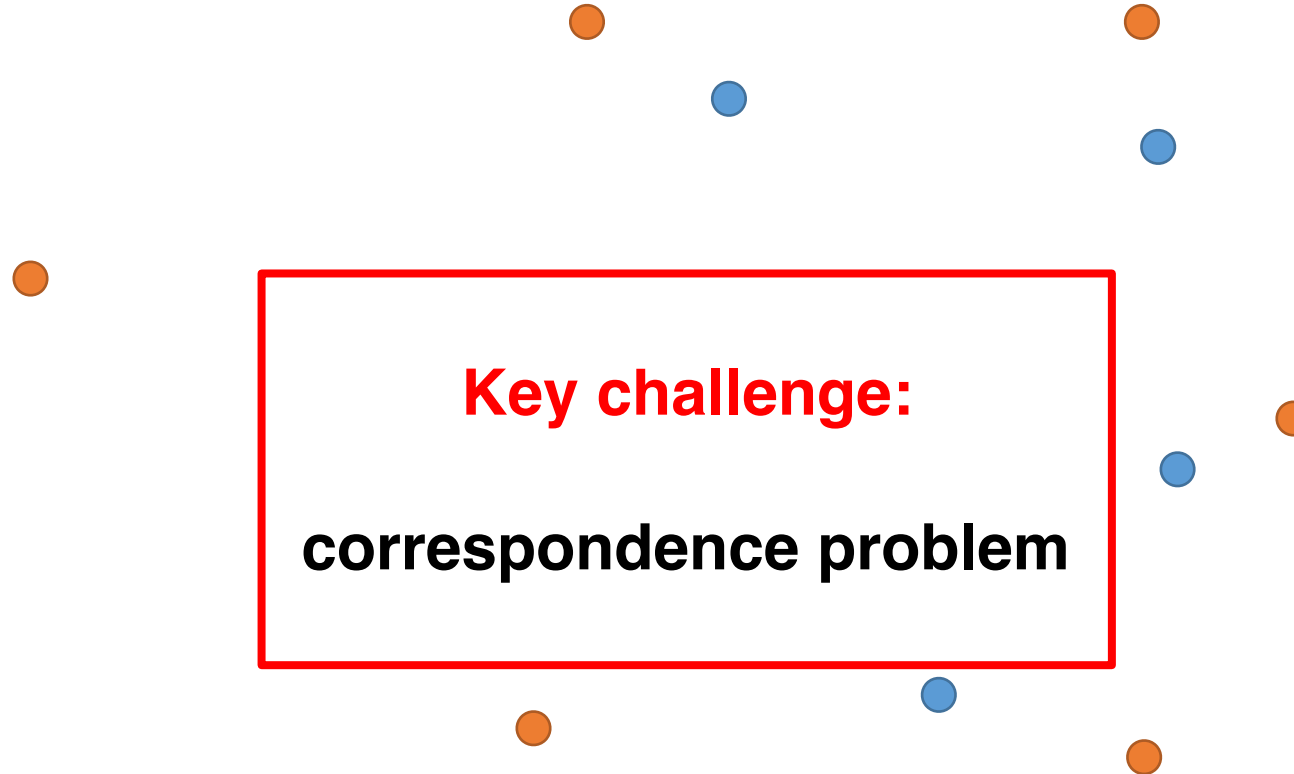
Set comparison

Given two sets of points, measure their discrepancy



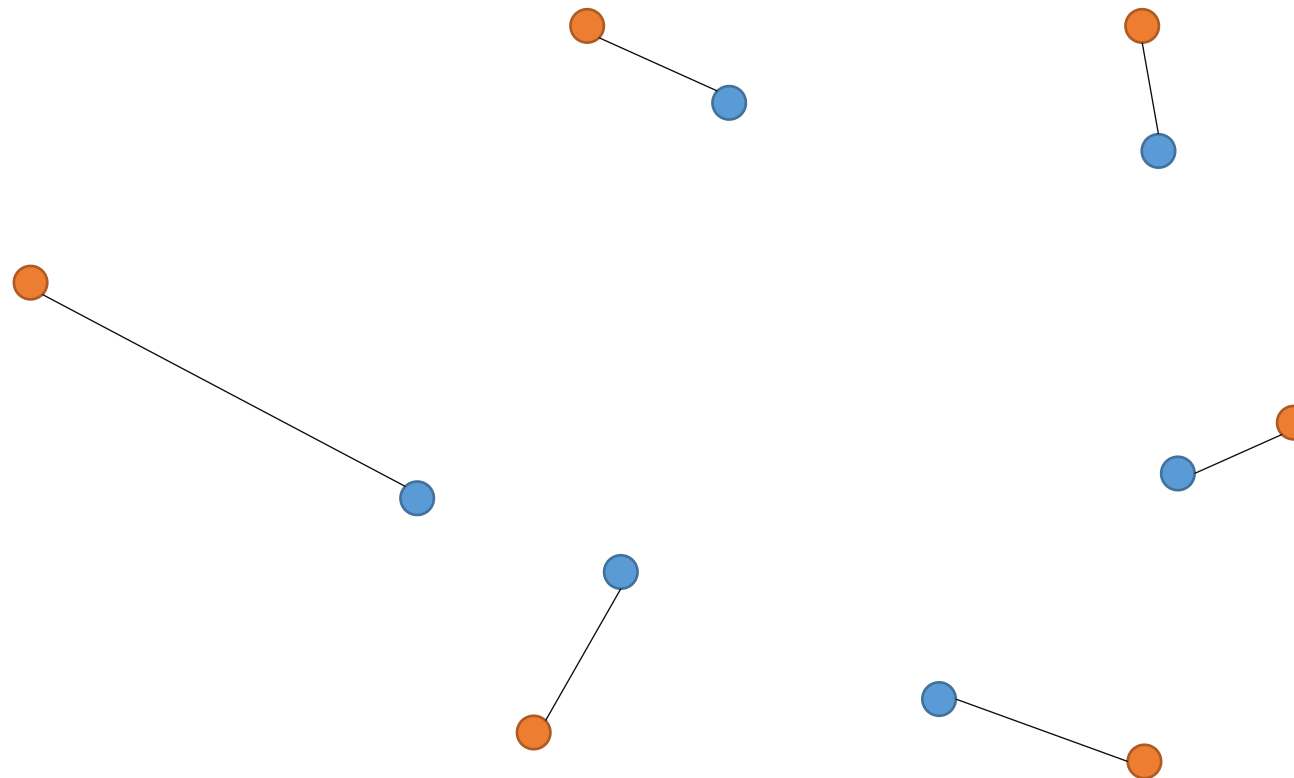
Set comparison

Given two sets of points, measure their discrepancy



Correspondence (I): optimal assignment

Given two sets of points, measure their discrepancy

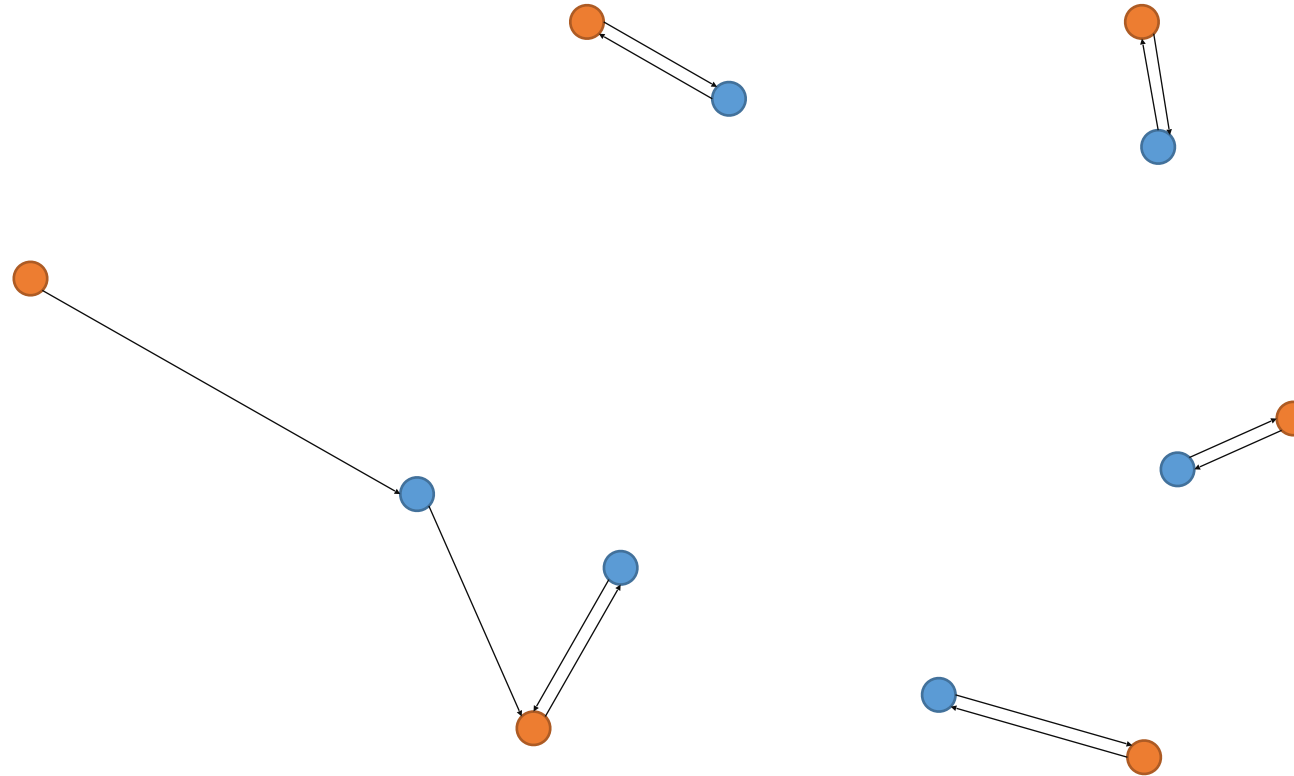


a.k.a Earth Mover's distance (EMD)

$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \rightarrow S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2 \quad \text{where } \phi : S_1 \rightarrow S_2 \text{ is a bijection.}$$

Correspondence (II): closest point

Given two sets of points, measure their discrepancy



a.k.a Chamfer distance (CD)

$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2^2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2^2$$

Required properties of distance metrics

Geometric requirement

Computational requirement

Required properties of distance metrics

Geometric requirement

- Reflects natural shape differences
- Induce a nice space for *shape interpolations*

Computational requirement

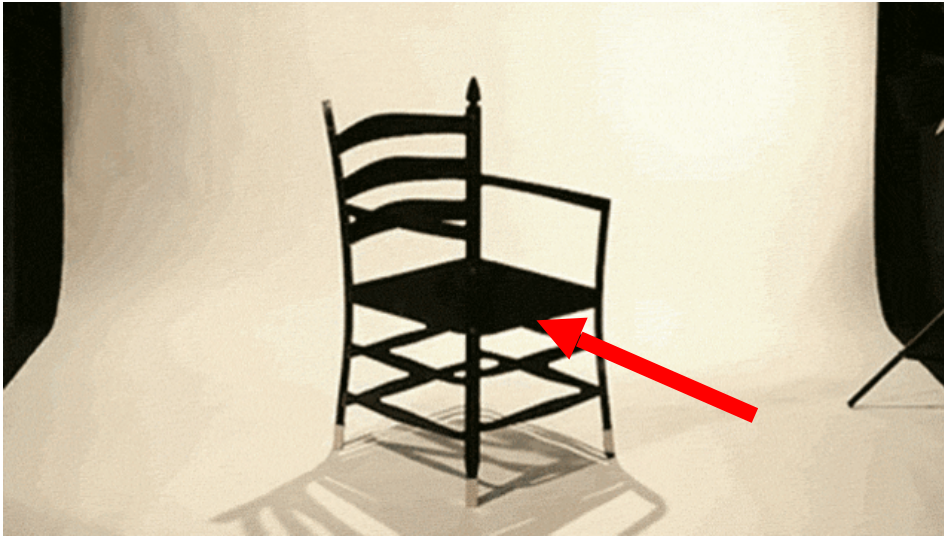
How distance metric affects learning?

A fundamental issue: inherent ambiguity in 2D-3D dimension lifting



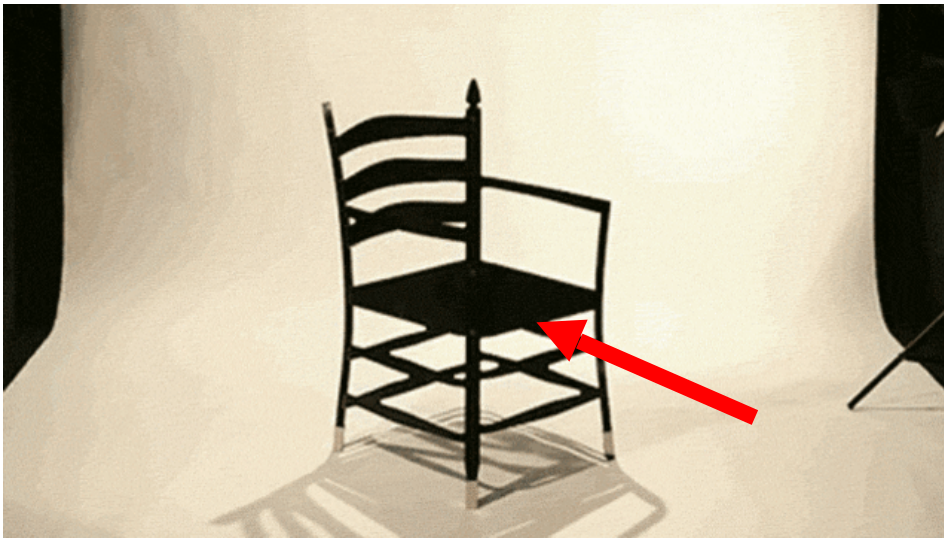
How distance metric affects learning?

A fundamental issue: inherent ambiguity in 2D-3D dimension lifting



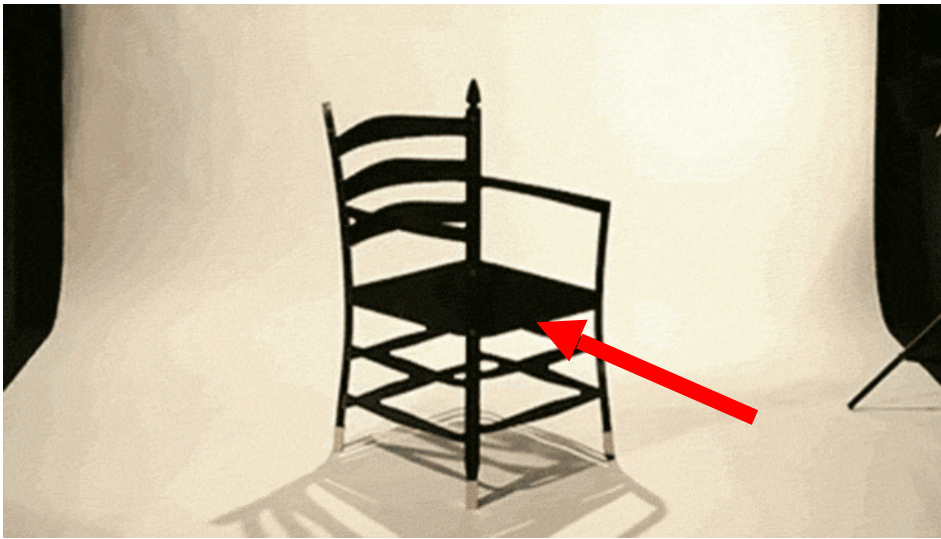
How distance metric affects learning?

A fundamental issue: inherent ambiguity in 2D-3D dimension lifting



How distance metric affects learning?

A fundamental issue: inherent ambiguity in 2D-3D dimension lifting



- By loss minimization, the network tends to predict a “**mean shape**” that **averages out** uncertainty

Distance metrics affect mean shapes

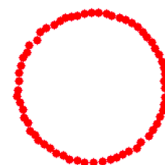
The mean shape carries characteristics of the distance metric

$$\bar{x} = \operatorname{argmin}_x \mathbb{E}_{s \sim \mathcal{S}} [d(x, s)]$$

continuous
hidden variable
(radius)



Input



EMD mean



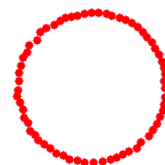
Chamfer mean

Mean shapes from distance metrics

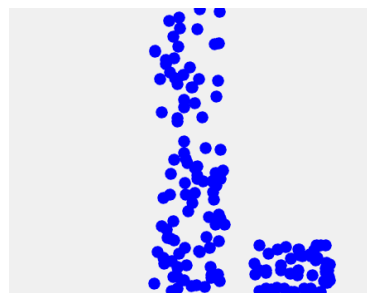
The mean shape carries characteristics of the distance metric

$$\bar{x} = \operatorname{argmin}_x \mathbb{E}_{s \sim \mathcal{S}} [d(x, s)]$$

continuous
hidden variable
(radius)



discrete
hidden variable
(add-on location)



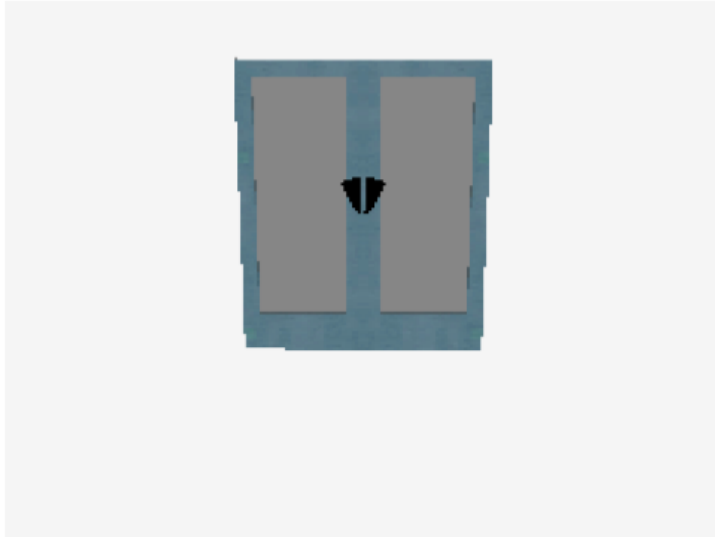
Input

EMD mean

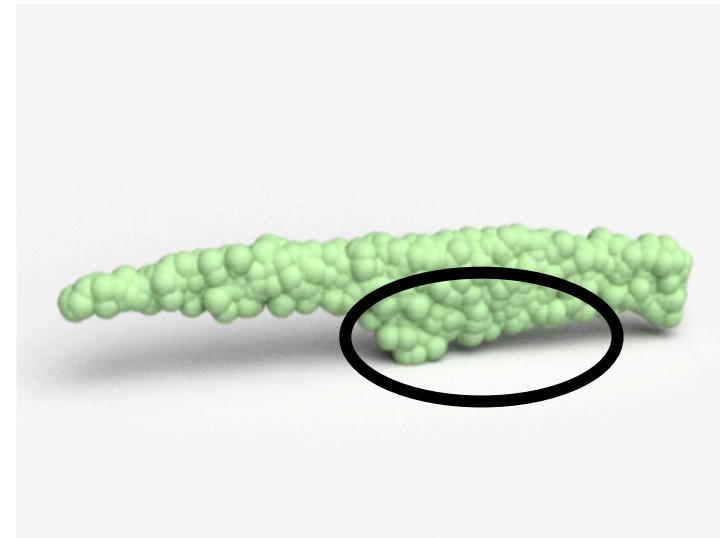
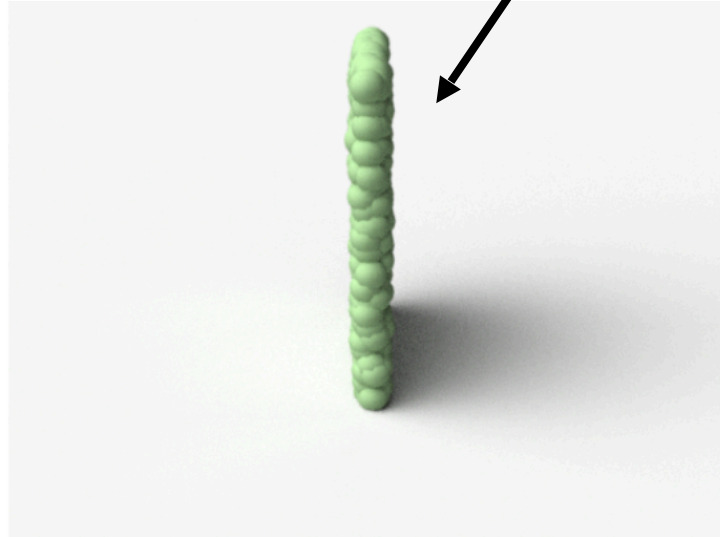
Chamfer mean

Comparison of predictions by EMD versus CD

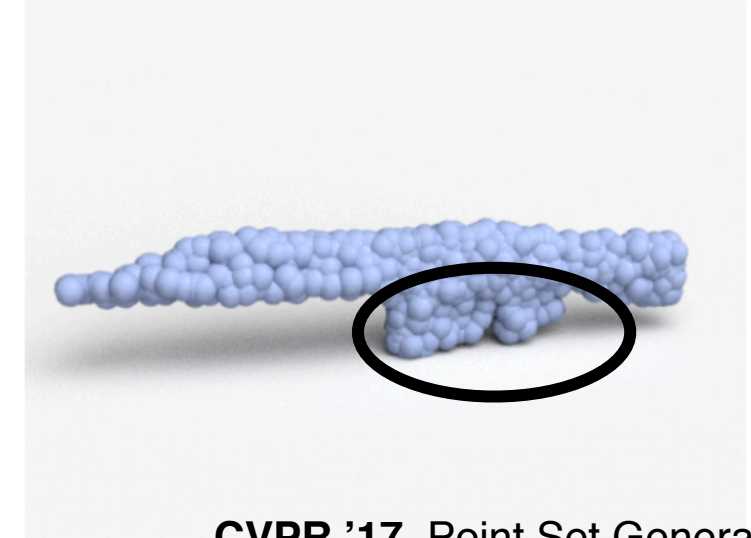
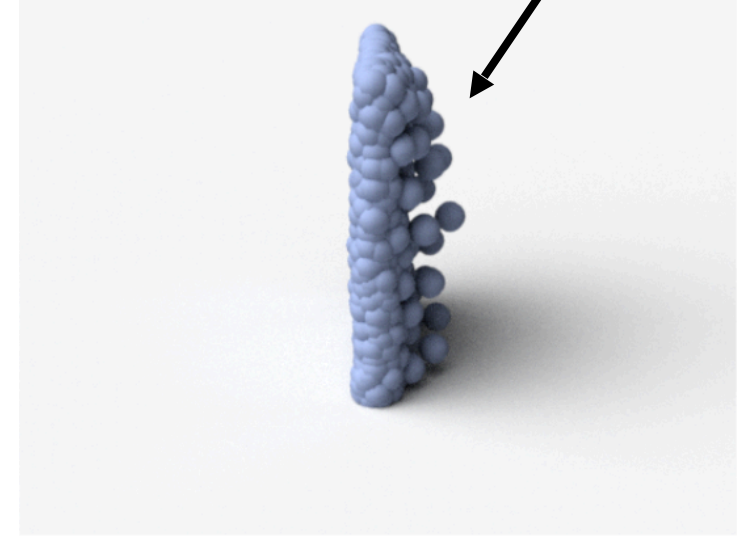
Input



EMD



Chamfer



Required properties of distance metrics

Geometric requirement

- Reflects natural shape differences
- Induce a nice space for shape interpolations

Computational requirement

- Defines a loss function that is numerically easy to optimize

Computational requirement of metrics

To be used as a loss function, the metric has to be

- **Differentiable** with respect to point locations
- **Efficient** to compute

Computational requirement of metrics

- **Differentiable** with respect to point location

Chamfer distance

$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2^2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2^2$$



Earth Mover's distance

$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \rightarrow S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2 \quad \text{where } \phi: S_1 \rightarrow S_2 \text{ is a bijection.}$$



- Simple function of coordinates
- In general positions, the correspondence is unique
- **With infinitesimal movement, the correspondence does not change**

Conclusion: differentiable almost everywhere

Computational requirement of metrics

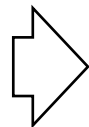
- **Efficient** to compute

Chamfer distance: trivially parallelizable on CUDA

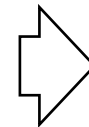
Earth Mover's distance (optimal assignment):

- We implement a **distributed** approximation algorithm on CUDA
- Based upon [Bertsekas, 1985], $(1 + \epsilon)$ -approximation

Pipeline

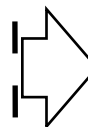


Deep network
(f)

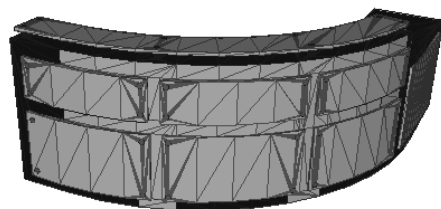


Prediction

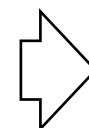
$$\begin{Bmatrix} (x_1, y_1, z_1) \\ (x_2, y_2, z_2) \\ \dots \\ (x_n, y_n, z_n) \end{Bmatrix}$$



Loss
on
sets
(L)



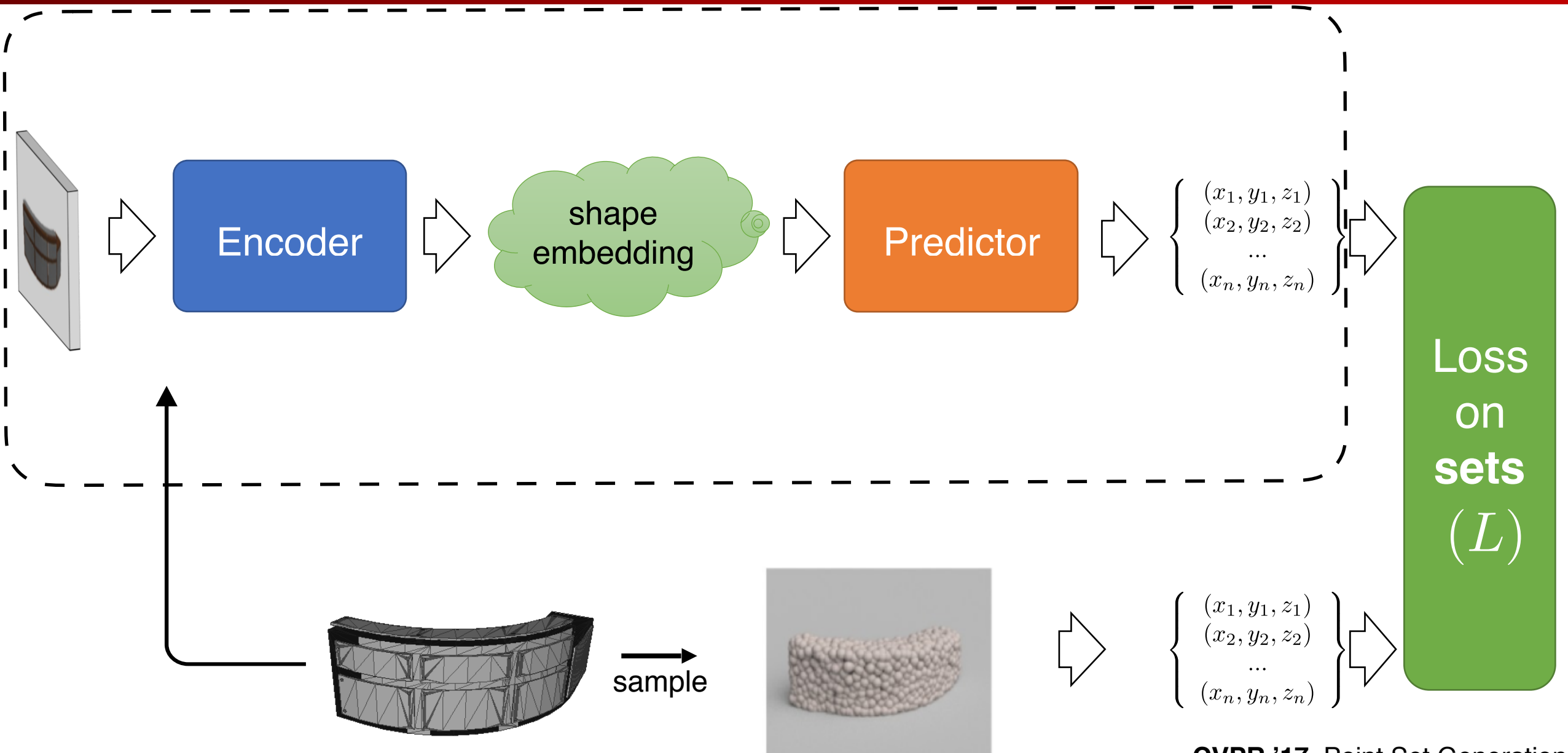
sample



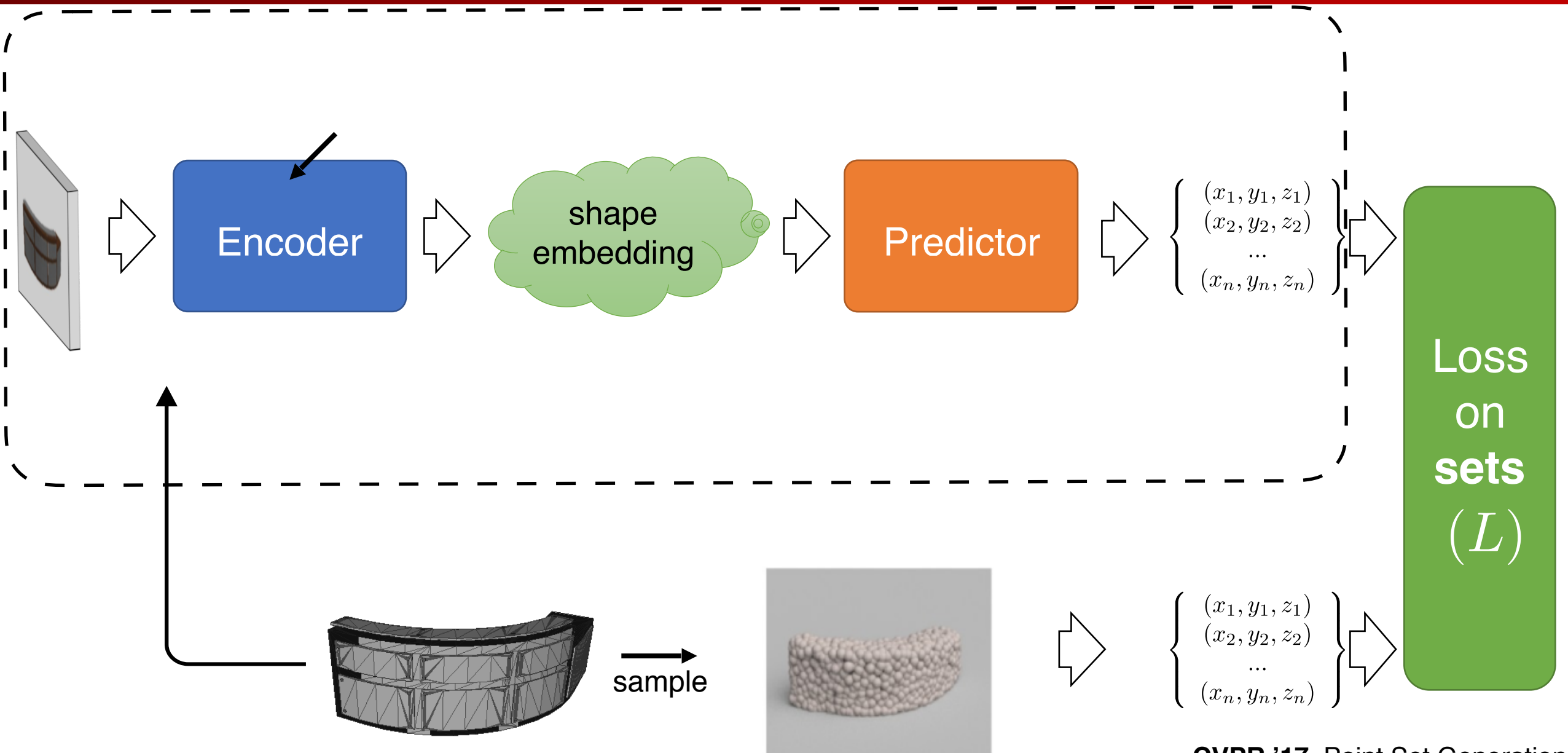
$$\begin{Bmatrix} (x_1, y_1, z_1) \\ (x_2, y_2, z_2) \\ \dots \\ (x_n, y_n, z_n) \end{Bmatrix}$$



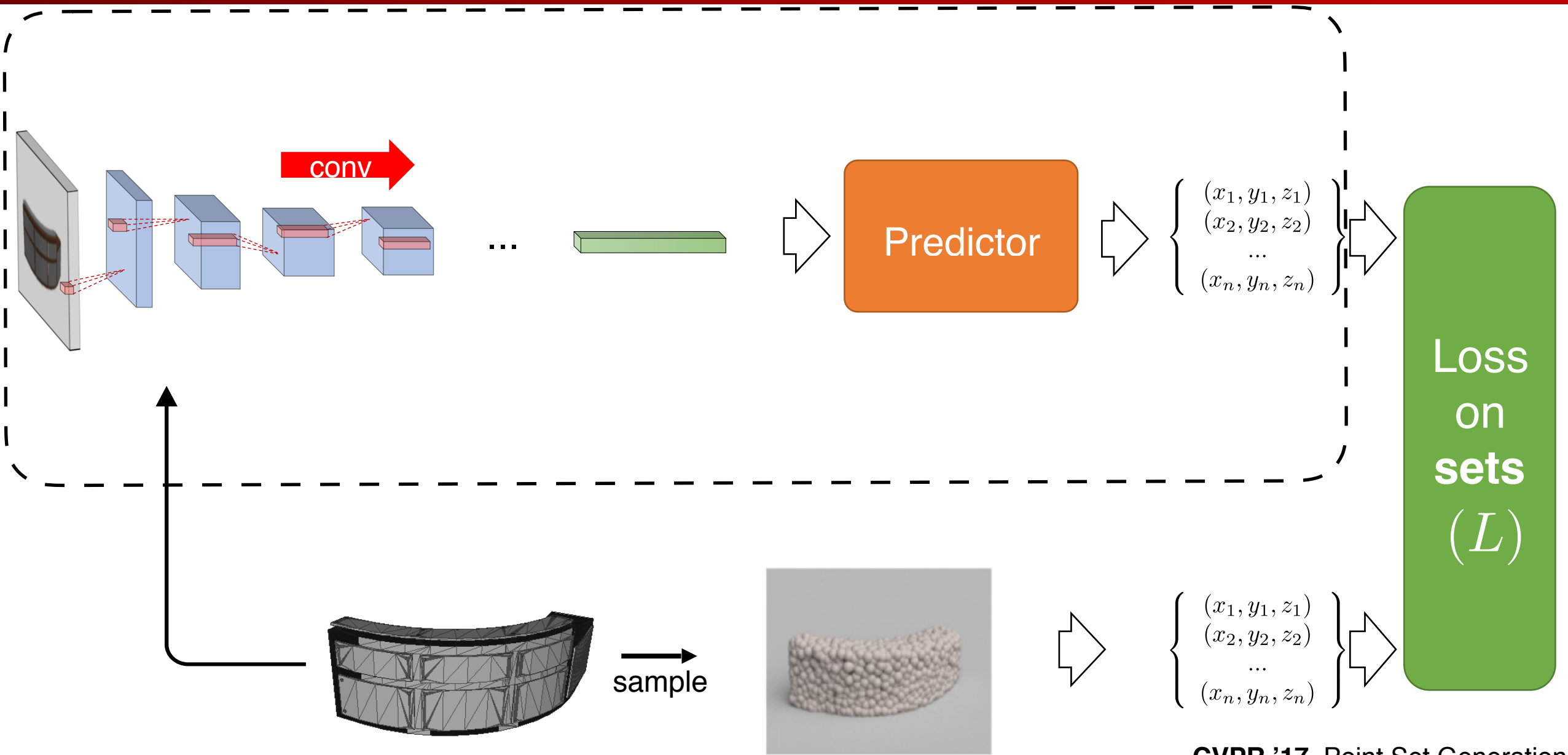
Pipeline



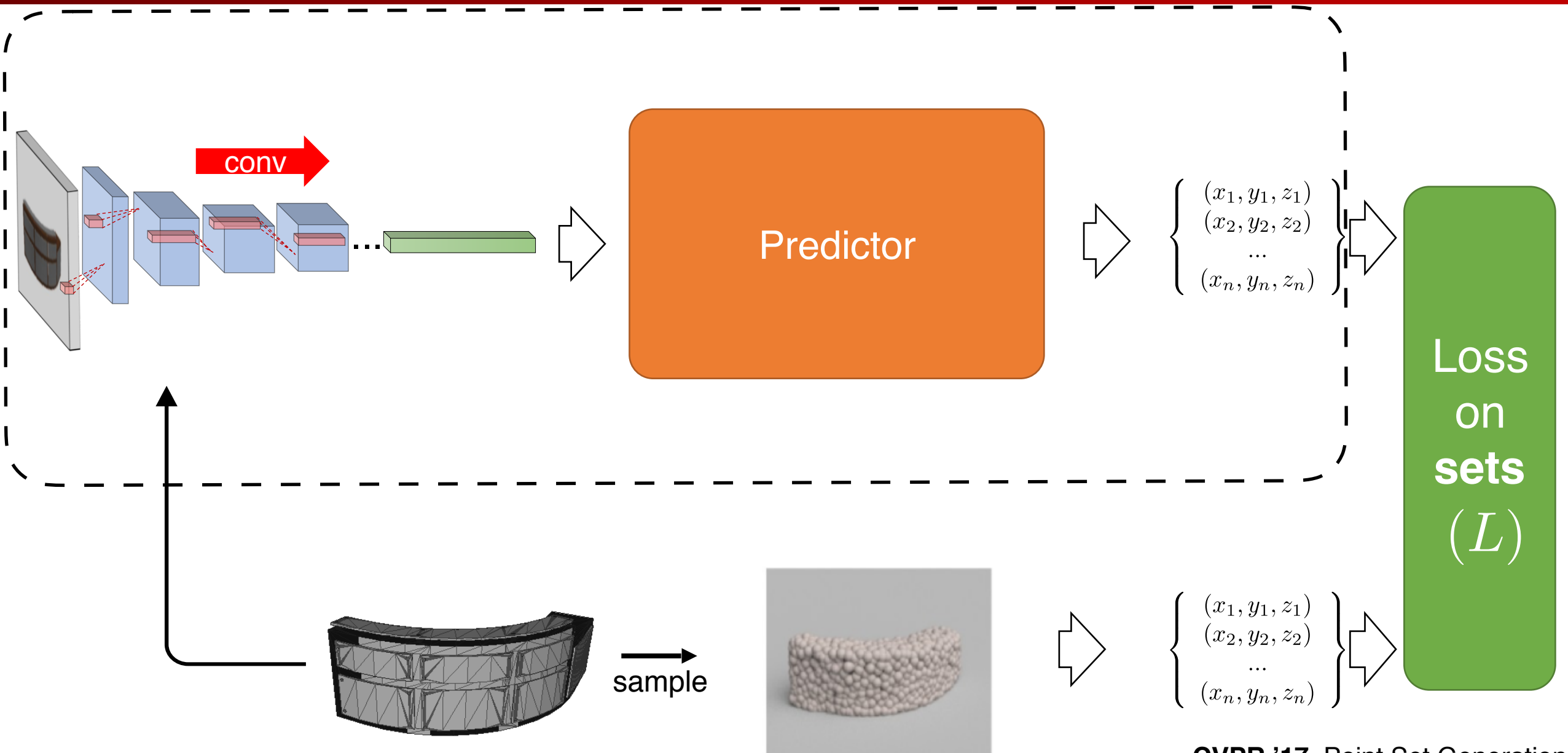
Pipeline



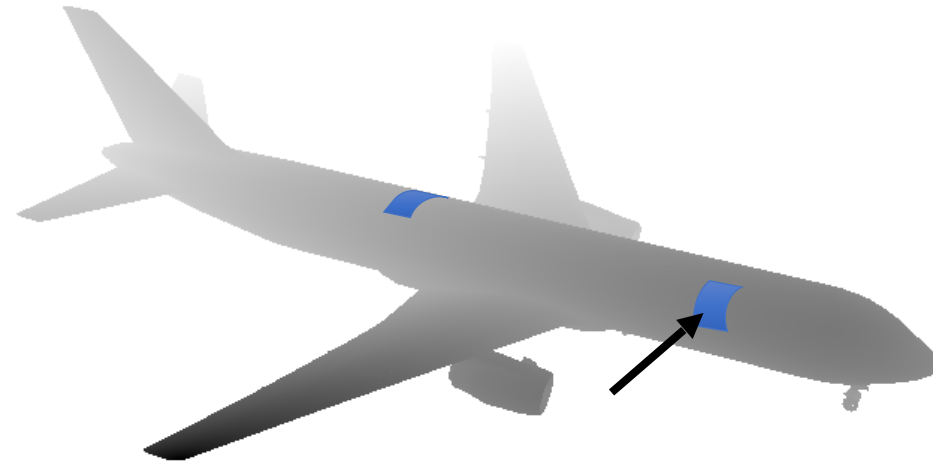
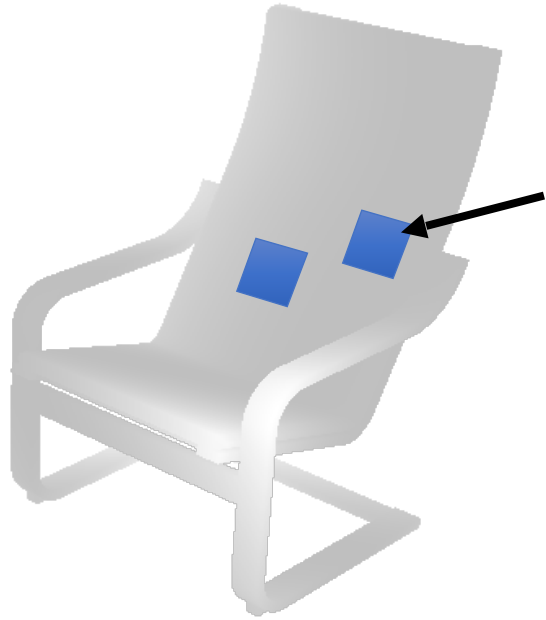
Pipeline



Pipeline

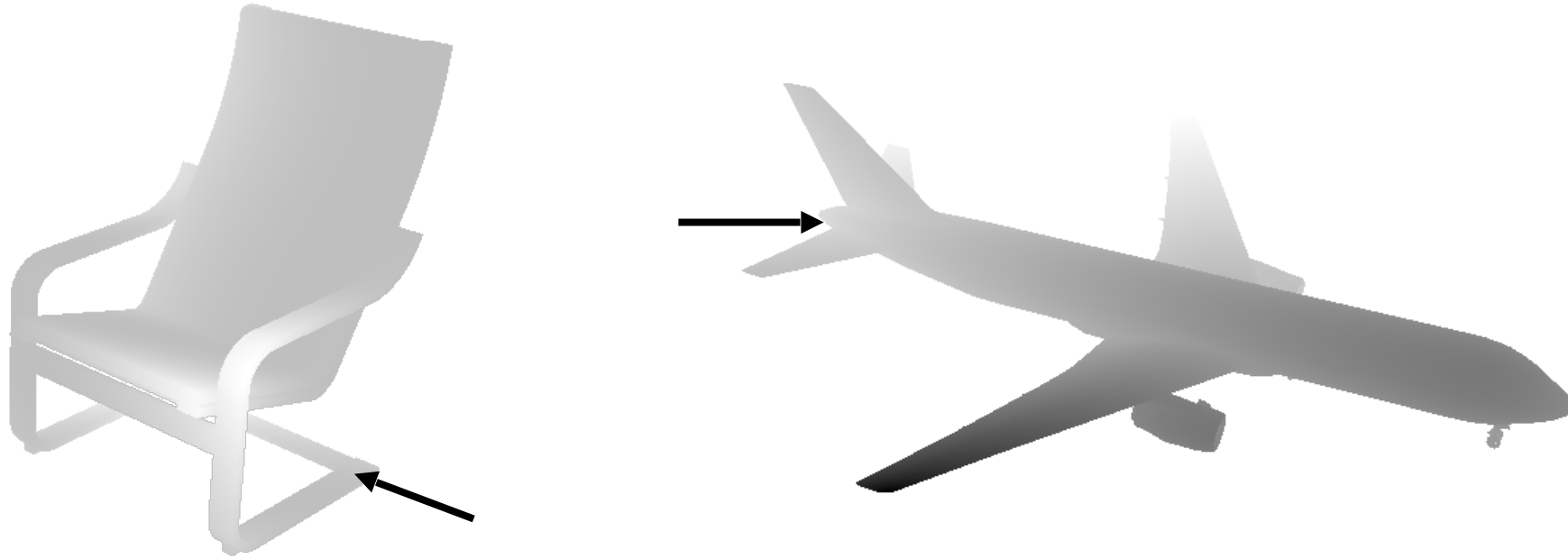


Natural statistics of geometry



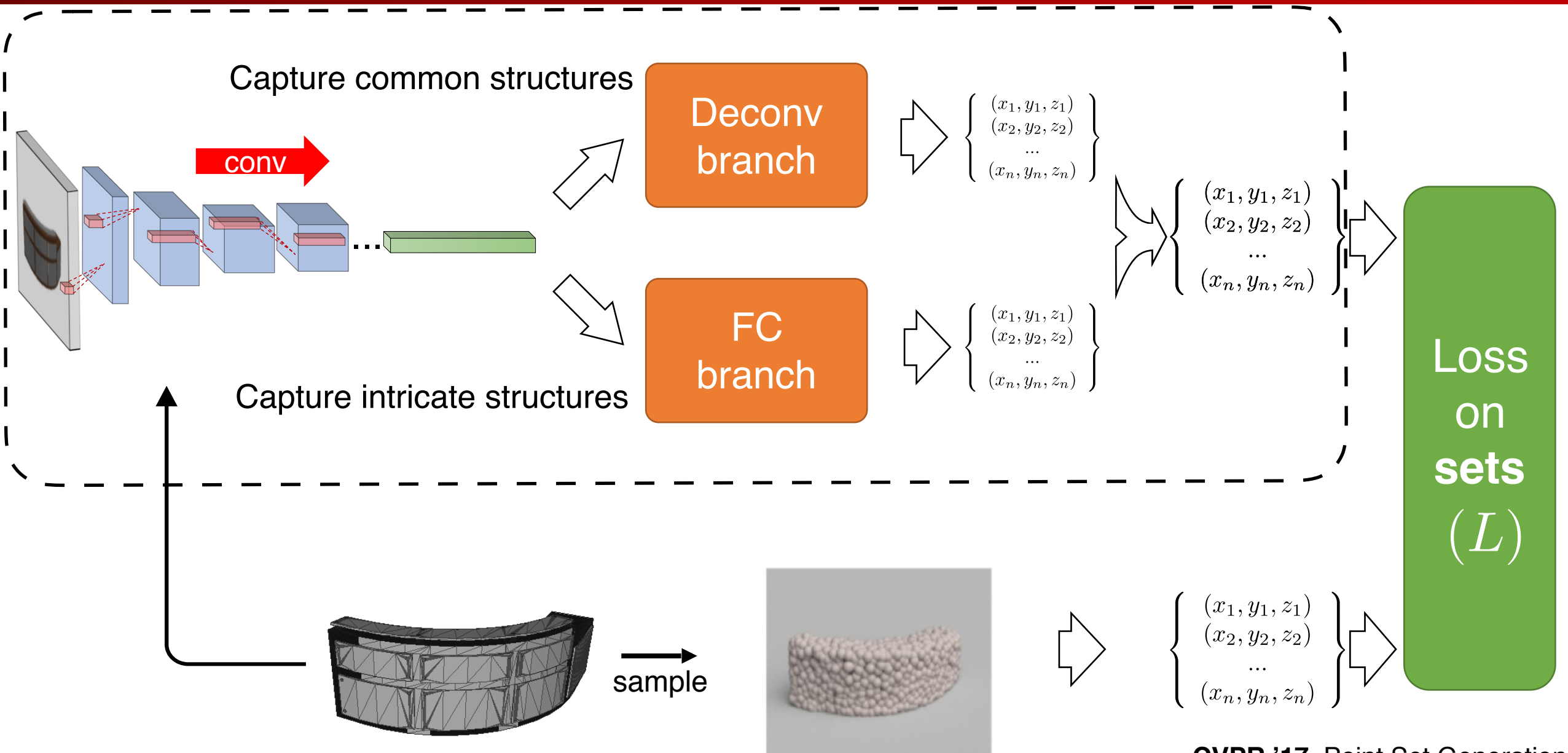
- Many local structures are common
 - e.g., planar patches, cylindrical patches
 - **strong local correlation** among point coordinates

Natural statistics of geometry

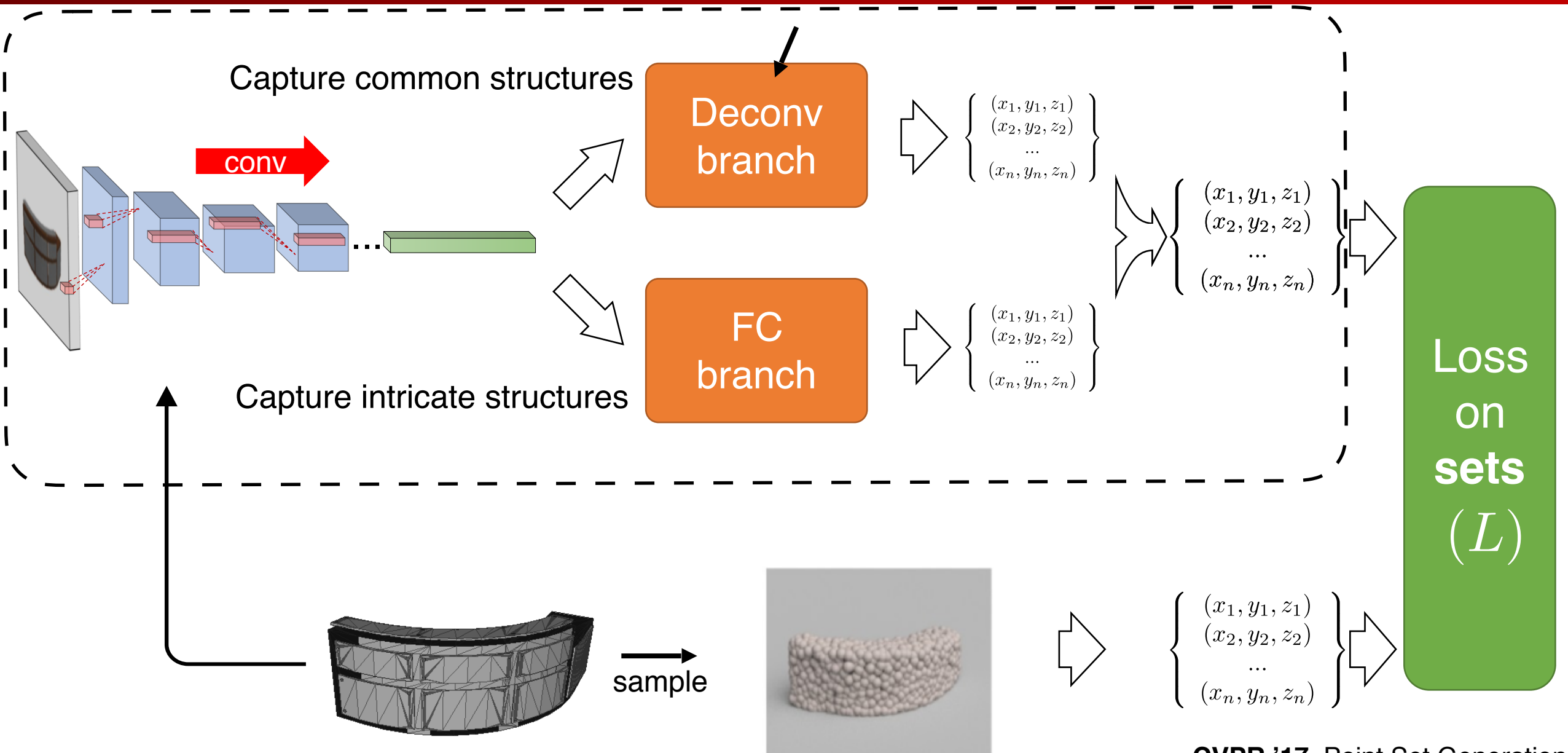


- Many local structures are common
 - e.g., planar patches, cylindrical patches
 - **strong local correlation** among point coordinates
- Also some intricate structures
 - points have **high local variation**

Pipeline

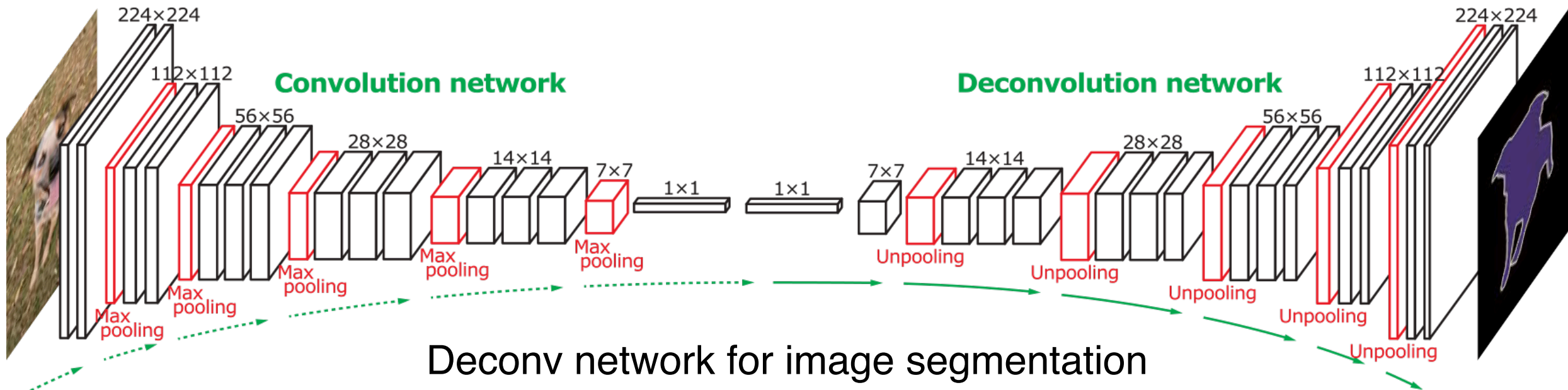


Pipeline



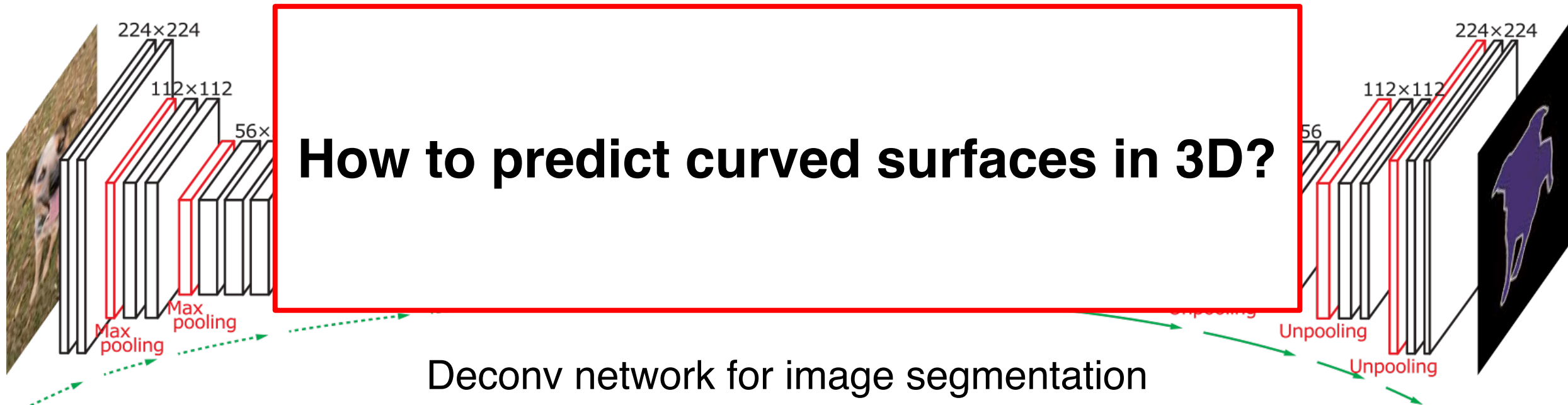
Review: deconv network

- Output n D arrays, e.g., 2D segmentation map
- **Common local patterns** are **learned from data**
- Predict **locally correlated** data well
- Weight sharing reduces the number of params



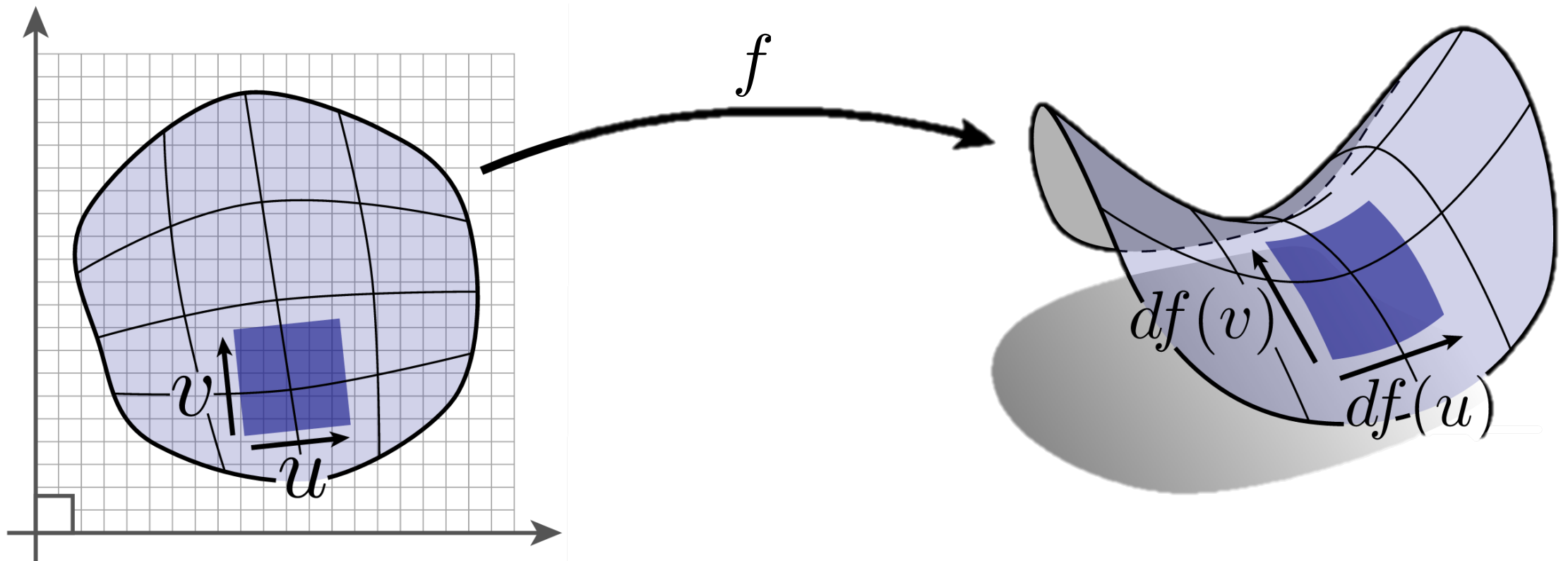
Review: deconv network

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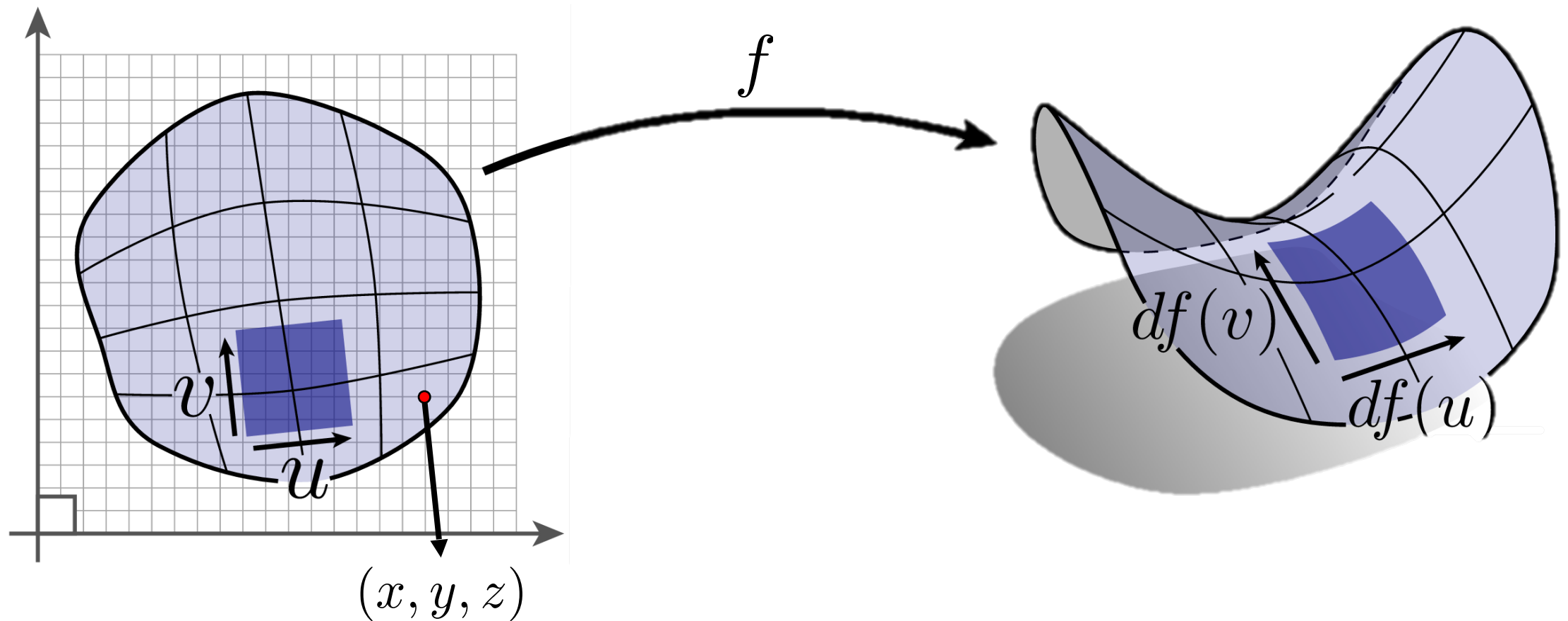
Prediction of curved 2D surfaces in 3D

- Surface parametrization ($2D \leftrightarrow 3D$ mapping)



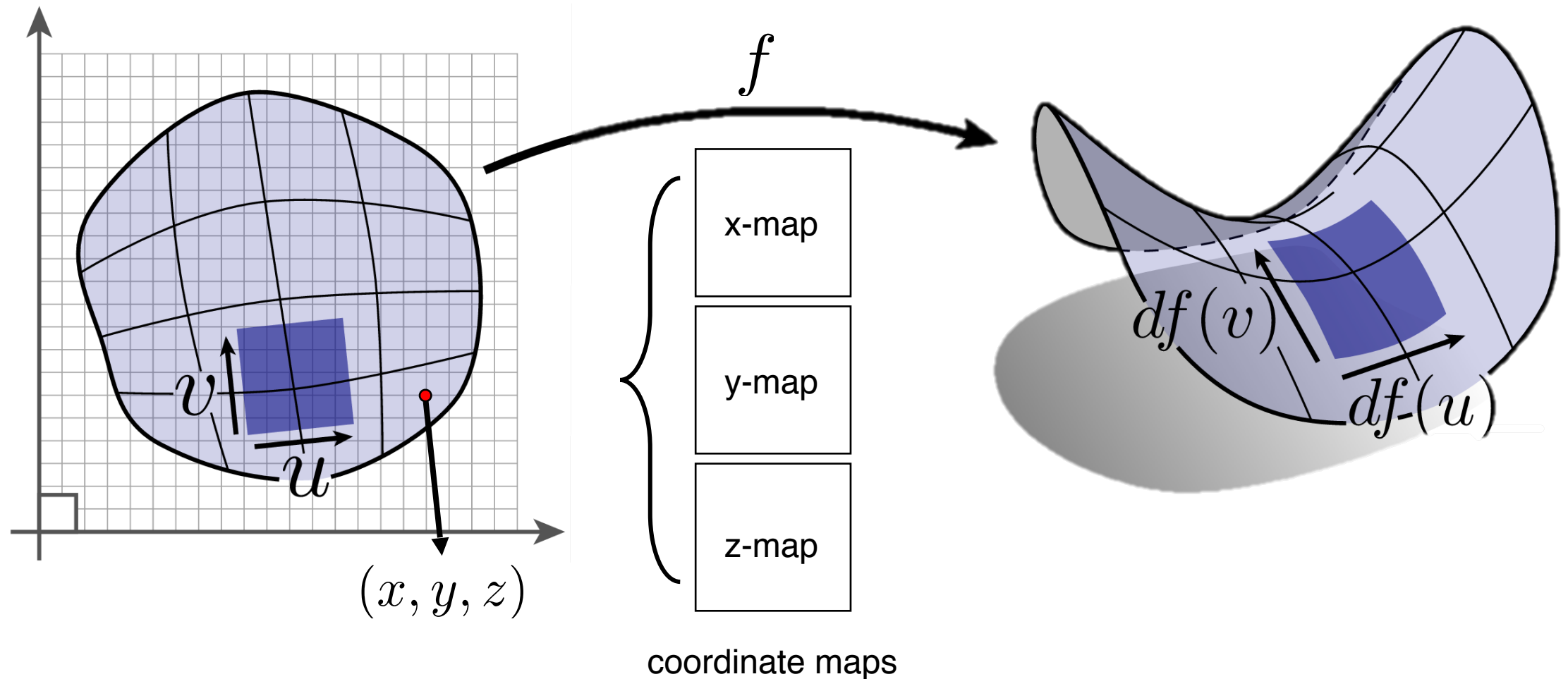
Prediction of curved 2D surfaces in 3D

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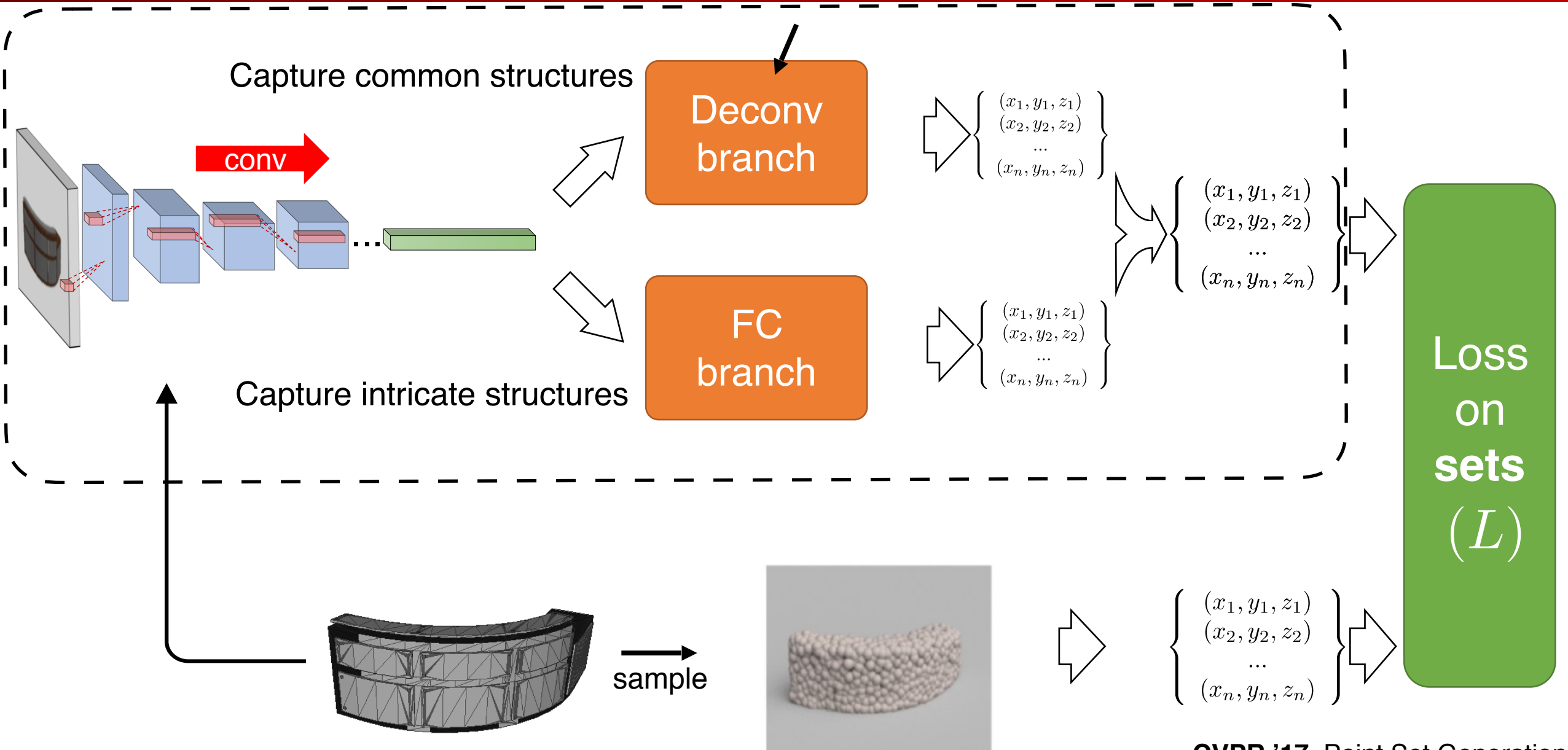


Prediction of curved 2D surfaces in 3D

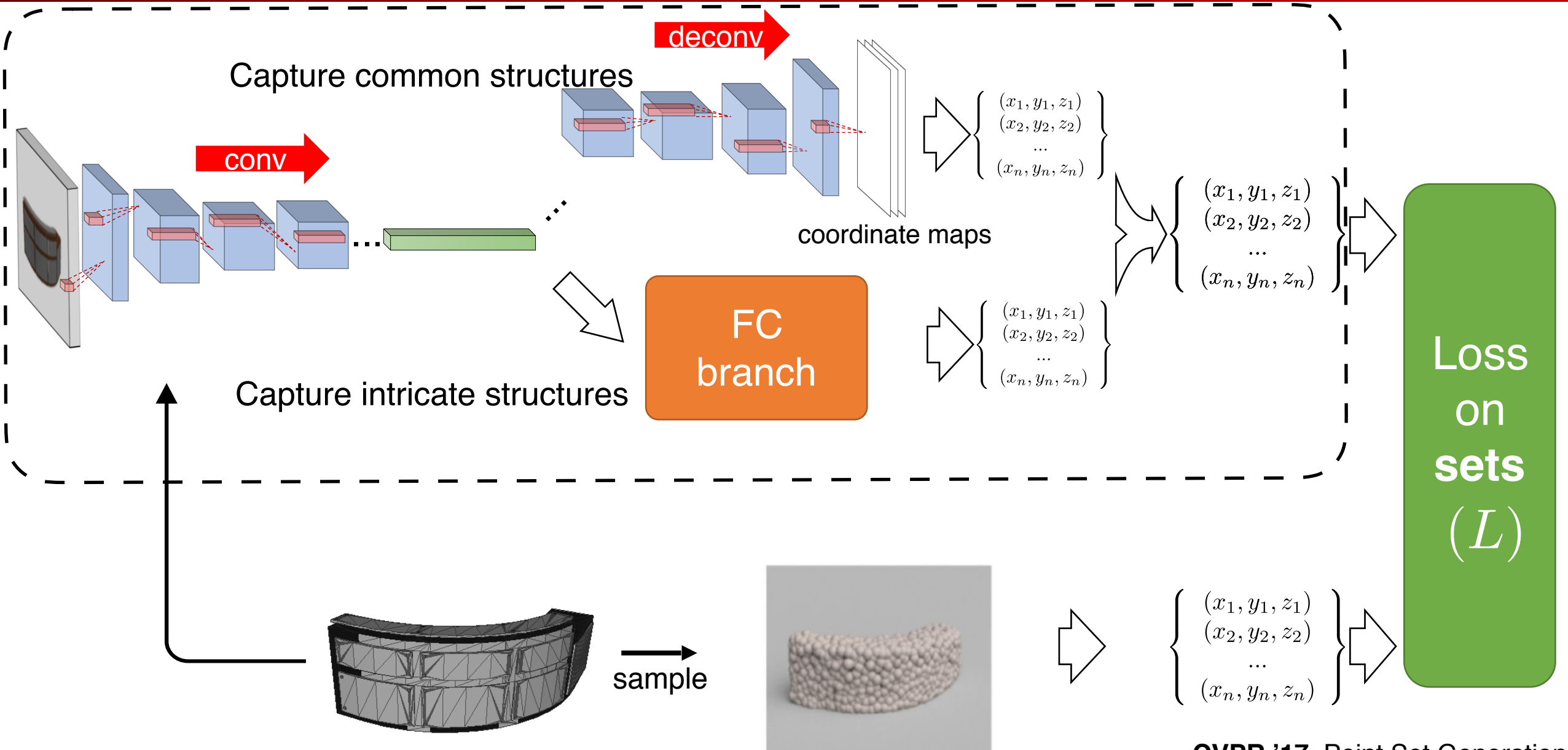
- Surface parametrization ($2D \leftrightarrow 3D$ mapping)



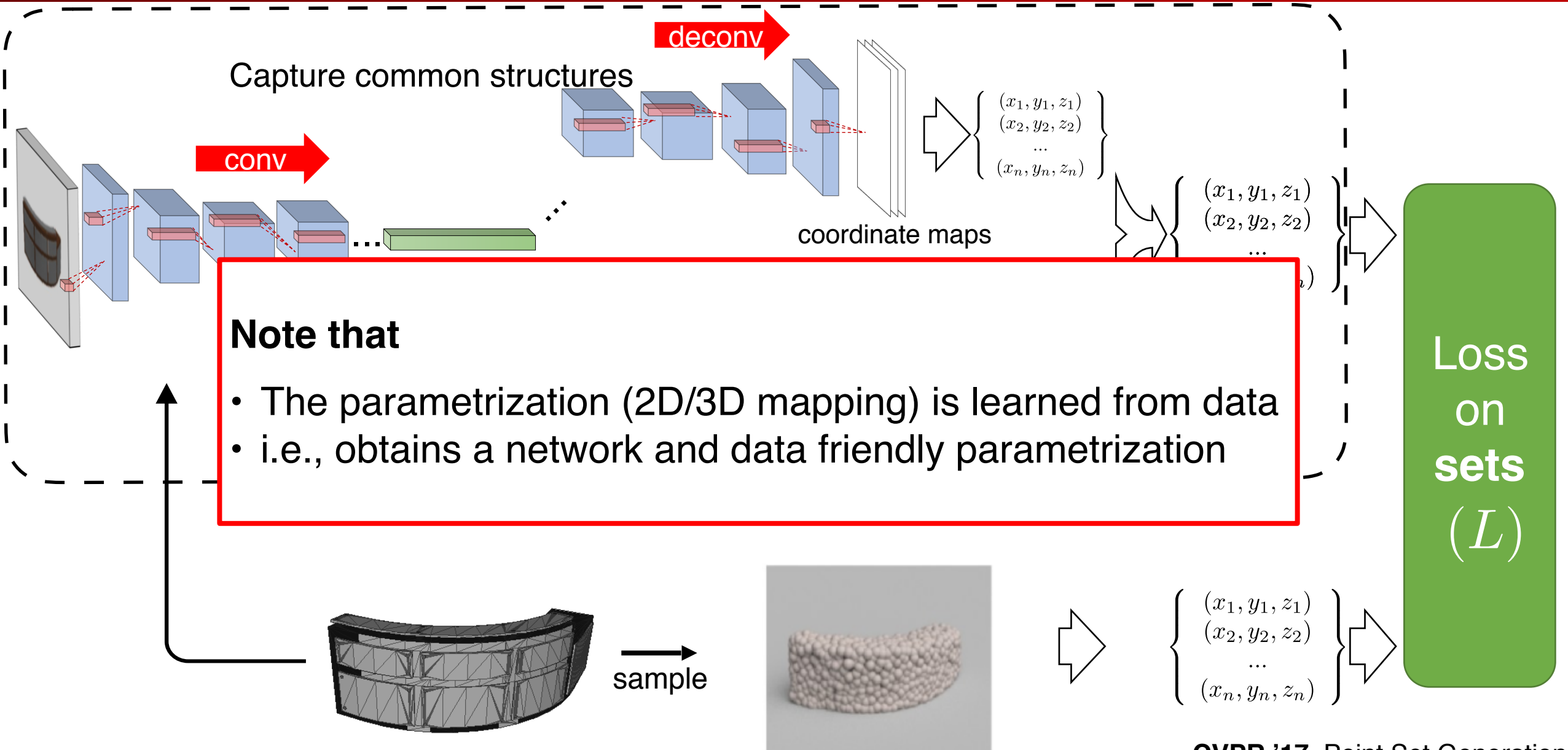
Parametrization prediction by deconv network



Parametrization prediction by deconv network



Parametrization prediction by deconv network

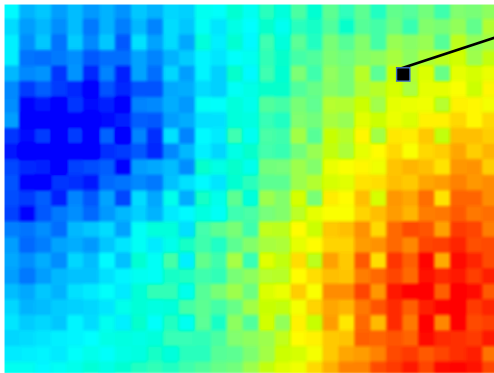
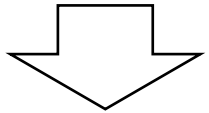


Visualization of the learned parameterization

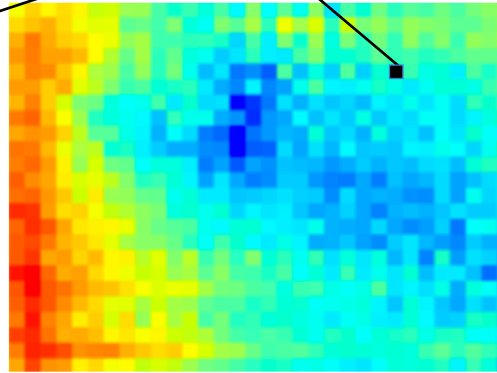


Observation:

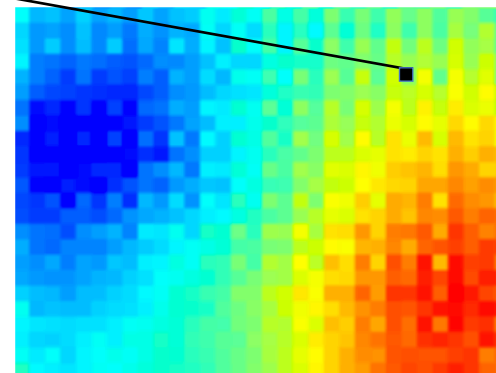
- Learns a **smooth** parametrization
- Because deconv net tends to predict data with local correlation



map of x coord



map of y coord



map of z coord

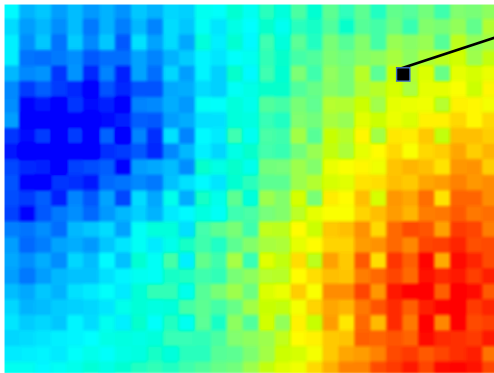
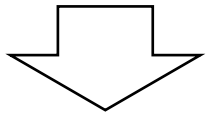
(x_k, y_k, z_k)

Visualization of the learned parameterization

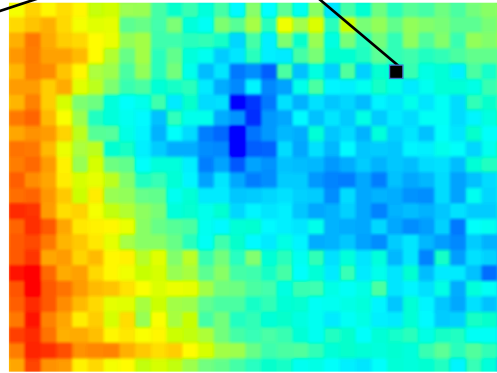


Observation:

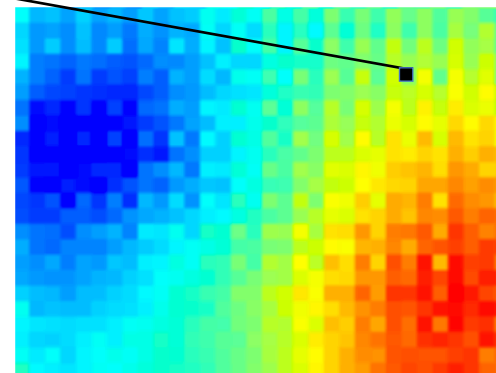
- Learns a **smooth** parametrization
- Because deconv net tends to predict data with local correlation
- Corresponds to **smooth surfaces!**



map of x coord

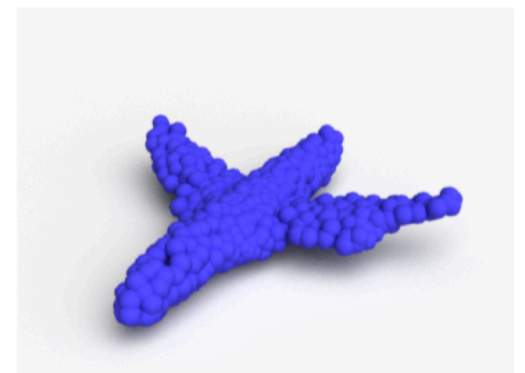
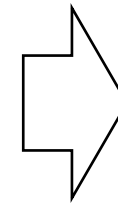


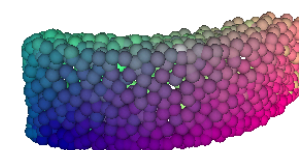
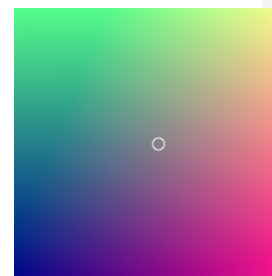
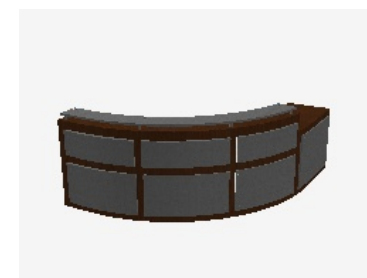
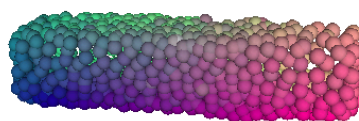
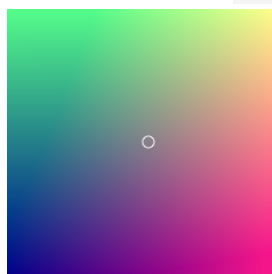
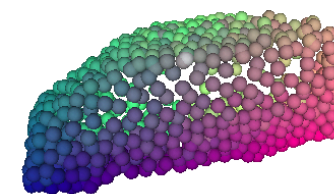
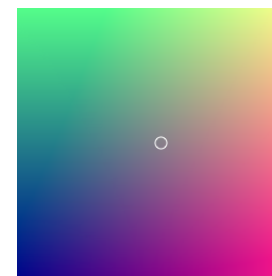
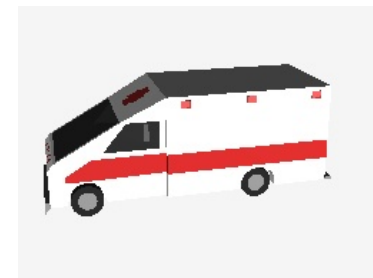
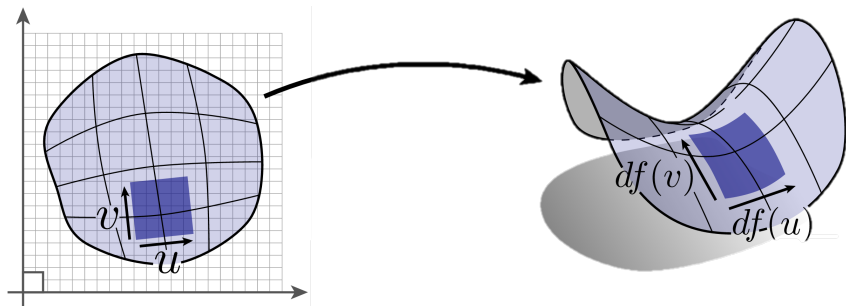
map of y coord



map of z coord

(x_k, y_k, z_k)



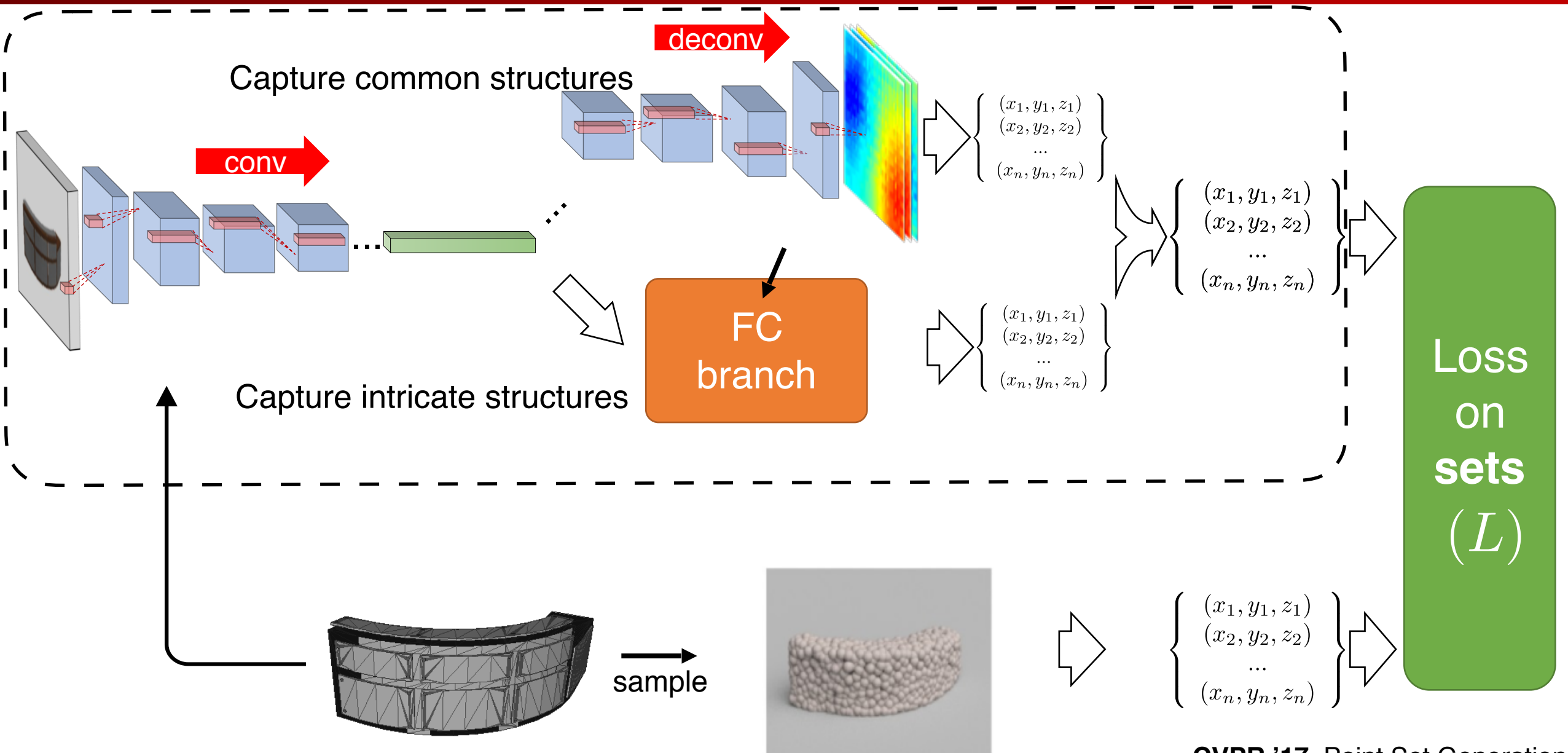


Natural statistics of geometry

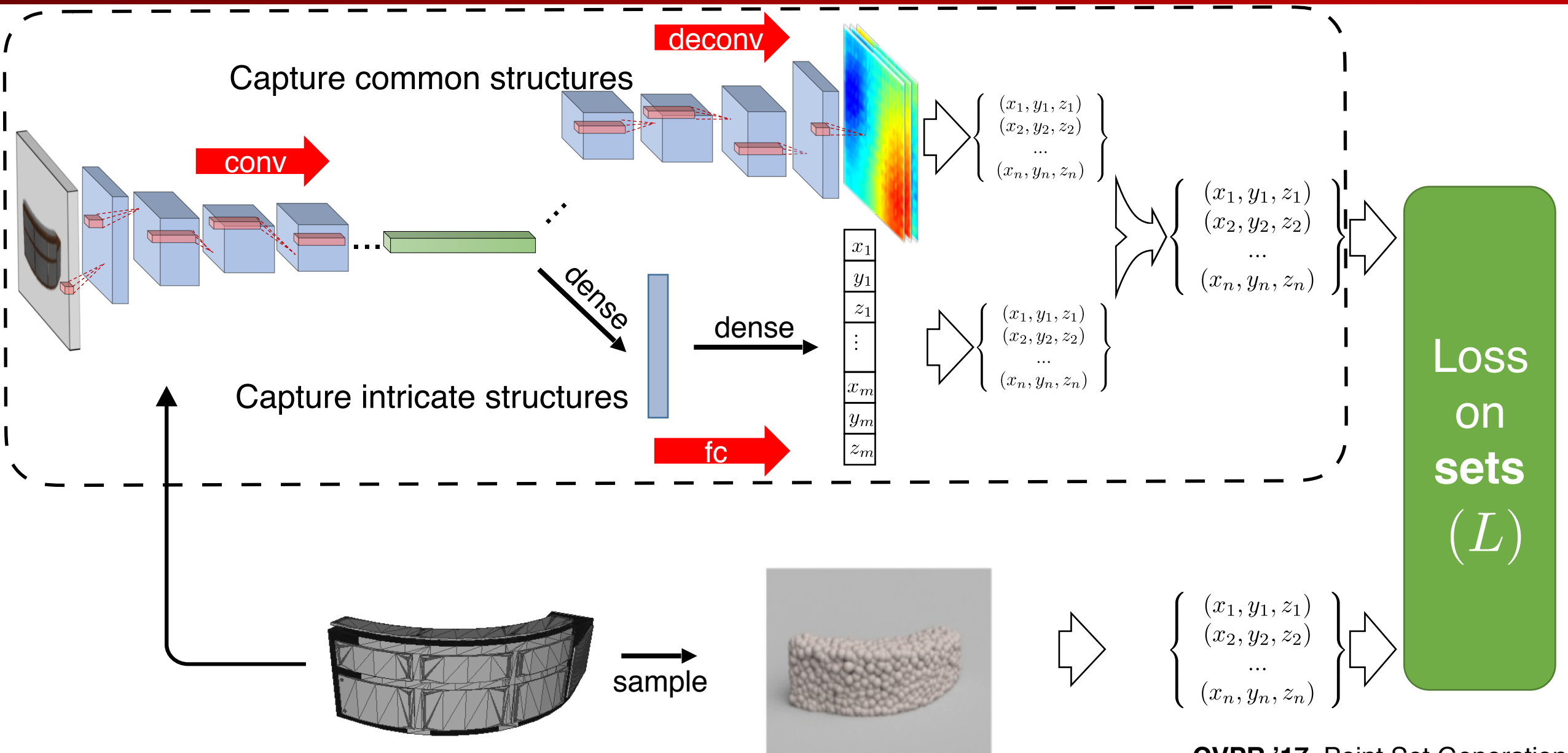


- Many local structures are common
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 - **strong local correlation** among point coordinates
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 - points have **high local variation**

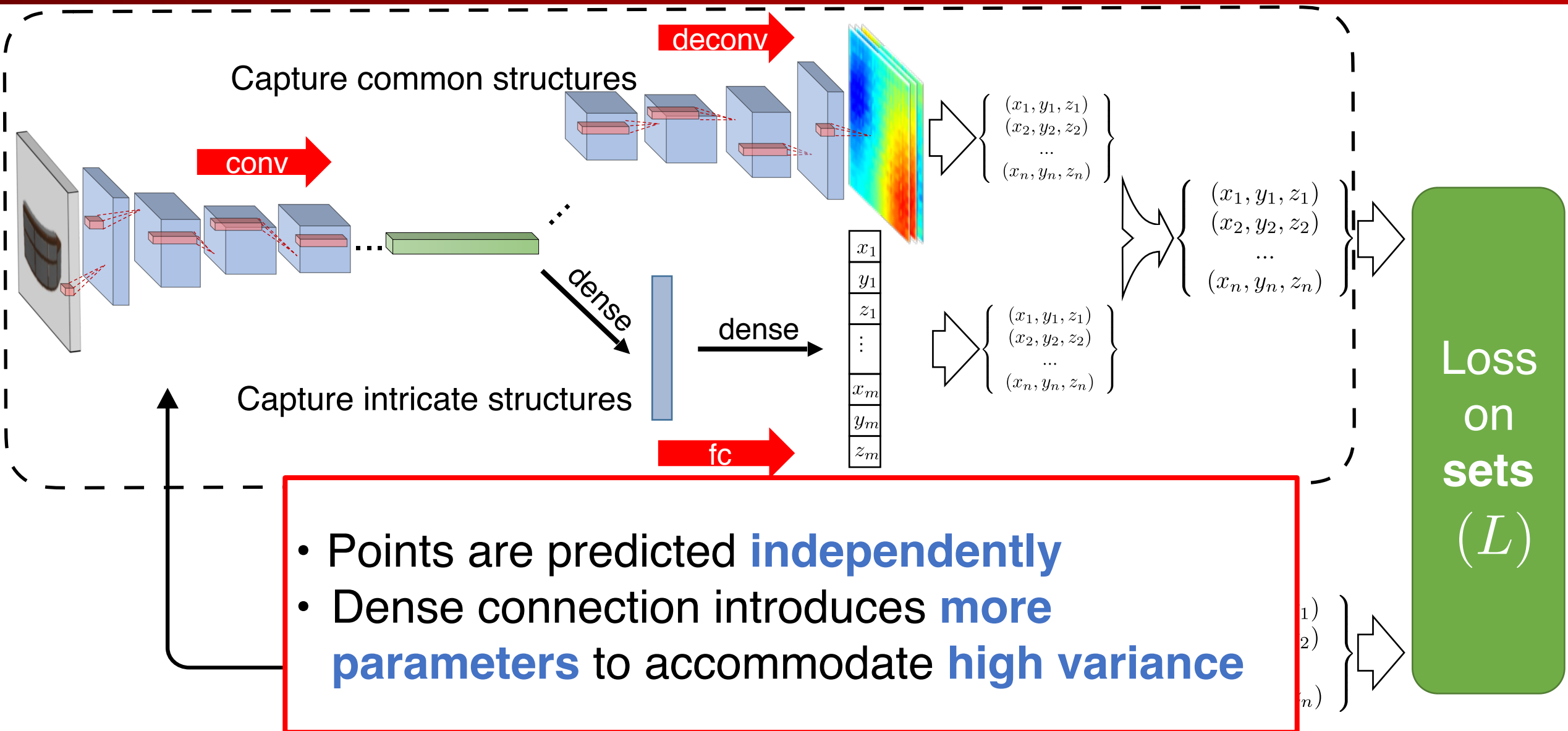
Pipeline



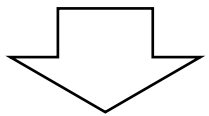
Pipeline



Pipeline

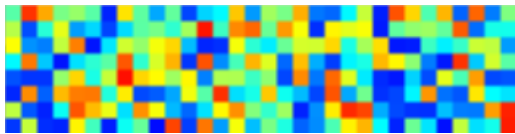


Visualization of the effect of FC branch

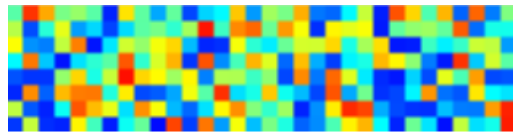


Observation:

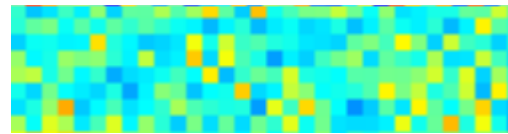
- The arrangement of predicted points are uncorrelated



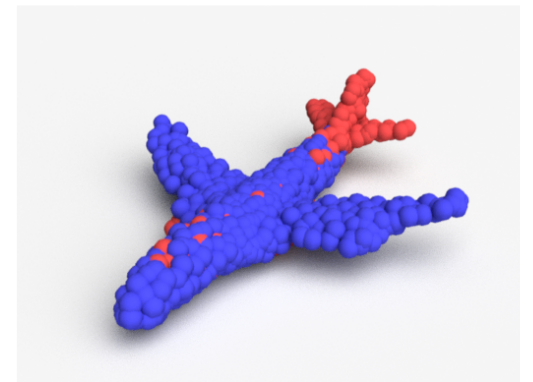
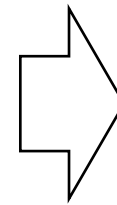
x-coord



y-coord

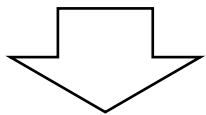


z-coord



red

Visualization of the effect of FC branch

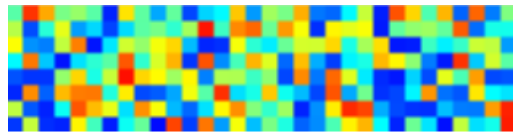


Observation:

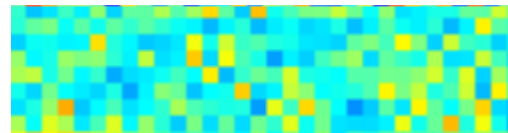
- The arrangement of predicted points are uncorrelated
- Located at **fine** structures



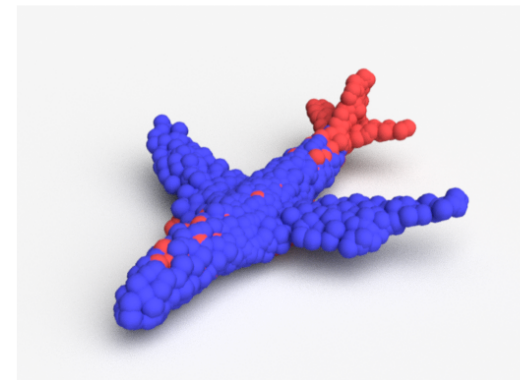
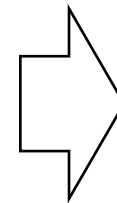
x-coord



y-coord

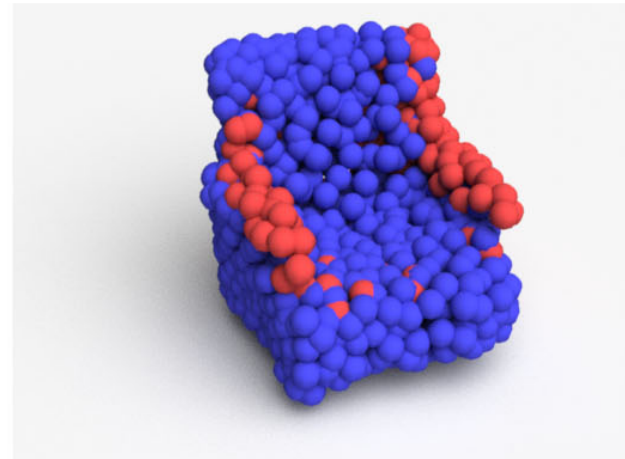
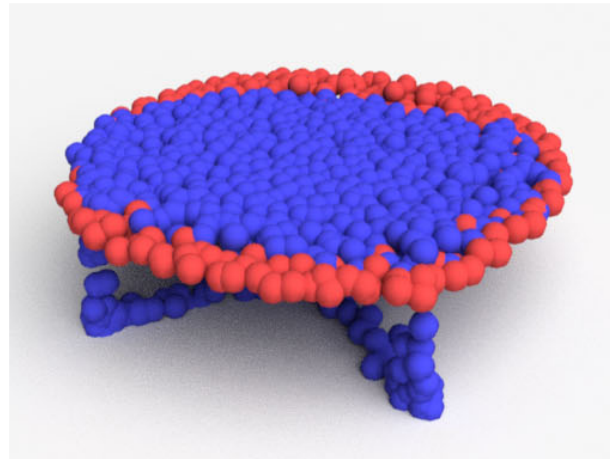
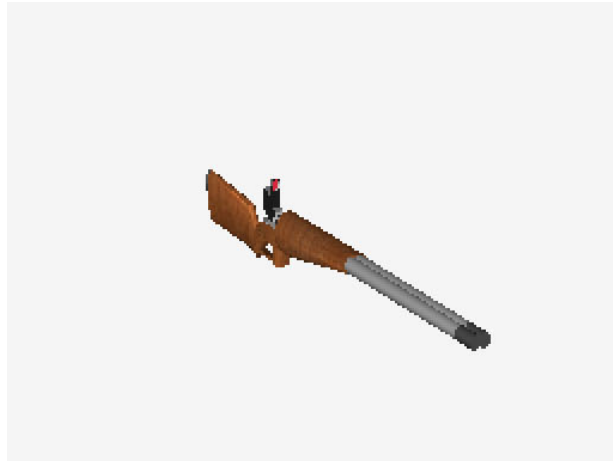


z-coord



red

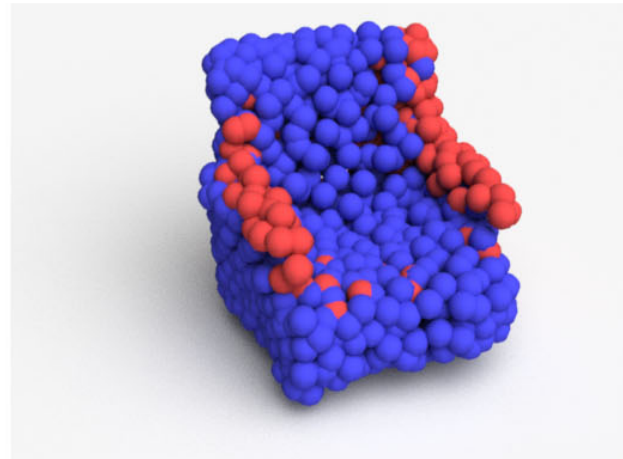
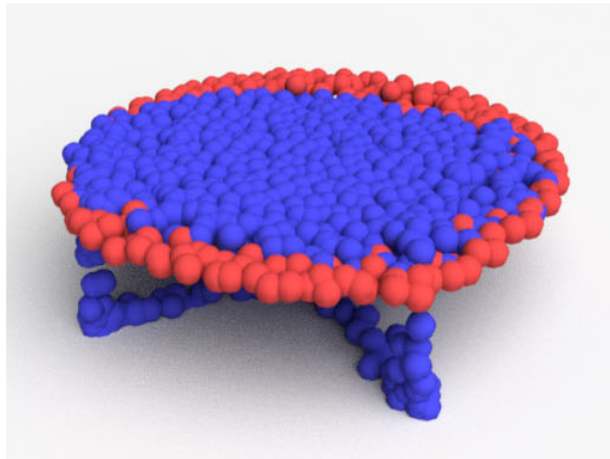
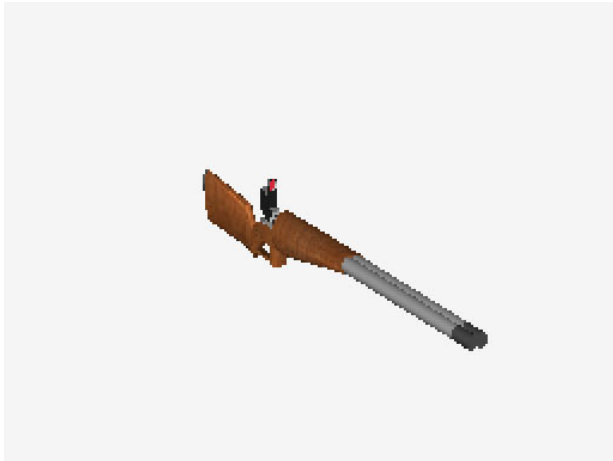
Q: Which color corresponds to the deconv branch? FC branch?



Q: Which color corresponds to the deconv branch? FC branch?

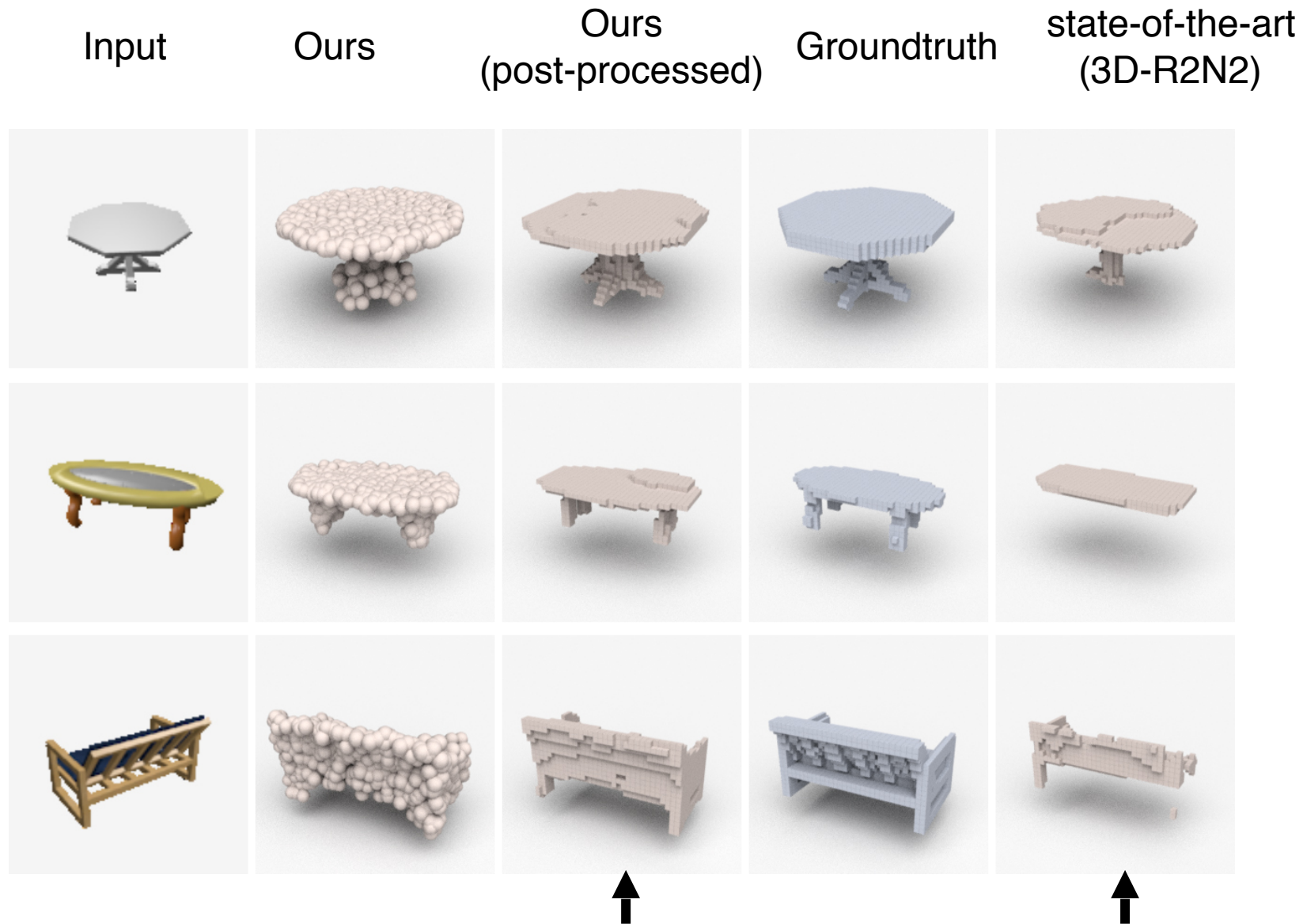
blue: deconv branch – **large, smooth** structures

red: FC branch – **intricate** structures



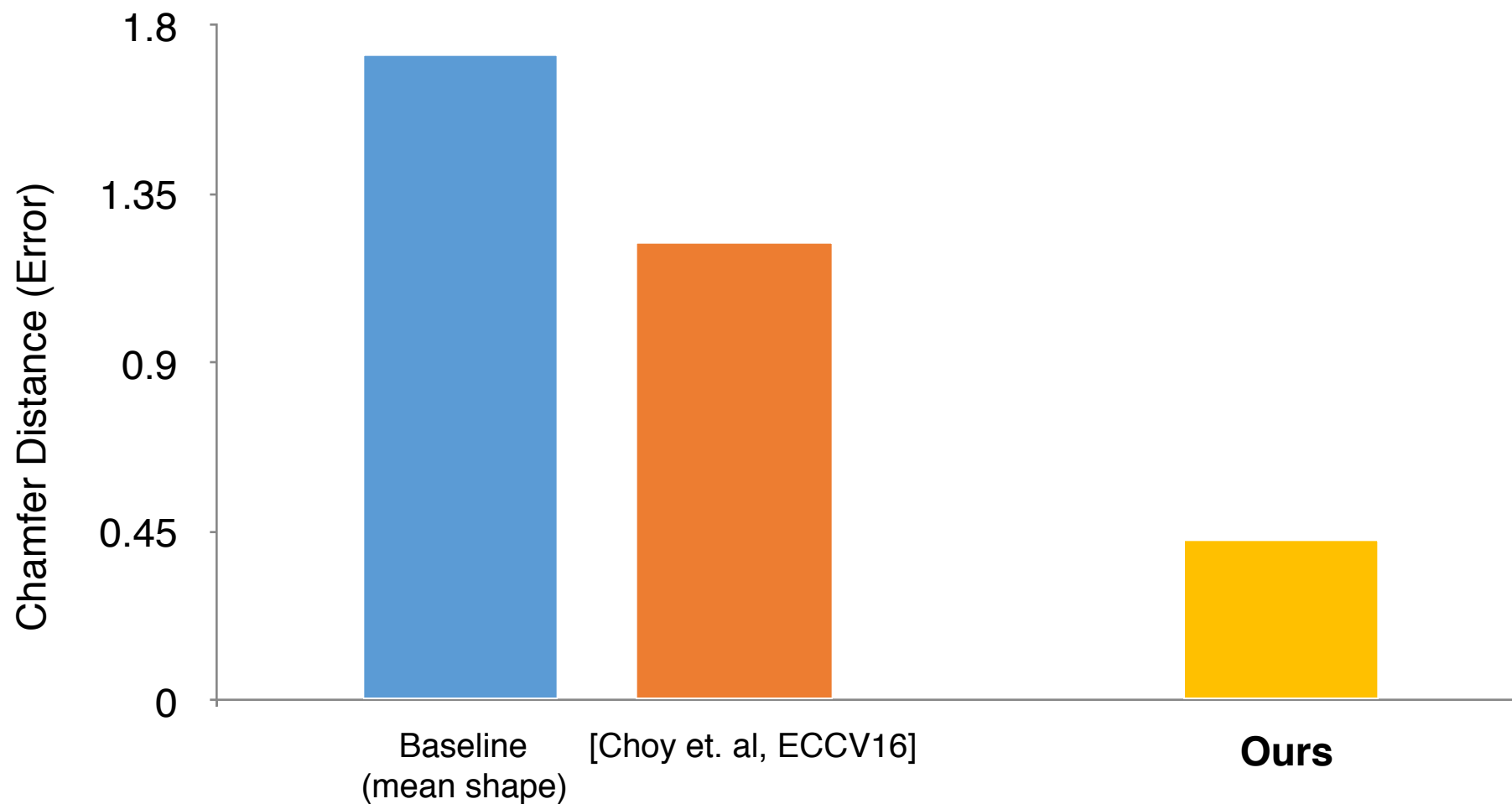
Comparison to state-of-the-art

- Better global structure
- Better details

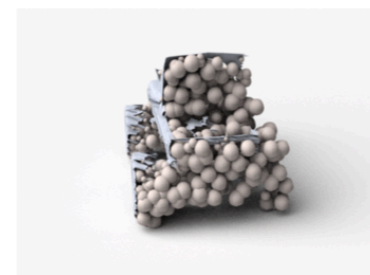
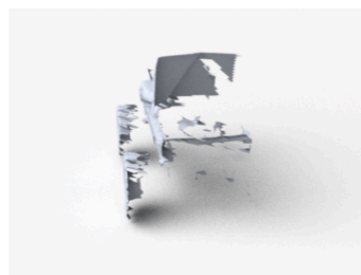
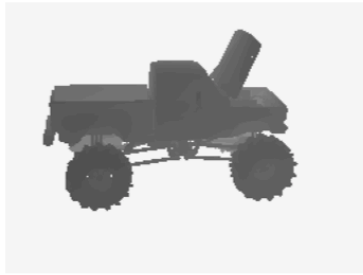
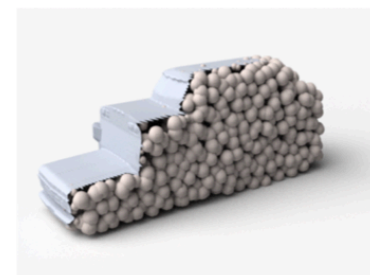
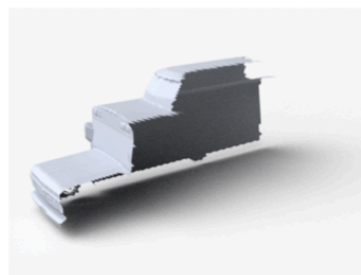
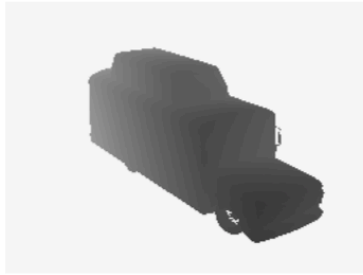
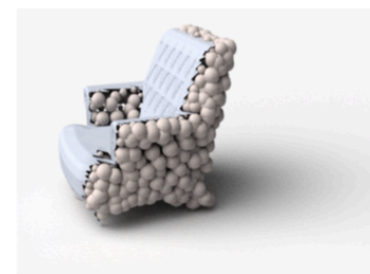


Comparison to state-of-the-art

Trained/tested on 2K object categories



Extension: shape completion for RGBD data



RGBD map (input)

90° view of input

output: completed point cloud

How about learning to predict geometric forms?

Candidates:

**Rasterized form
(regular grids)**

multi-view images

depth map

volumetric

**Geometric form
(irregular)**

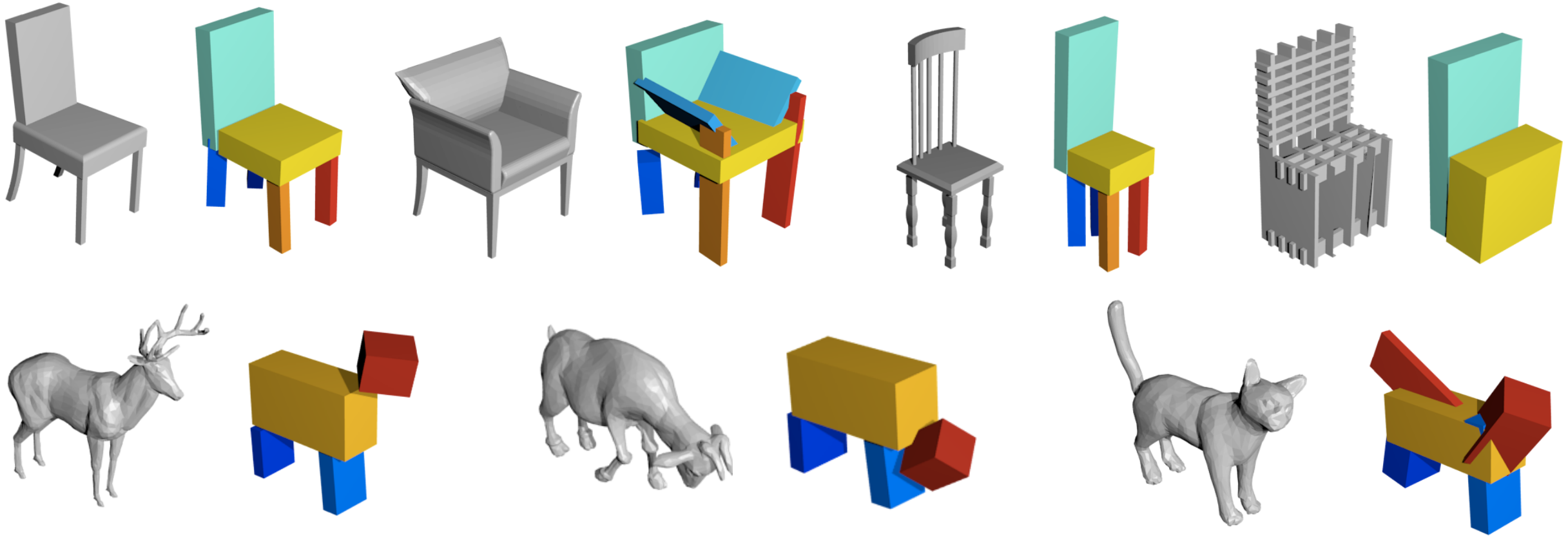
polygonal mesh

point cloud



primitive-based CAD models

Primitive-based assembly



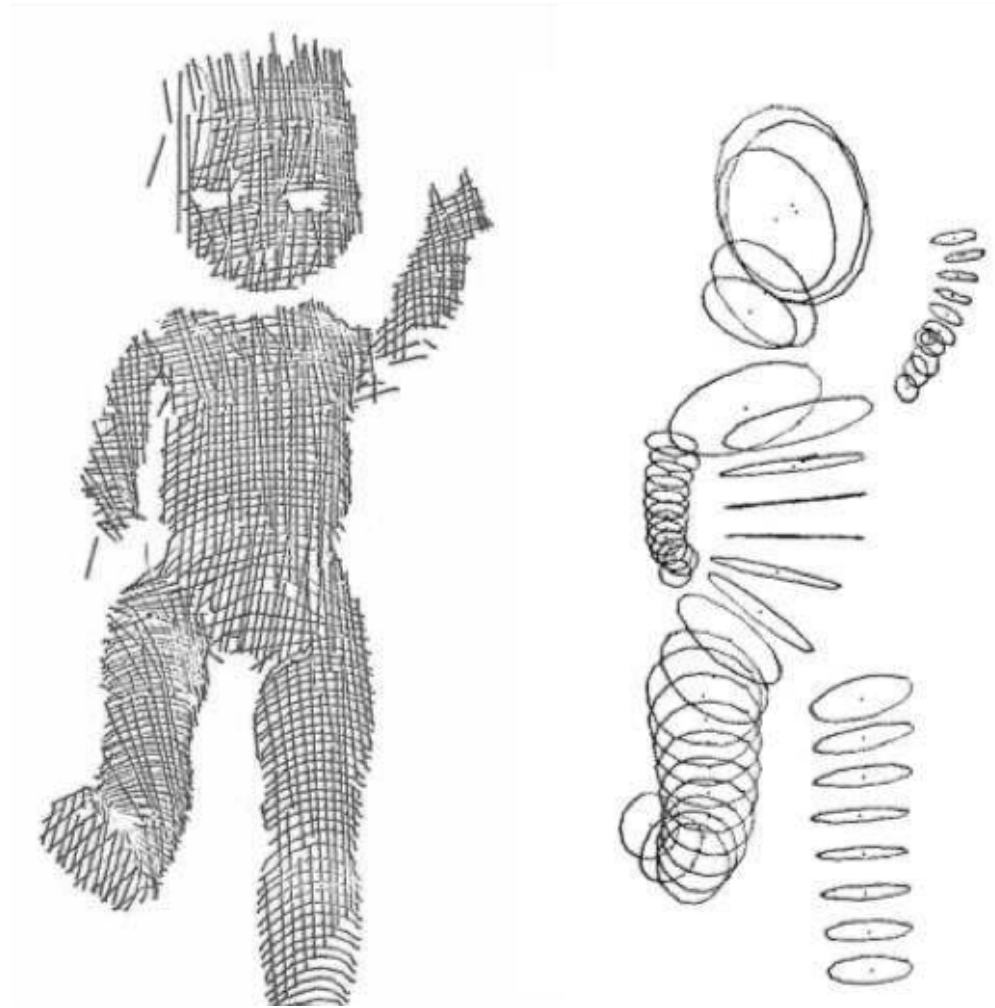
We **learn** to predict a corresponding shape composed by primitives. It allows us to predict **consistent** compositions across objects.

Unsupervised parsing



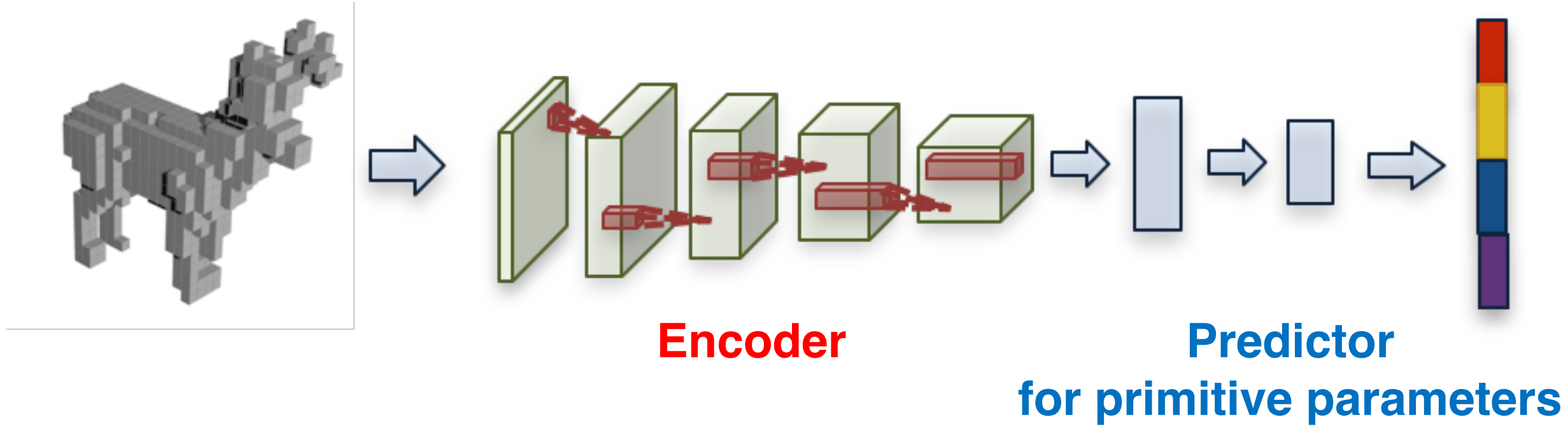
Each point is colored according to the assigned primitive

A historical overview



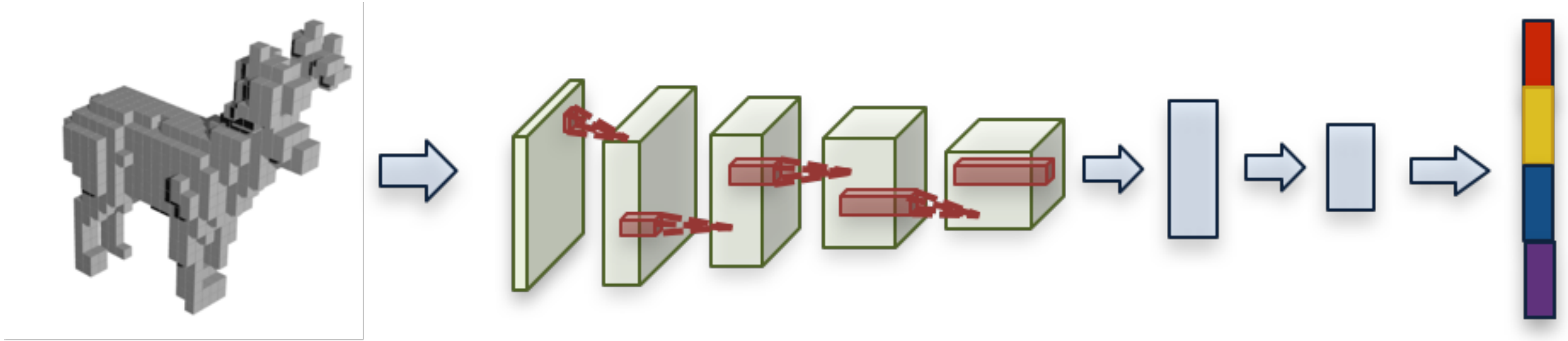
Generalized Cylinders, Binford (1971)

Approach



We predict primitive parameters: size, rotation, translation of M cuboids.

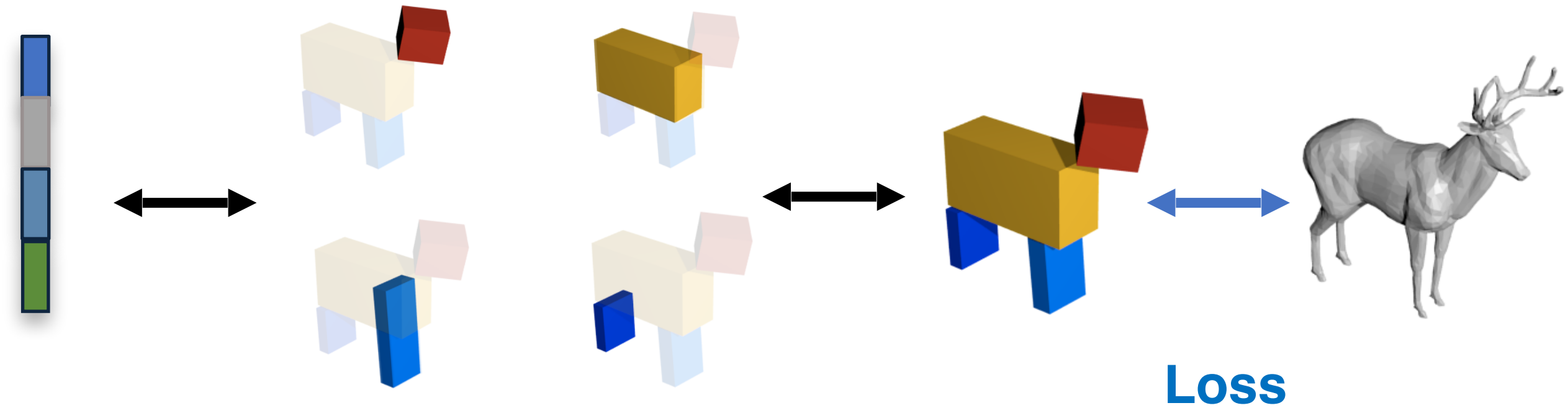
Approach



We predict primitive parameters: size, rotation, translation of M cuboids.

Variable number of parts? We predict “primitive existence probability”

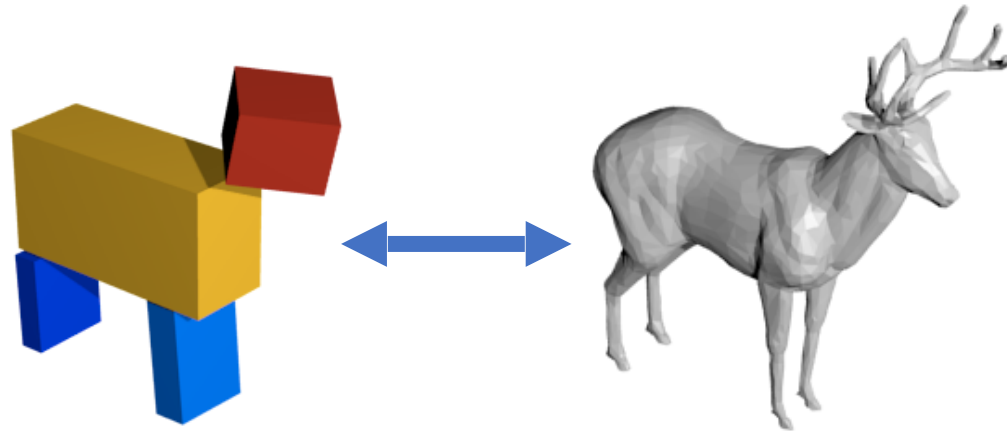
Loss function



Loss function construction

Basic idea: **Chamfer distance!**

$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2^2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2^2$$



Loss function construction

Sample points on the groundtruth mesh and predicted assembly

$$\Delta(\text{deer}, \text{assembly}) + \Delta(\text{deer}, \text{assembly}) + \Delta(\text{deer}, \text{assembly}) \dots + \Delta(\text{deer}, \text{assembly})$$

Each point is a **linear function** of mesh/primitive vertex coordinates

Differentiable!

Loss function construction

Sample points on the groundtruth mesh and predicted assembly

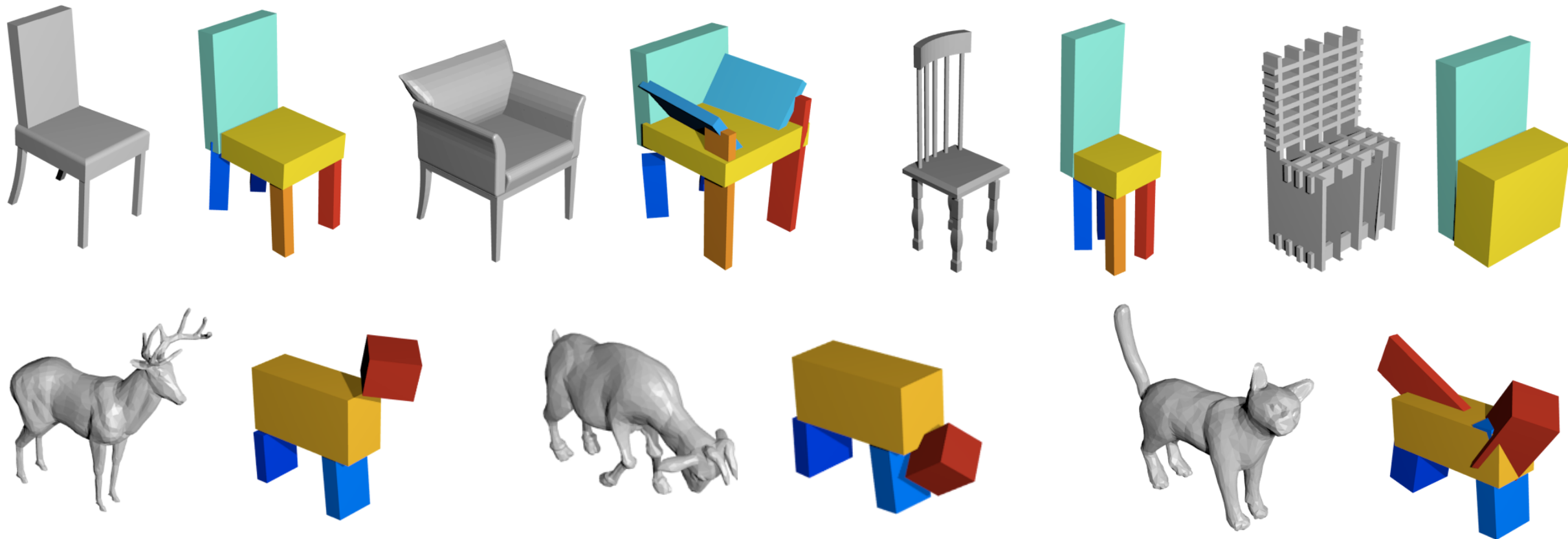
$$\Delta(\text{deer}, \text{assembly}) + \Delta(\text{deer}, \text{assembly}) + \Delta(\text{deer}, \text{assembly}) \dots + \Delta(\text{deer}, \text{assembly})$$

Each point is a **linear function** of mesh/primitive vertex coordinates

Differentiable!

Speed up the computation leveraging parameterization of primitives

Consistent primitive configurations



Primitive locations are **consistent** due to the **smoothness** of primitive prediction network

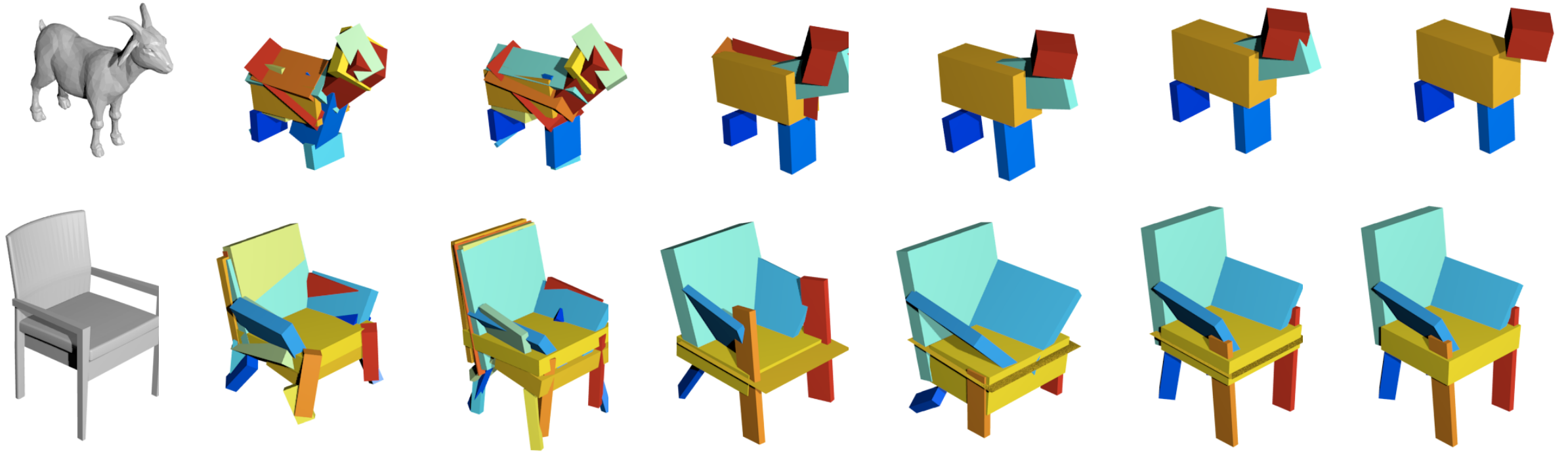
Unsupervised parsing



Method	[31] (initial)	[31] (refined)	Ours
Accuracy	78.6	84.8	89.0

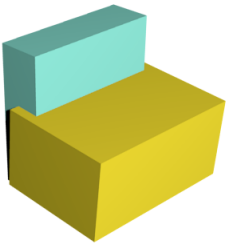
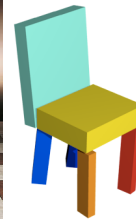
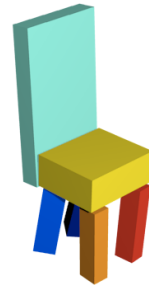
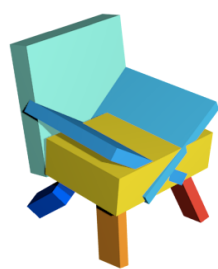
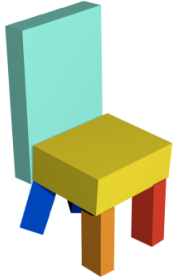
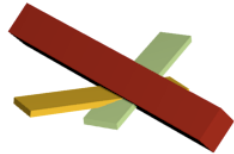
Mean accuracy (face area) on Shape COSEG chairs.

Analysis



Shapes become more parsimonious as training progresses (due to our parsimony reward)

Image-based modeling



Agenda

- Point cloud generation
- **Point cloud analysis**

Applications of Point Set Learning

- **Robot Perception**

What and where are the objects in a LiDAR scanned scene?

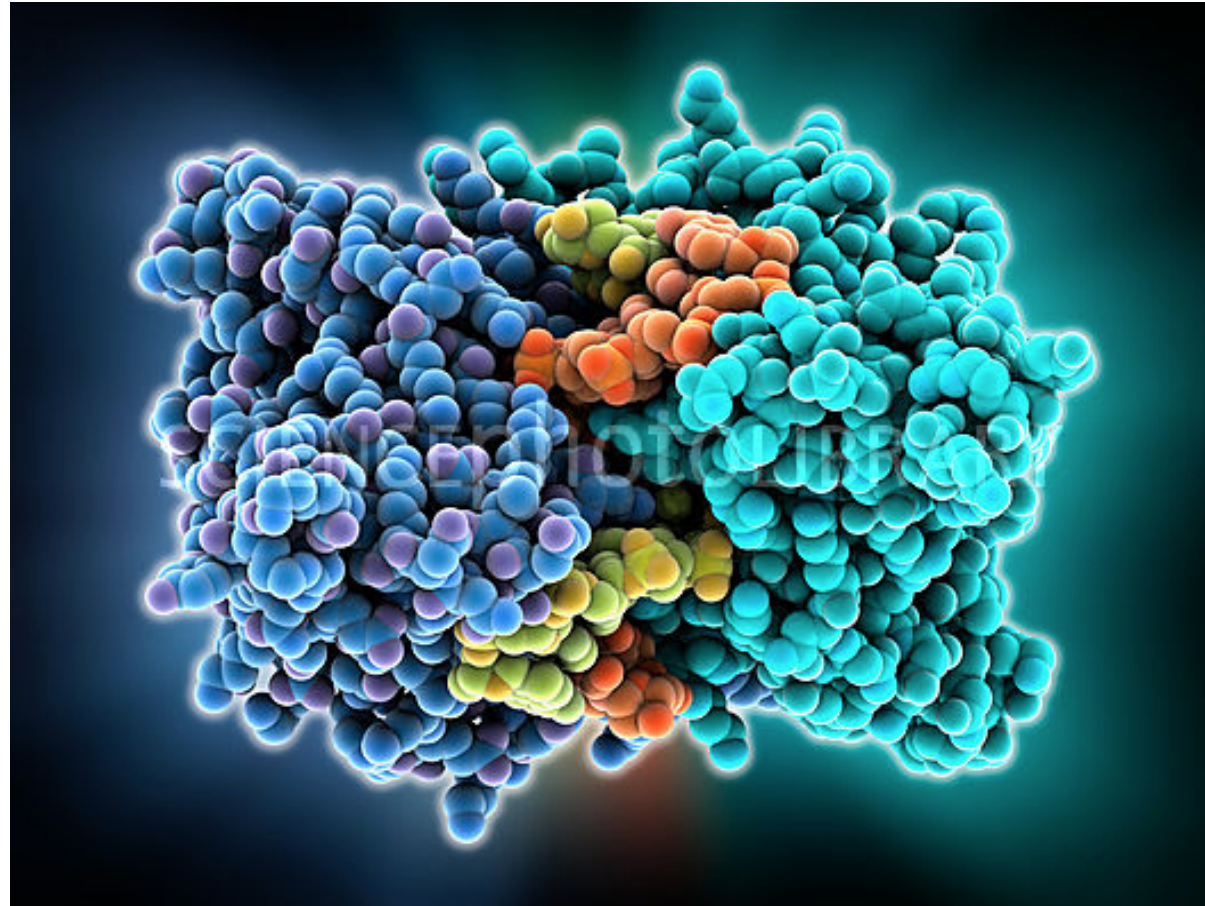


<https://3dprint.com/116569/self-driving-cars-privacy/>

Applications of Point Set Learning

- **Molecular Biology**

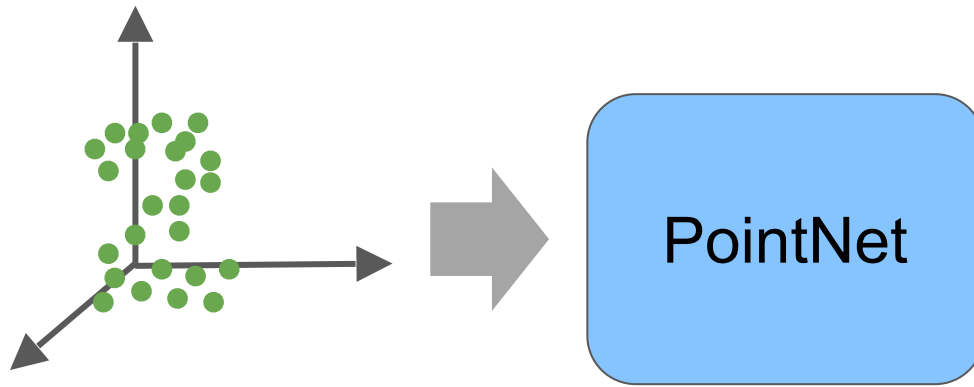
Can we infer an enzyme's category (reactions they catalyze) from its structure?



EcoRV restriction enzyme molecule, LAGUNA DESIGN/SCIENCE PHOTO LIBRARY

Directly process point cloud data

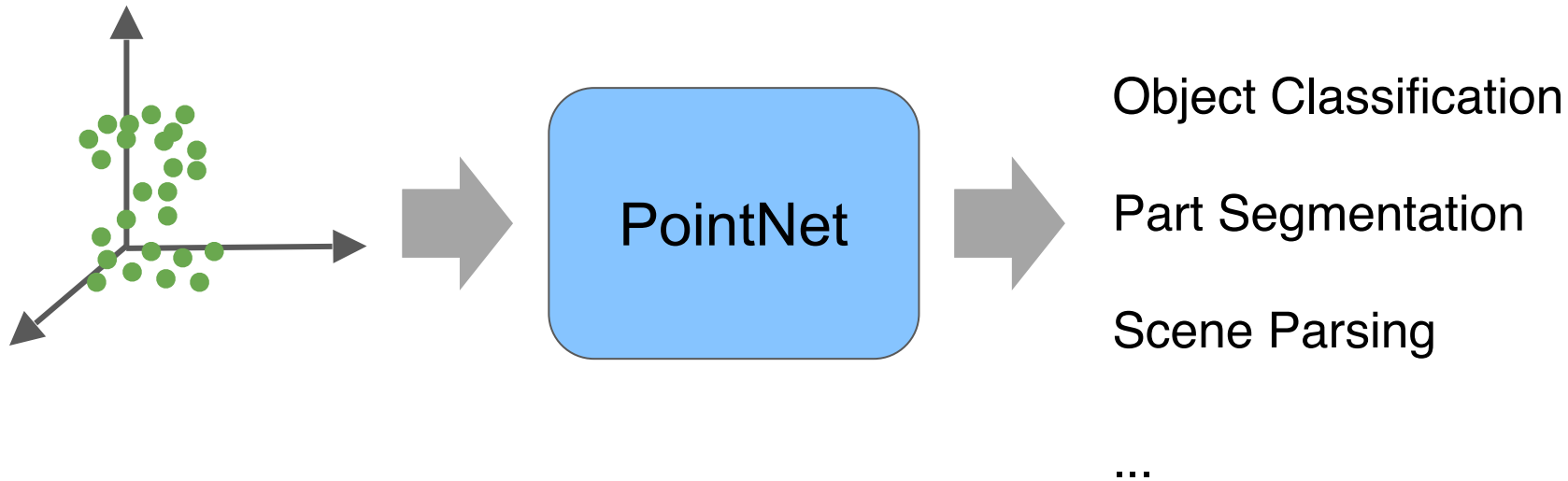
End-to-end learning for **unstructured, unordered** point data



Directly process point cloud data

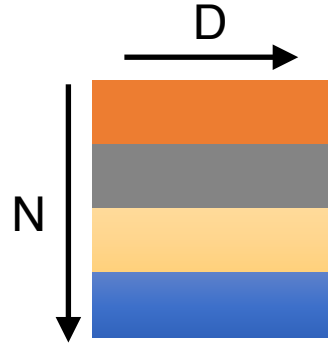
End-to-end learning for **unstructured, unordered** point data

Unified framework for various tasks



Properties of a desired neural network on point clouds

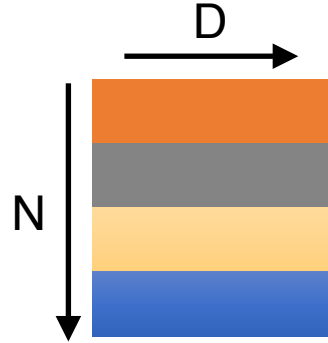
Point cloud: N **orderless** points, each represented by a D dim coordinate



2D array representation

Properties of a desired neural network on point clouds

Point cloud: N **orderless** points, each represented by a D dim coordinate



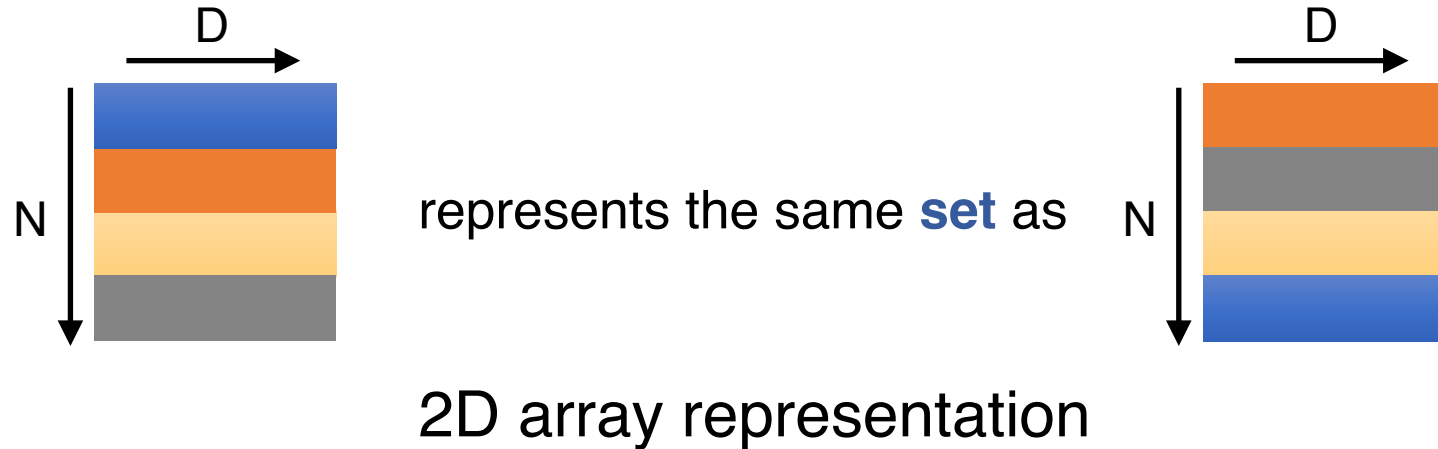
2D array representation

Permutation invariance

Transformation invariance

Properties of a desired neural network on point clouds

Point cloud: N **orderless** points, each represented by a D dim coordinate



Permutation invariance

Permutation invariance: Symmetric function

$$f(x_1, x_2, \dots, x_n) \equiv f(x_{\pi_1}, x_{\pi_2}, \dots, x_{\pi_n}), \quad x_i \in \mathbb{R}^D$$

Examples:

$$f(x_1, x_2, \dots, x_n) = \max\{x_1, x_2, \dots, x_n\}$$

$$f(x_1, x_2, \dots, x_n) = x_1 + x_2 + \dots + x_n$$

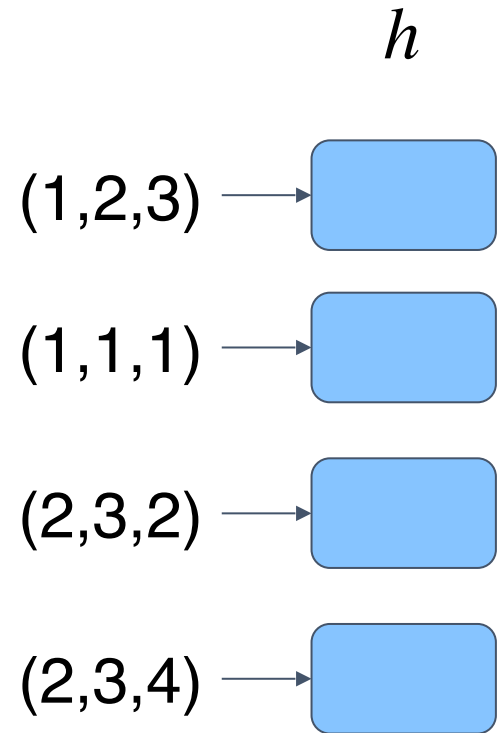
...

Construct symmetric function family

Observe: $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$ is symmetric if g is symmetric

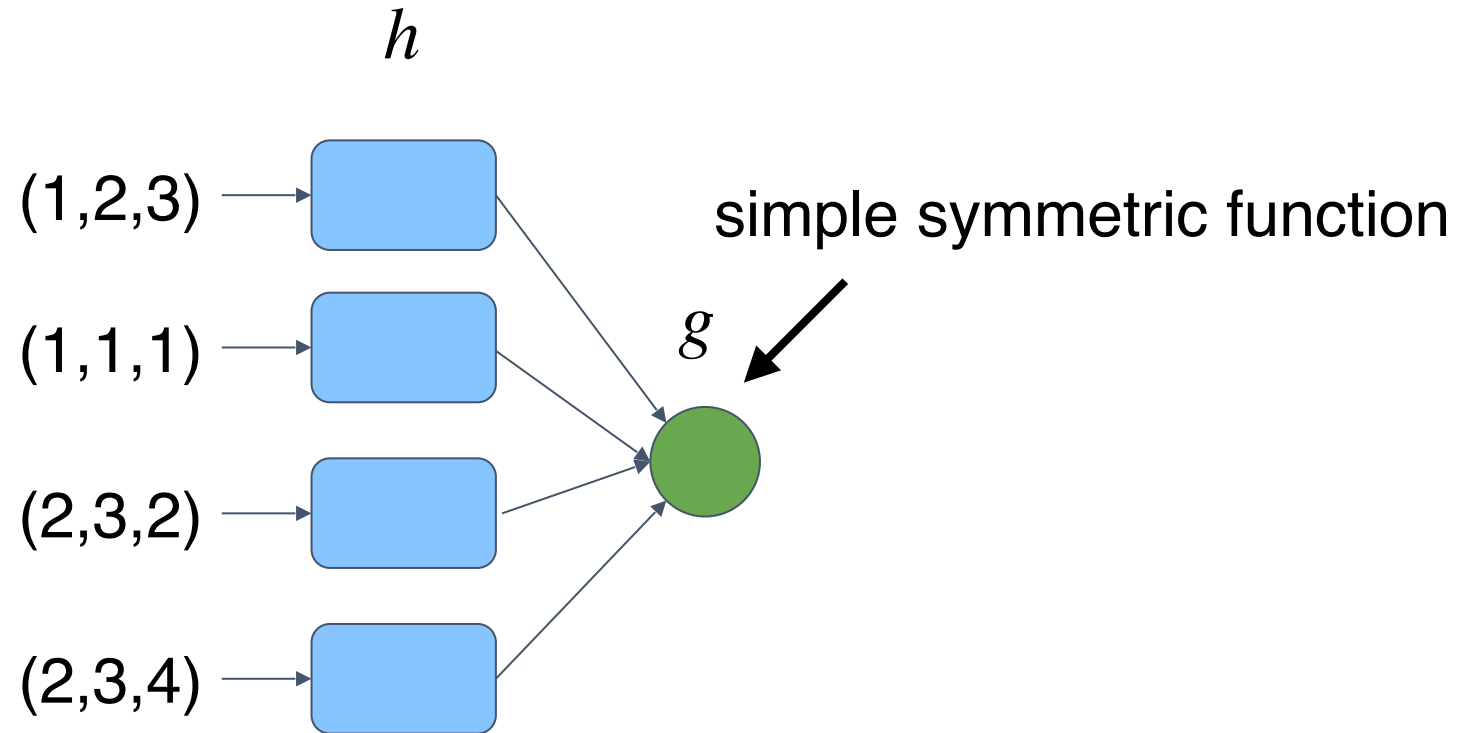
Construct symmetric function family

Observe: $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$ is symmetric if g is symmetric



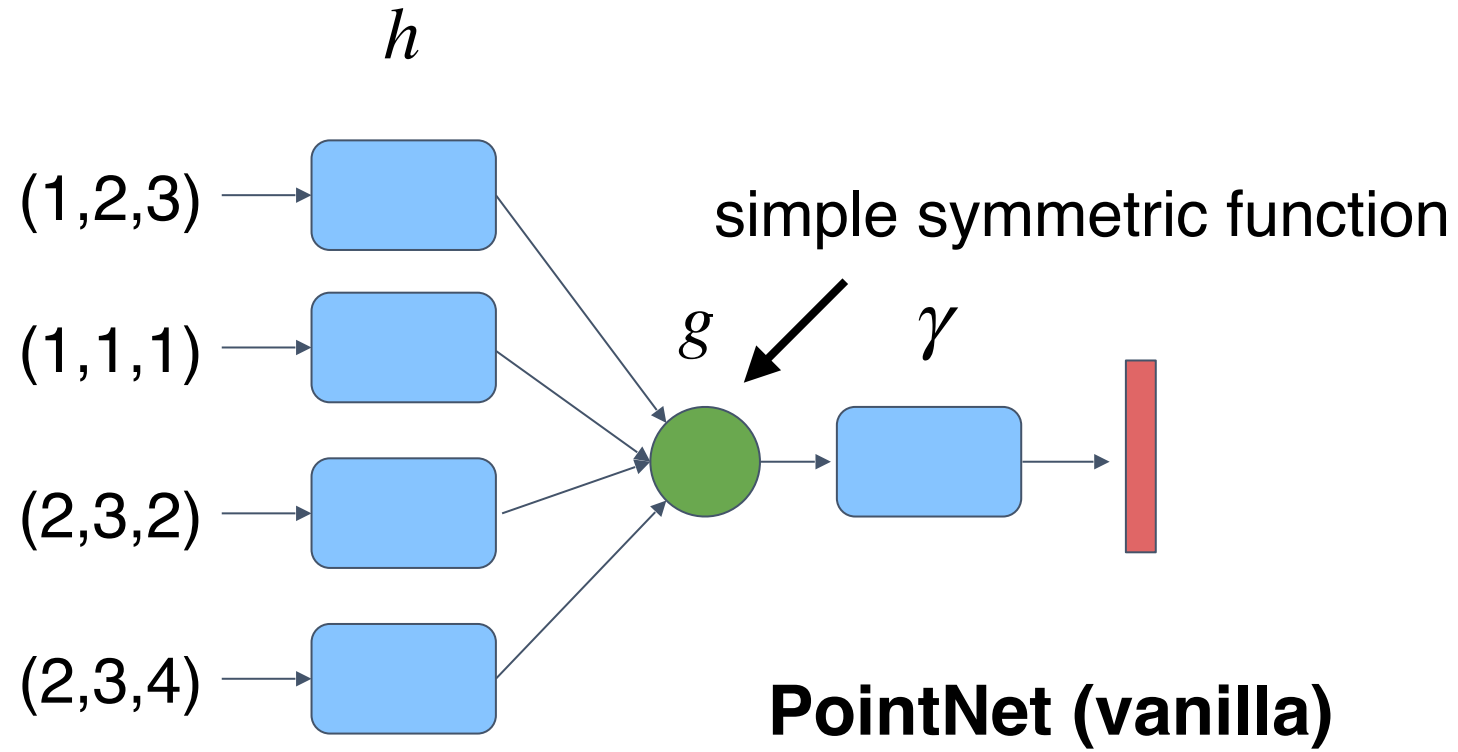
Construct symmetric function family

Observe: $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$ is symmetric if g is symmetric

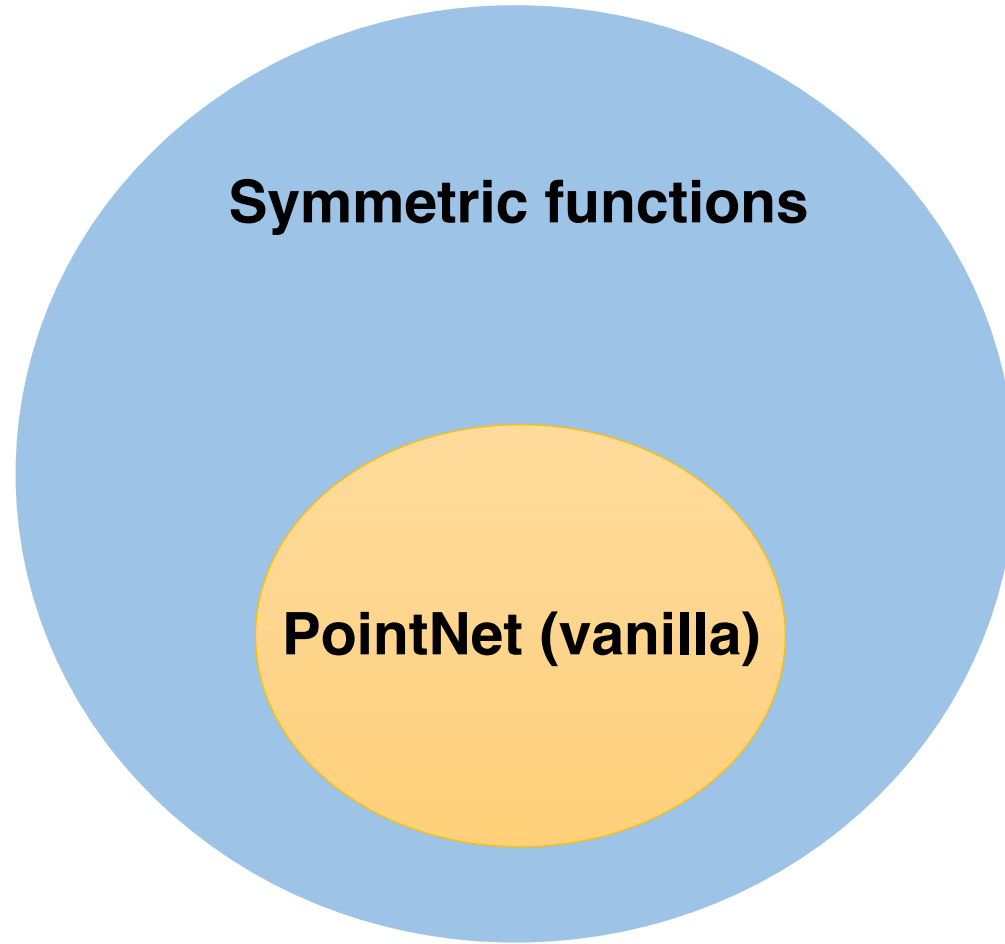


Construct symmetric function family

Observe: $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$ is symmetric if g is symmetric



Q: What symmetric functions can be constructed by PointNet?



A: Universal approximation to **continuous** symmetric functions

Theorem:

A Hausdorff continuous symmetric function $f : 2^{\mathcal{X}} \rightarrow \mathbb{R}$ can be arbitrarily approximated by PointNet.

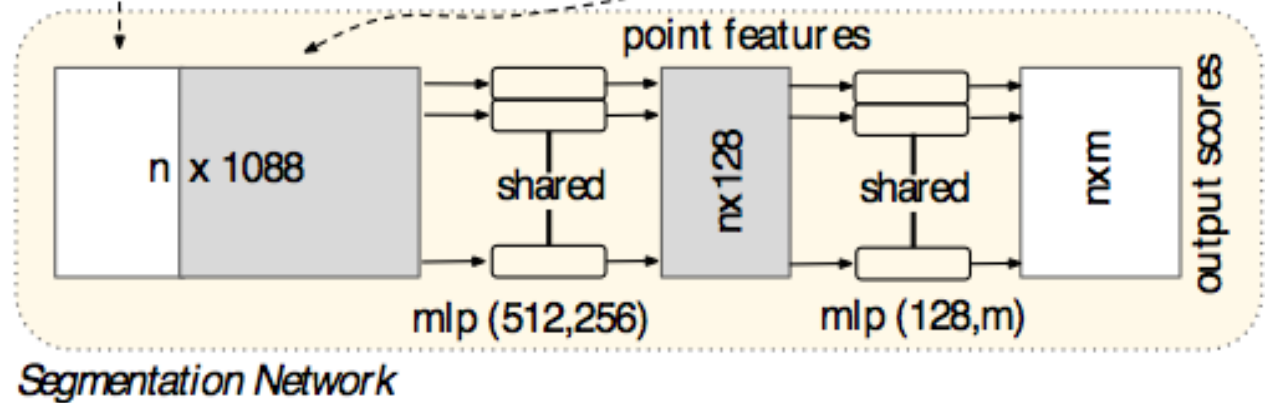
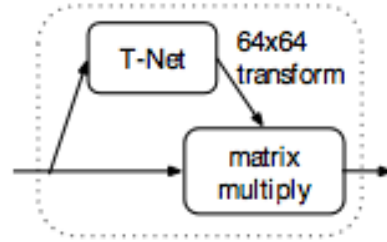
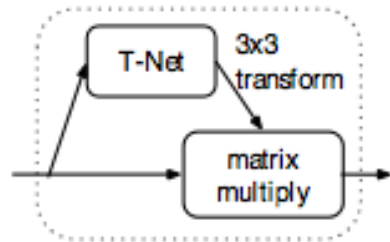
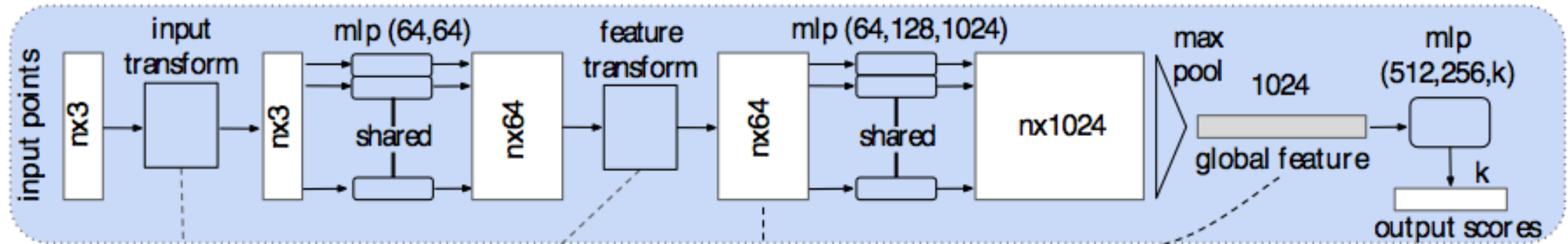
$$\left| f(S) - \gamma \left(\underset{x_i \in S}{\text{MAX}} \{h(x_i)\} \right) \right| < \epsilon$$

$$S \subseteq \mathbb{R}^d,$$

PointNet (vanilla)

PointNet Architecture

Classification Network

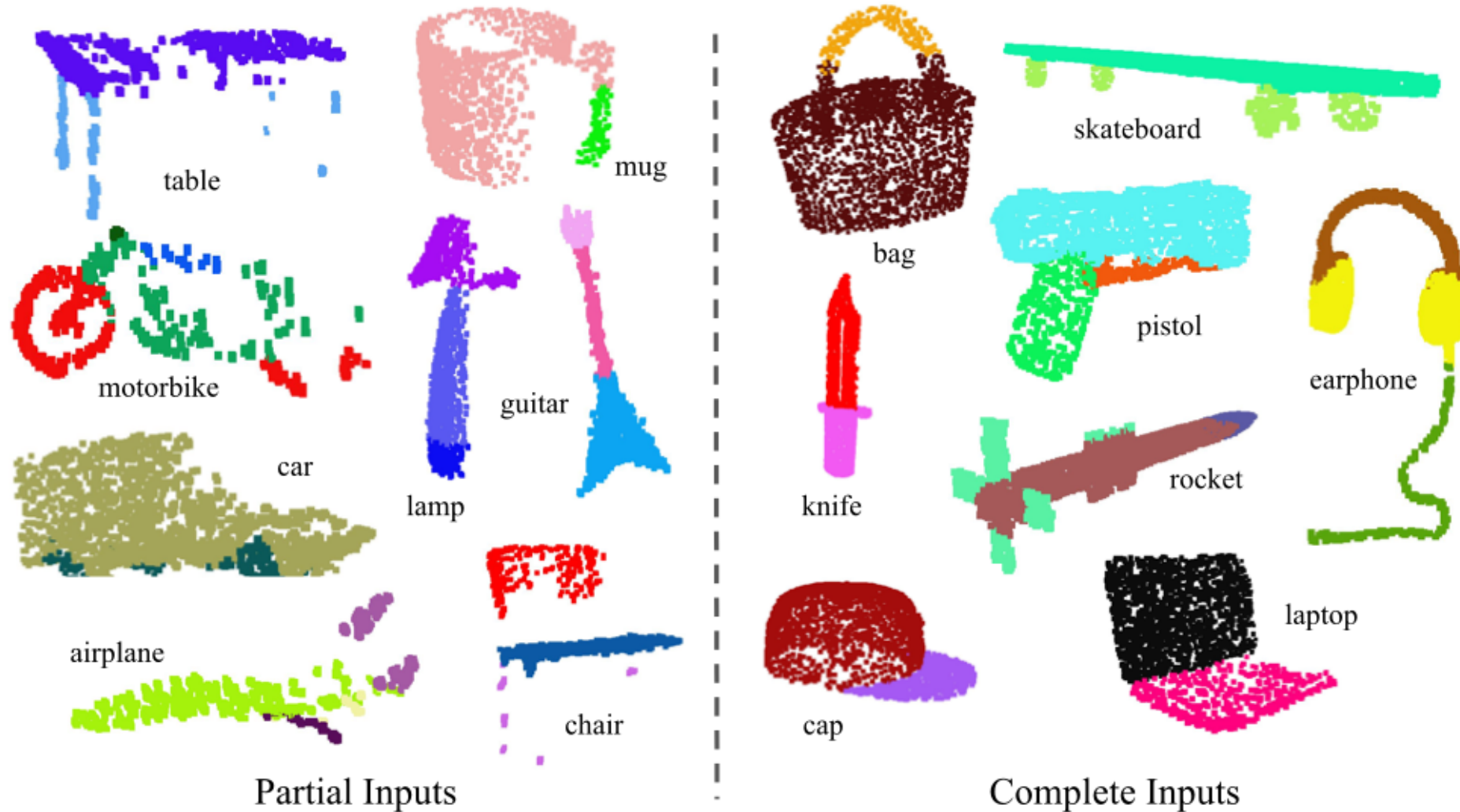


Results on Object Classification

Object Classification Accuracy on ModelNet40

	input	#views	accuracy avg. class	accuracy overall
SPH [12]	mesh	-	68.2	-
3DShapeNets [29]	volume	1	77.3	84.7
VoxNet [18]	volume	12	83.0	85.9
Subvolume [19]	volume	20	86.0	89.2
LFD [29]	image	10	75.5	-
MVCNN [24]	image	80	90.1	-
Ours baseline	point	-	72.6	77.4
Ours PointNet	point	1	86.2	89.2

Results on Object Part Segmentation



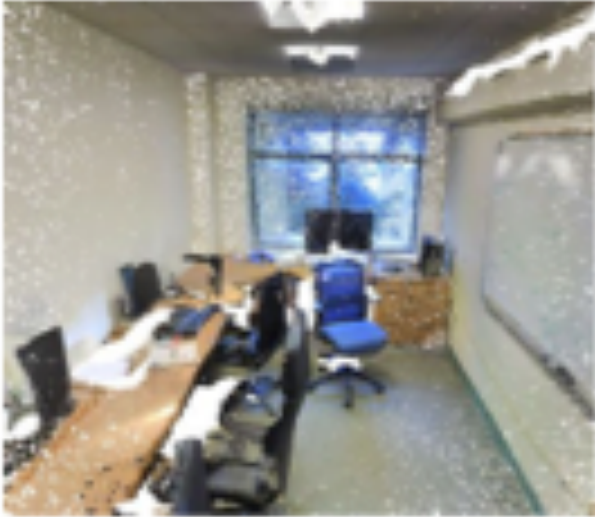
Results on Object Part Segmentation

Part Segmentation mIoU on ShapeNet Part Dataset

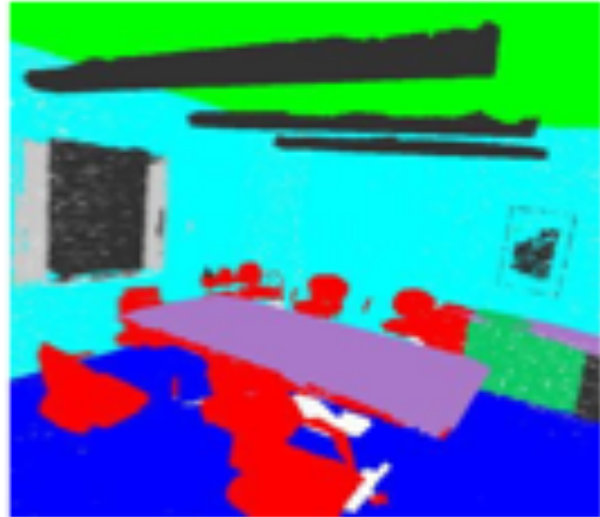
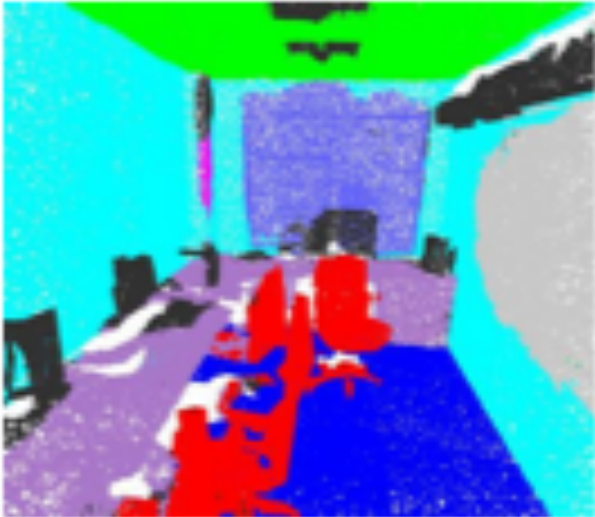
	mean	aero	bag	cap	car	chair	ear phone	guitar	knife	lamp	laptop	motor	mug	pistol	rocket	skate board	table
# shapes		2690	76	55	898	3758	69	787	392	1547	451	202	184	283	66	152	5271
Wu [28]	-	63.2	-	-	-	73.5	-	-	-	74.4	-	-	-	-	-	-	74.8
Yi [30]	81.4	81.0	78.4	77.7	75.7	87.6	61.9	92.0	85.4	82.5	95.7	70.6	91.9	85.9	53.1	69.8	75.3
3DCNN	79.4	75.1	72.8	73.3	70.0	87.2	63.5	88.4	79.6	74.4	93.9	58.7	91.8	76.4	51.2	65.3	77.1
Ours	83.7	83.4	78.7	82.5	74.9	89.6	73.0	91.5	85.9	80.8	95.3	65.2	93.0	81.2	57.9	72.8	80.6

Results on Semantic Scene Segmentation

Input



Output



Results on Semantic Scene Parsing

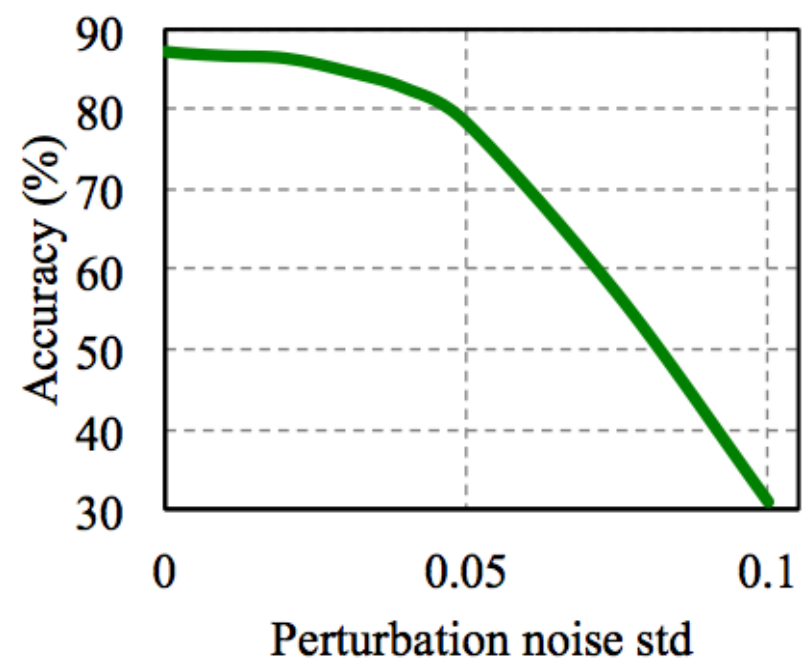
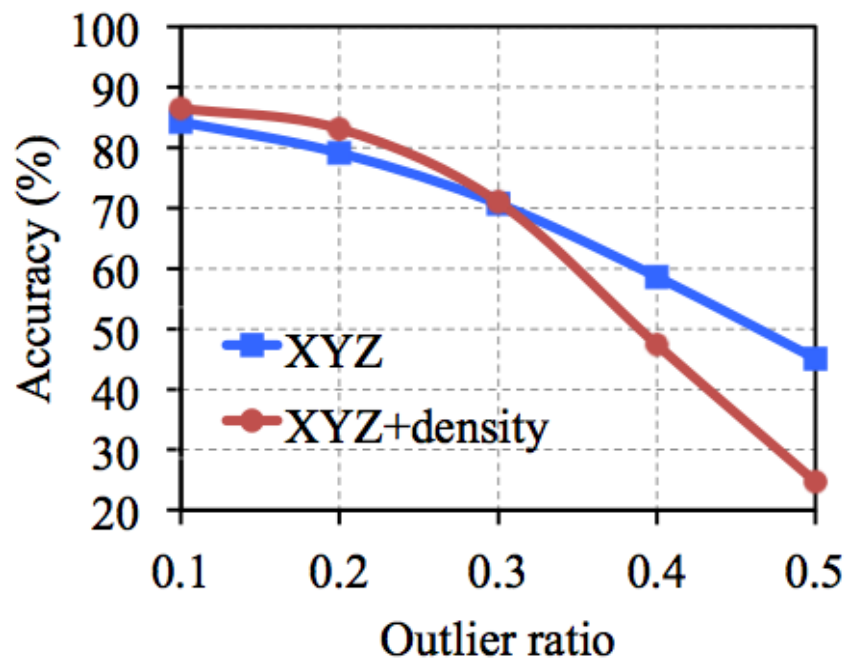
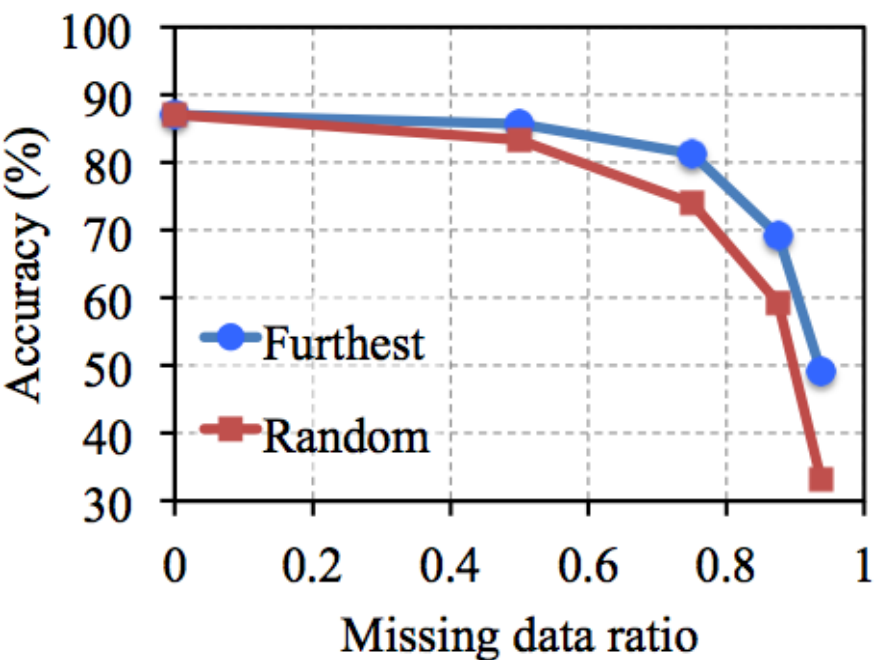
Semantic Segmentation (point based)
on Stanford Semantic Parsing dataset

	mean IoU	overall accuracy
Ours baseline	20.12	53.19
Ours PointNet	47.71	78.62

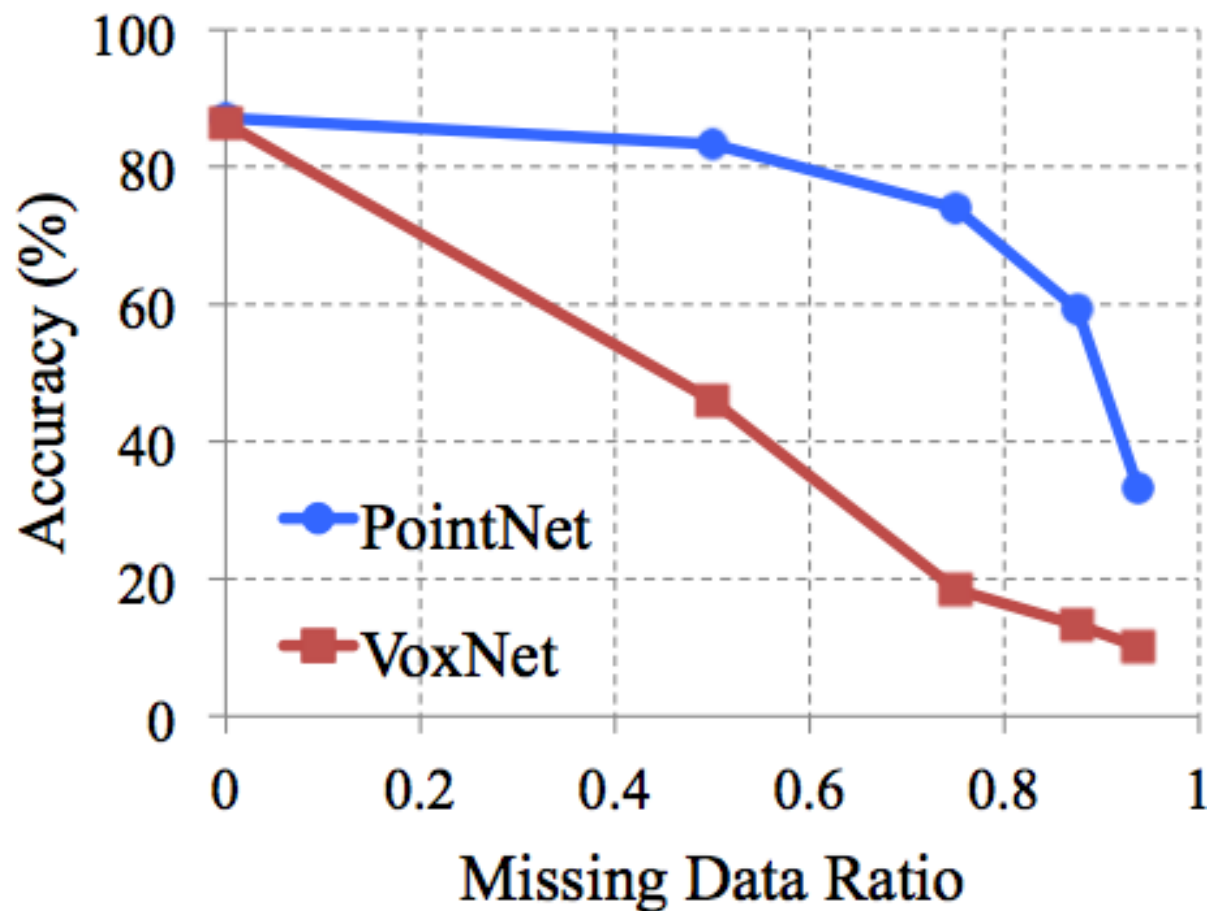
3D Object Detection (bounding box based)

	table	chair	sofa	board	mean
# instance	455	1363	55	137	
Armeni et al. [2]	46.02	16.15	6.78	3.91	18.22
Ours	46.67	33.80	4.76	11.72	24.24

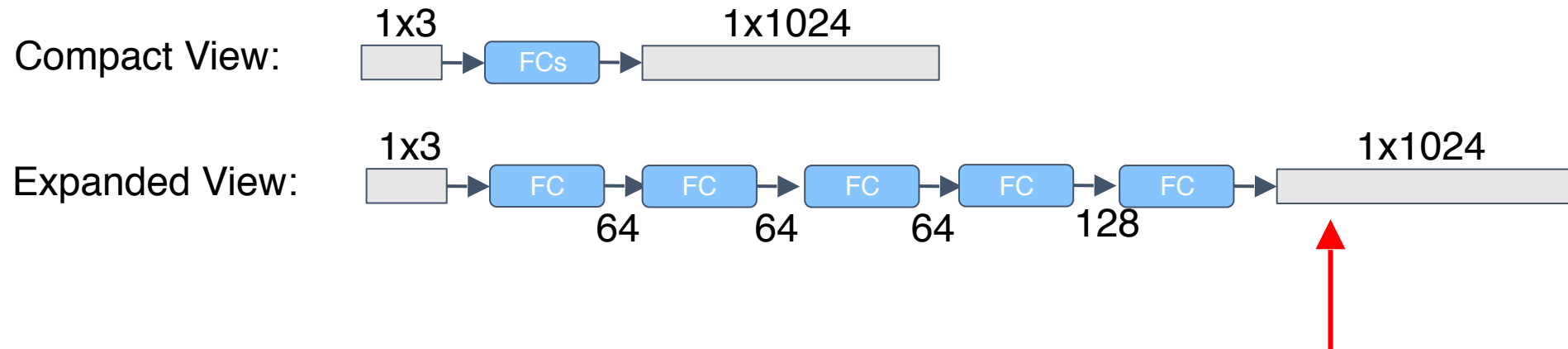
Robustness to Data Corruption



Robustness to Data Corruption



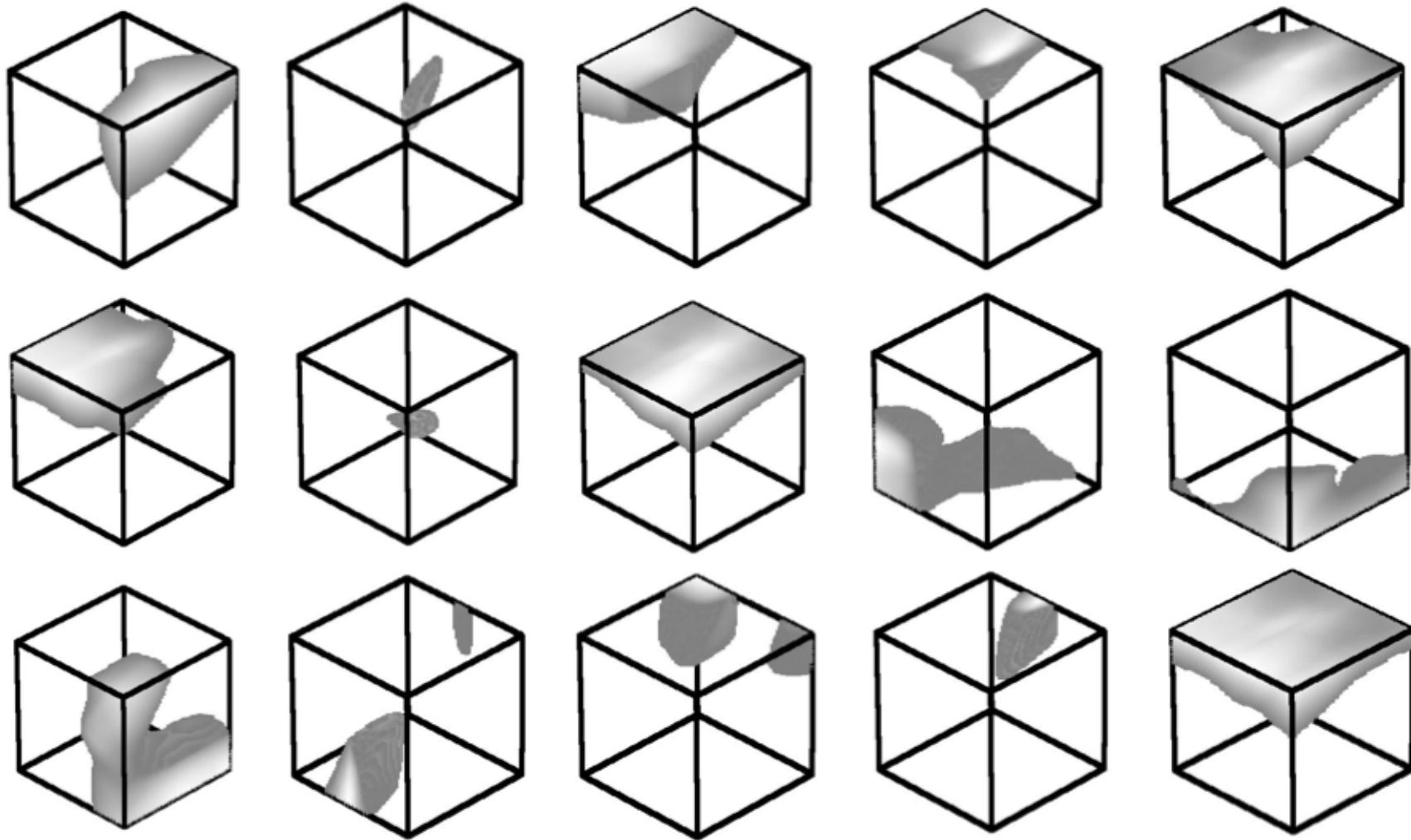
Visualizing Point Functions



Which input point will activate neuron j?

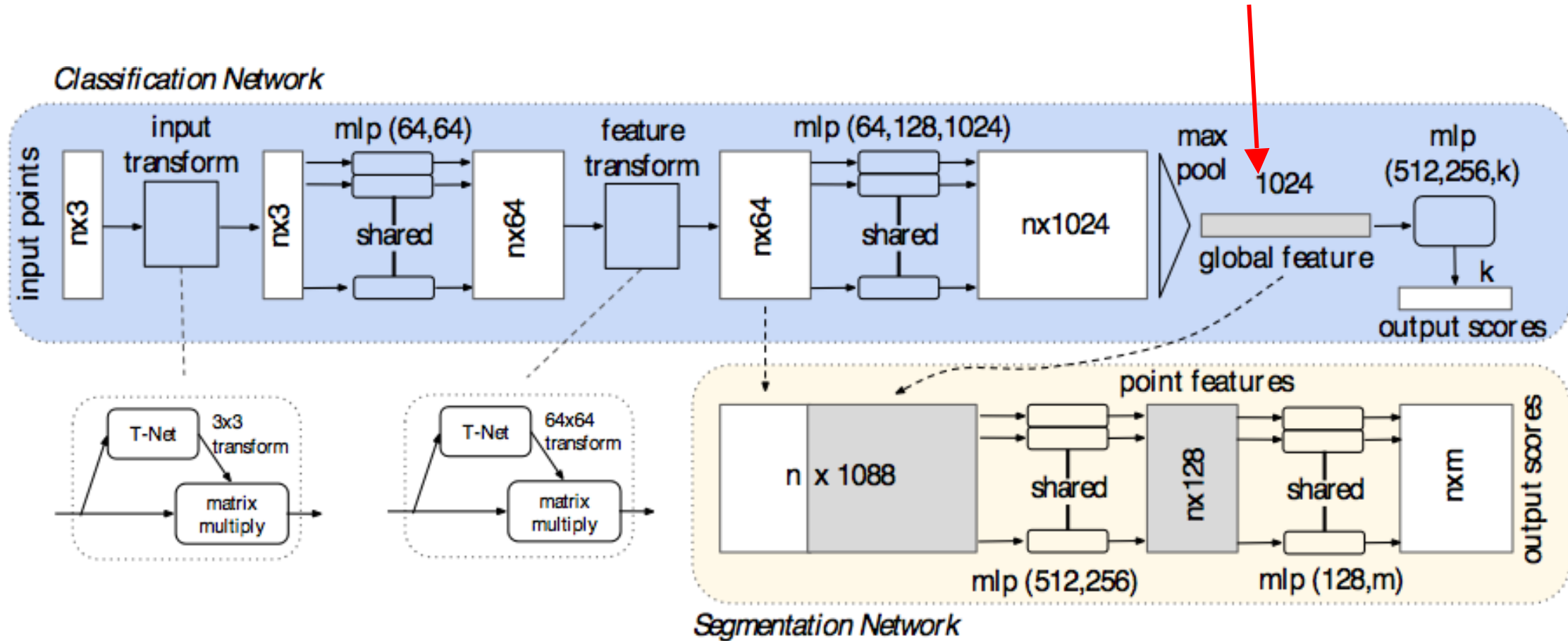
Find the top-K points in a dense volumetric grid that activates neuron j.

Visualizing Point Functions

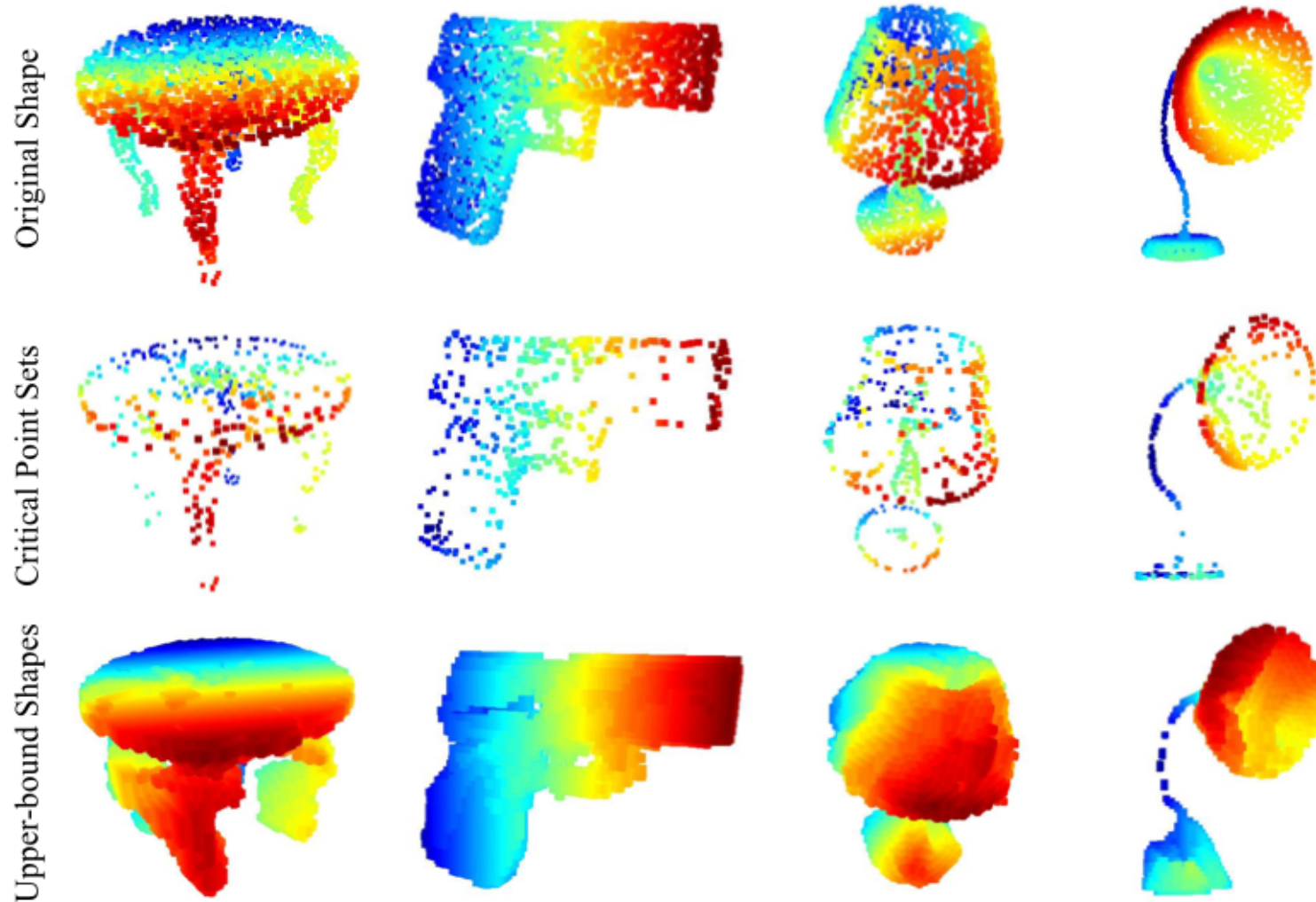


Visualizing Global Point Cloud Features

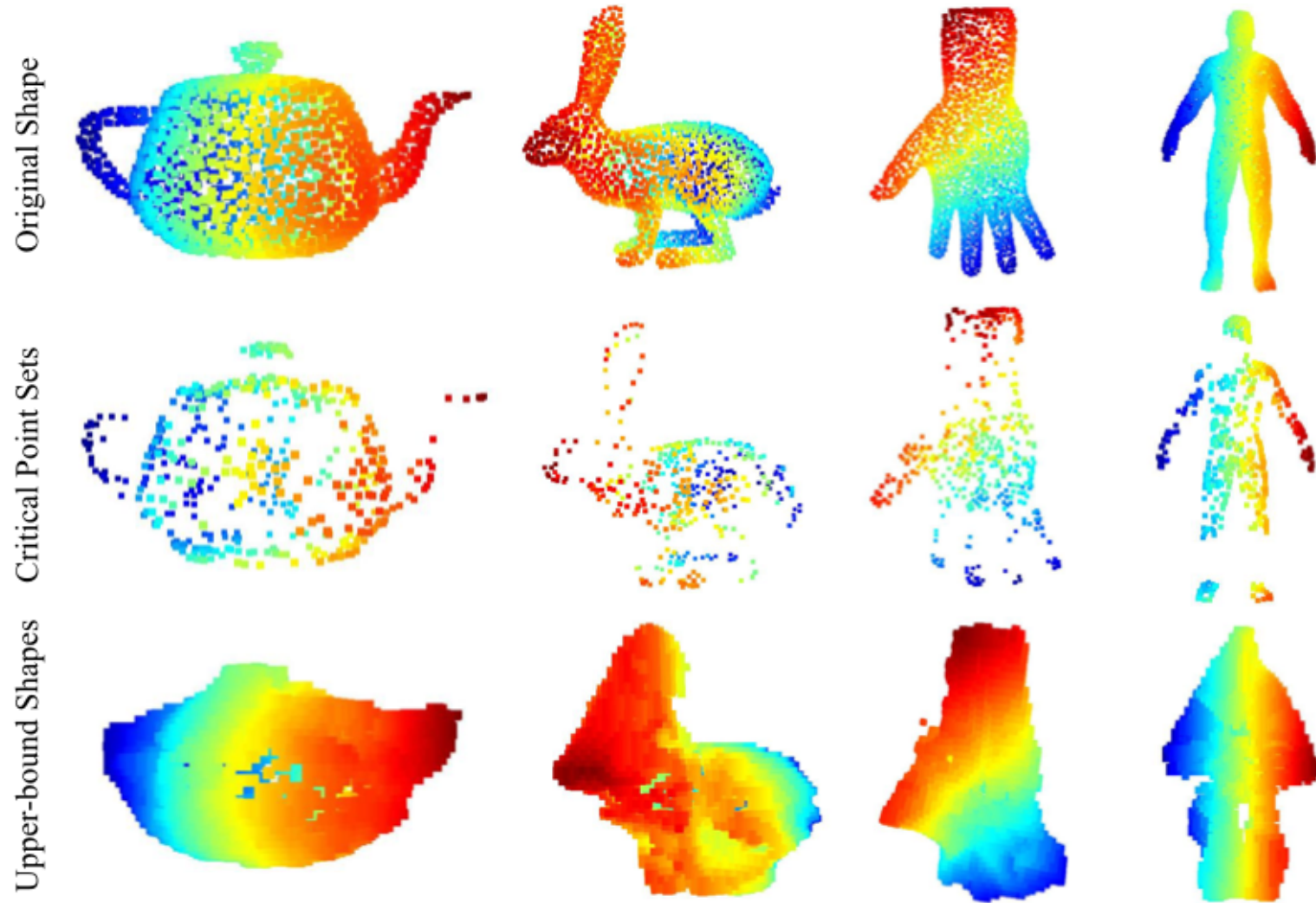
What's captured and left out here?



Visualizing Global Point Cloud Features

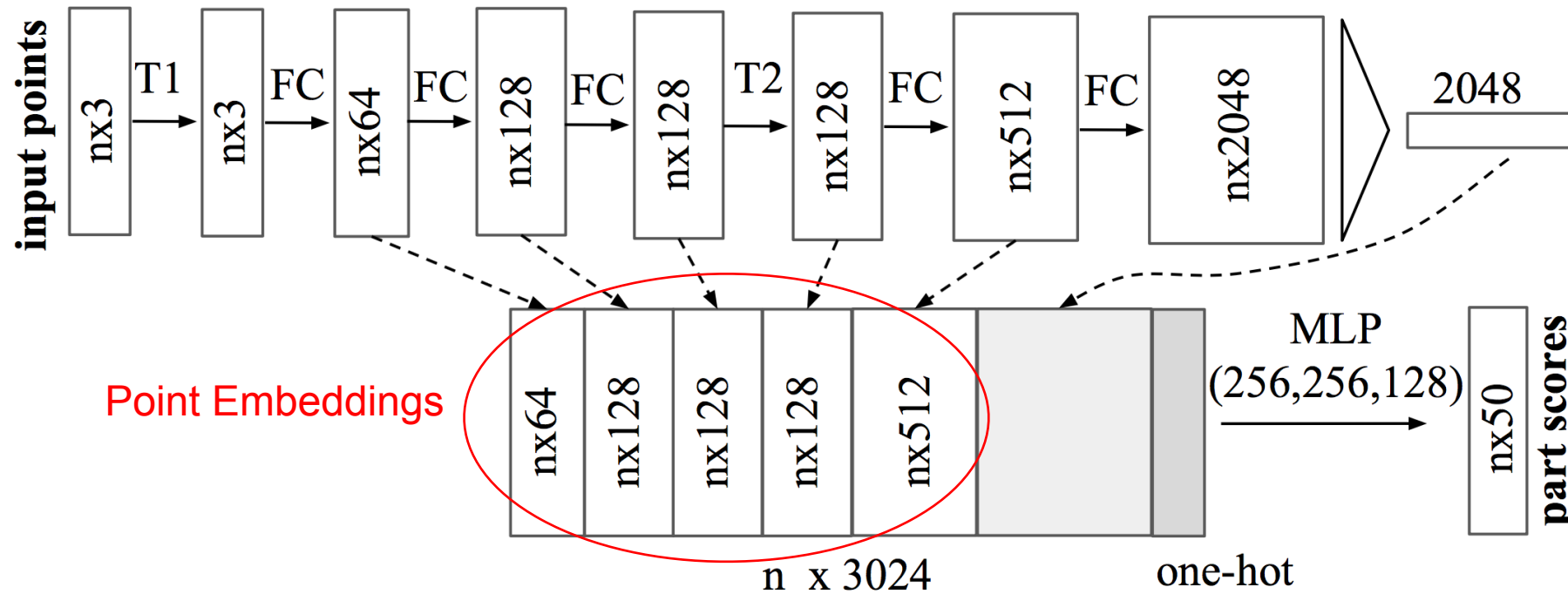


Visualizing Global Point Cloud Features (OOS)



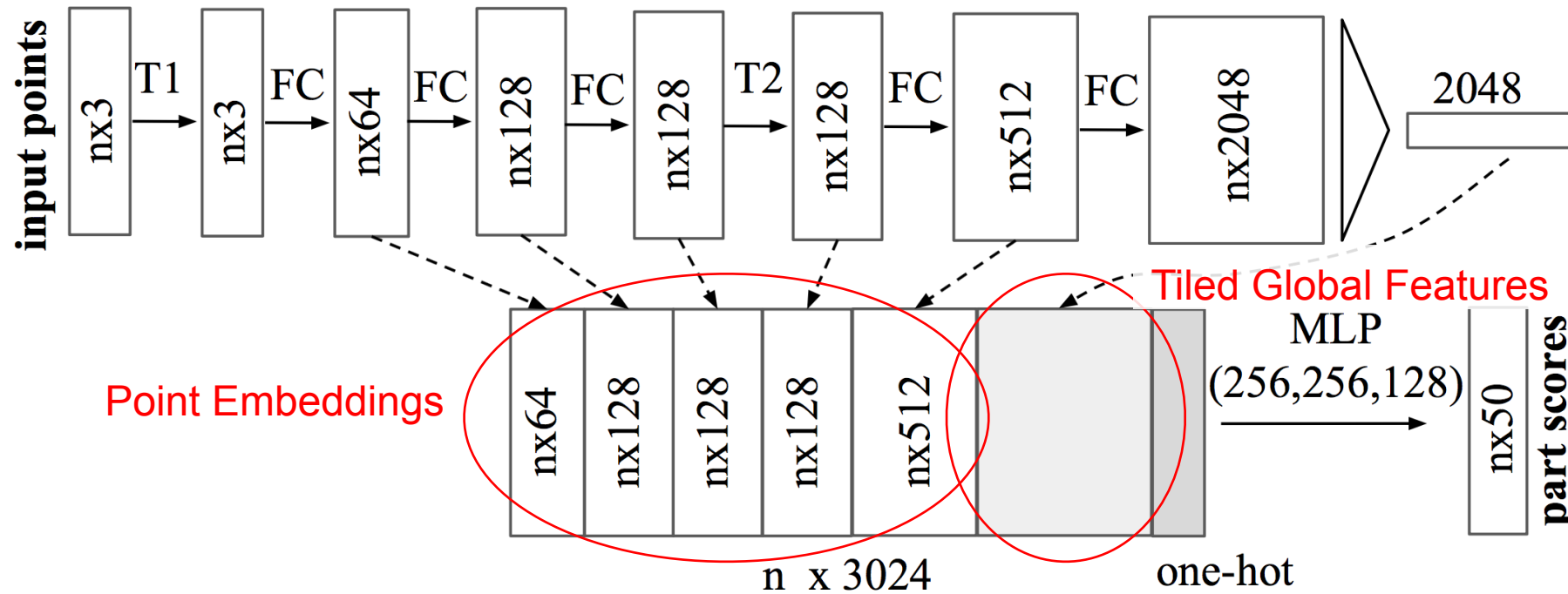
Previous Work: PointNet v1.0

Segmentation Network



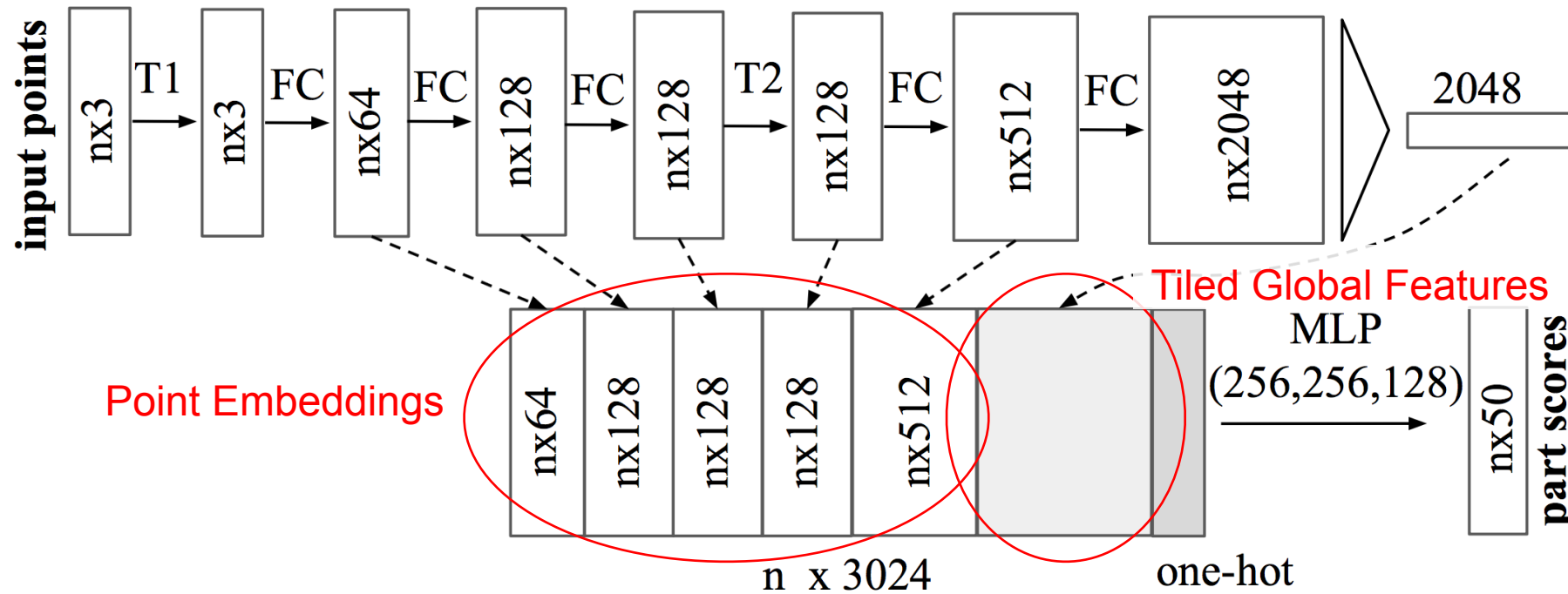
Previous Work: PointNet v1.0

Segmentation Network



Previous Work: PointNet v1.0

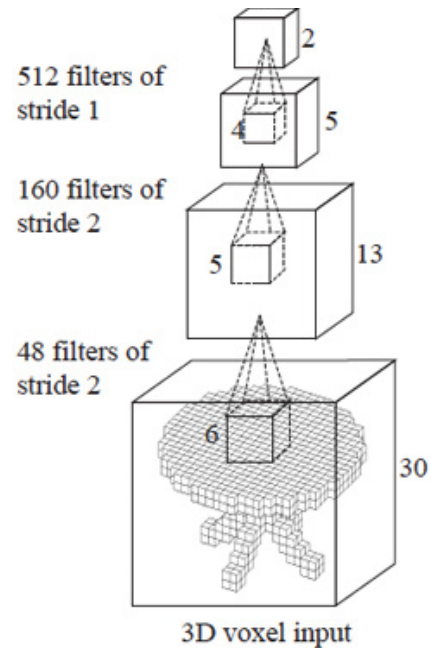
Segmentation Network



- No local context for each point!

Limitations of PointNet v1.0

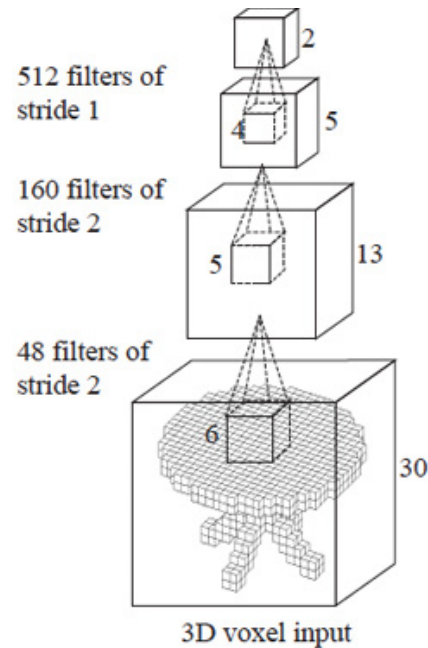
- Hierarchical Feature Learning
- Increasing receptive field



3D CNN (Wu et al.)

Limitations of PointNet v1.0

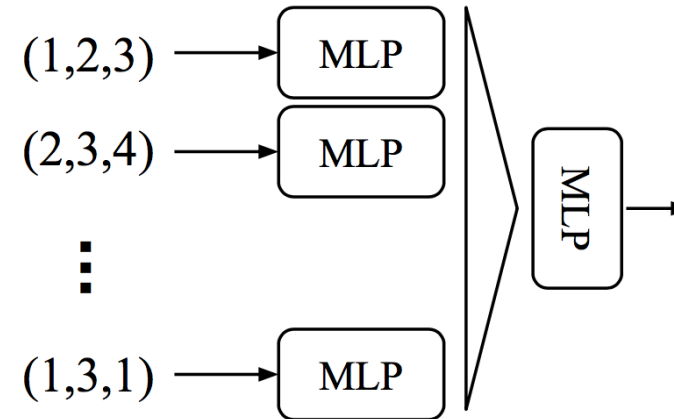
- Hierarchical Feature Learning
- Increasing receptive field



3D CNN (Wu et al.)

V.S.

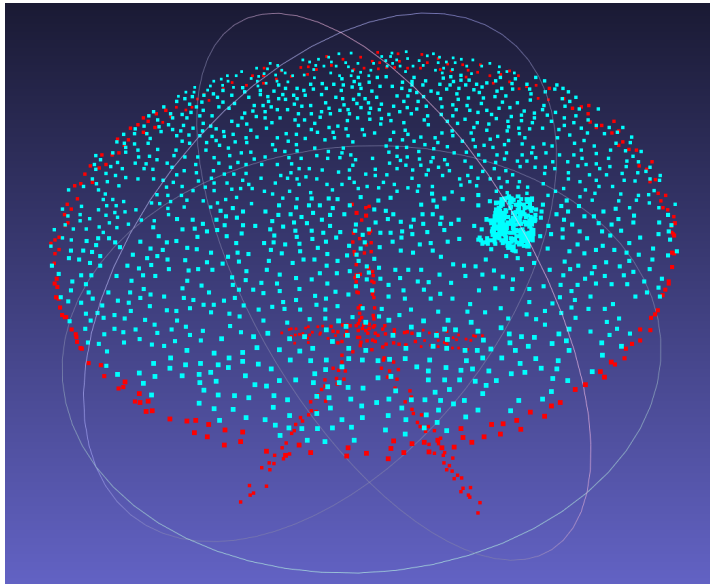
Global Feature Learning
Receptive field:
one point OR all points



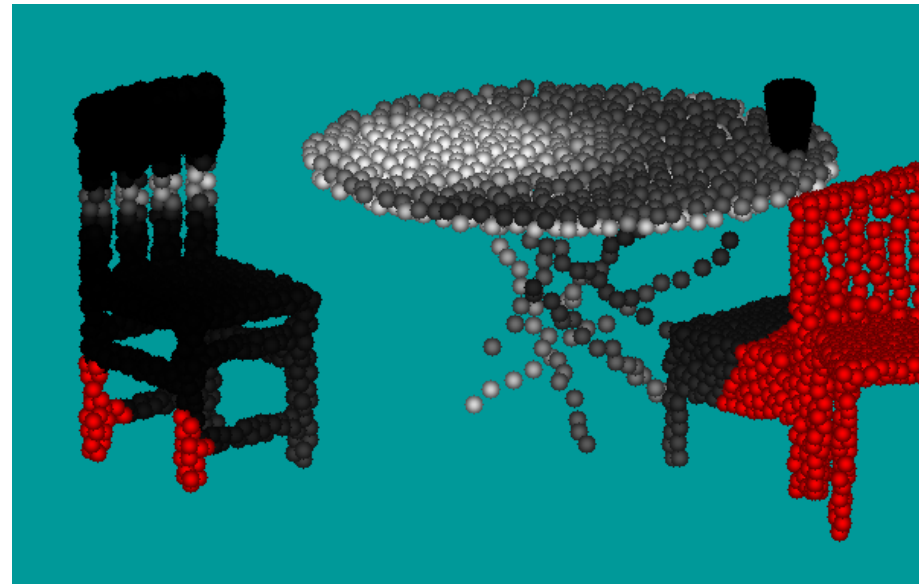
PointNet (vanilla) (Qi et al.)

Limitations of PointNet v1.0

Artifacts in segmentation tasks:



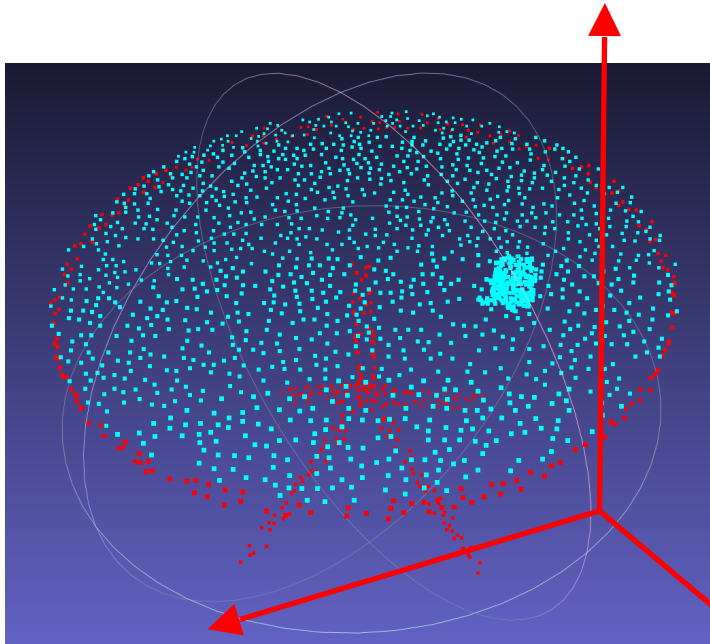
Semantic segmentation in randomly translated table-cup scene.



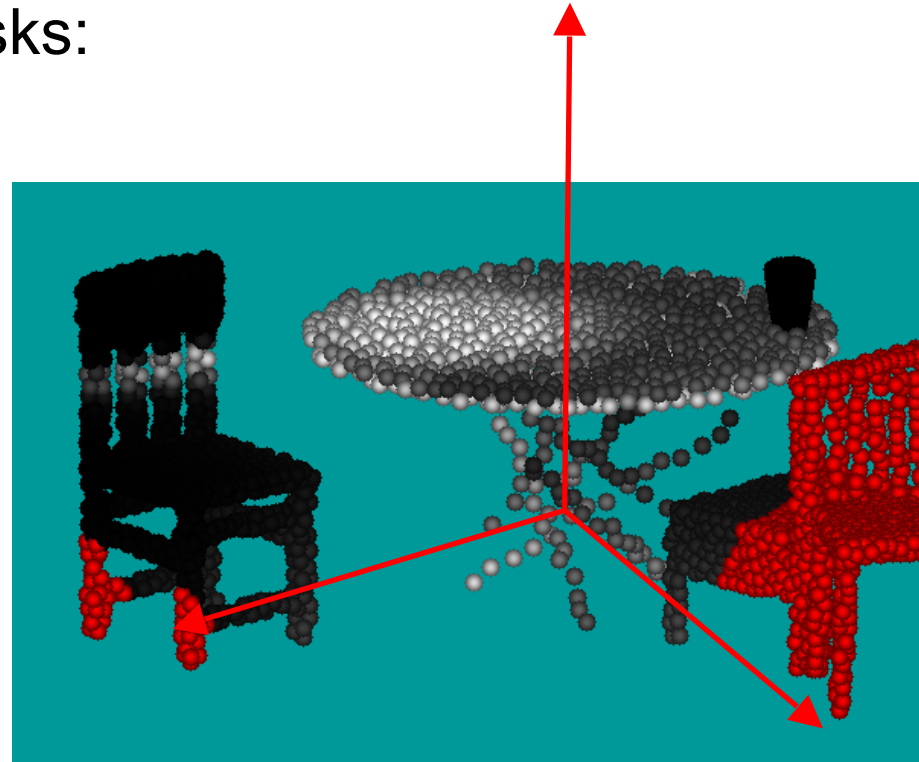
Instance segmentation in table-chair-cup scene

Limitations of PointNet v1.0

Artifacts in segmentation tasks:



Semantic segmentation in randomly translated table-cup scene.



Instance segmentation in table-chair-cup scene

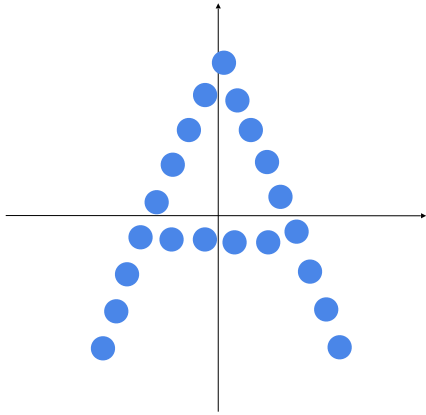
- Global feature depends on absolute XYZ!
- Hard to generalize to unseen point configurations

Question

- How to learn local context feature for points?
- Use PointNet in local regions, aggregate local region features by PointNet again..
-
- Hierarchical feature learning!

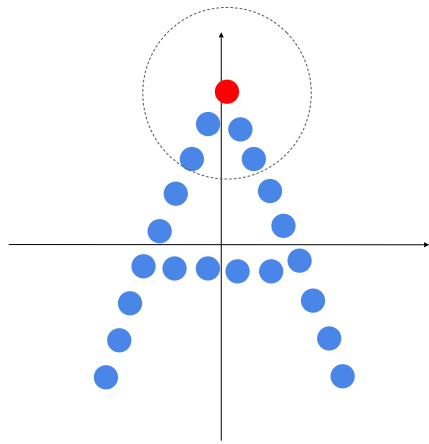
Multi-Scale PointNet for Hierarchical Feature Learning

PointNet v2.0: Multi-Scale PointNet

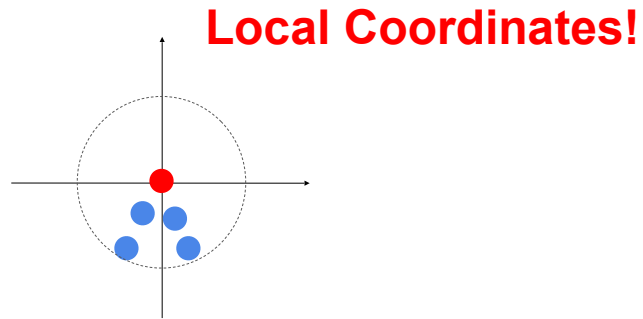


N points in (x,y)

PointNet v2.0: Multi-Scale PointNet

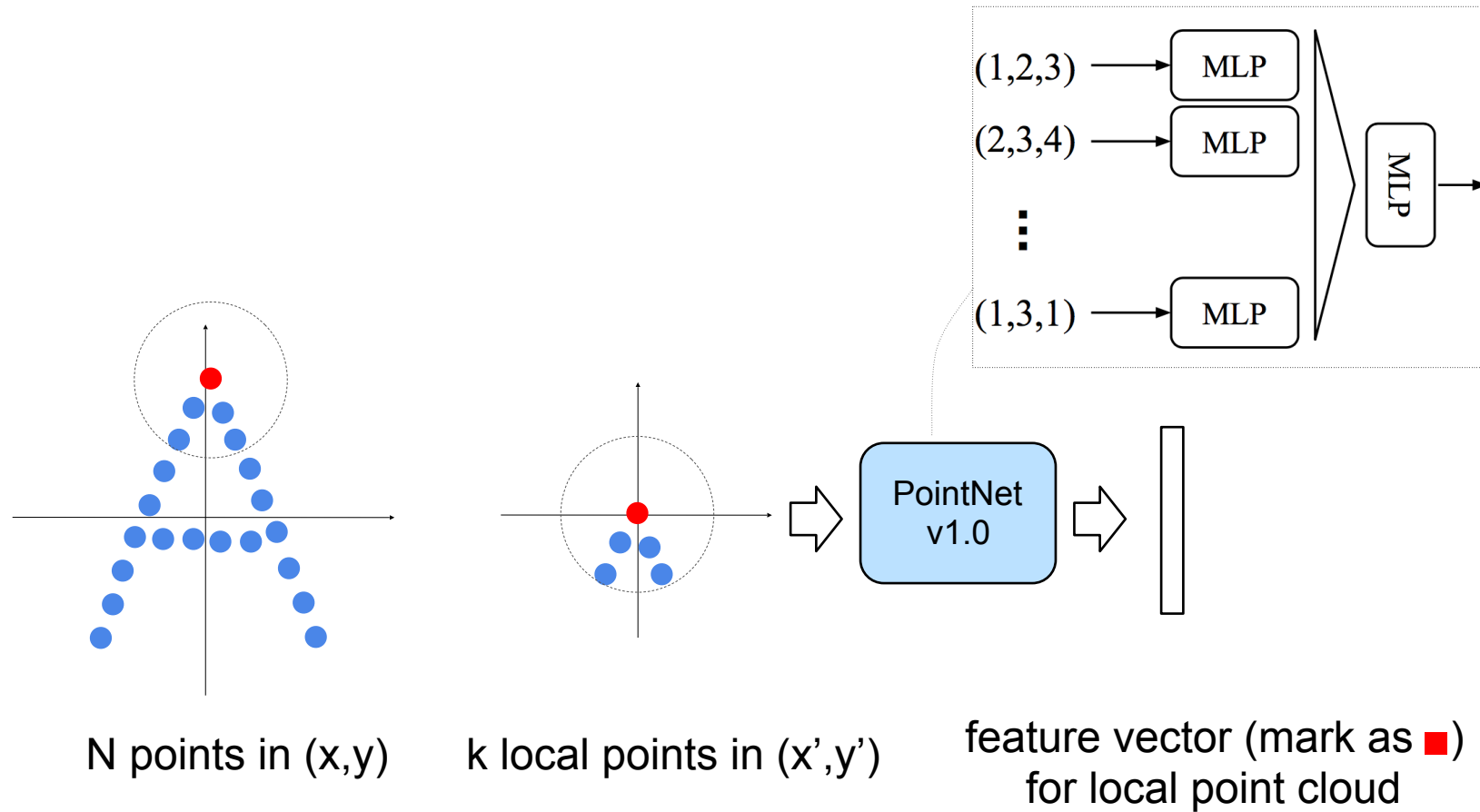


N points in (x,y)



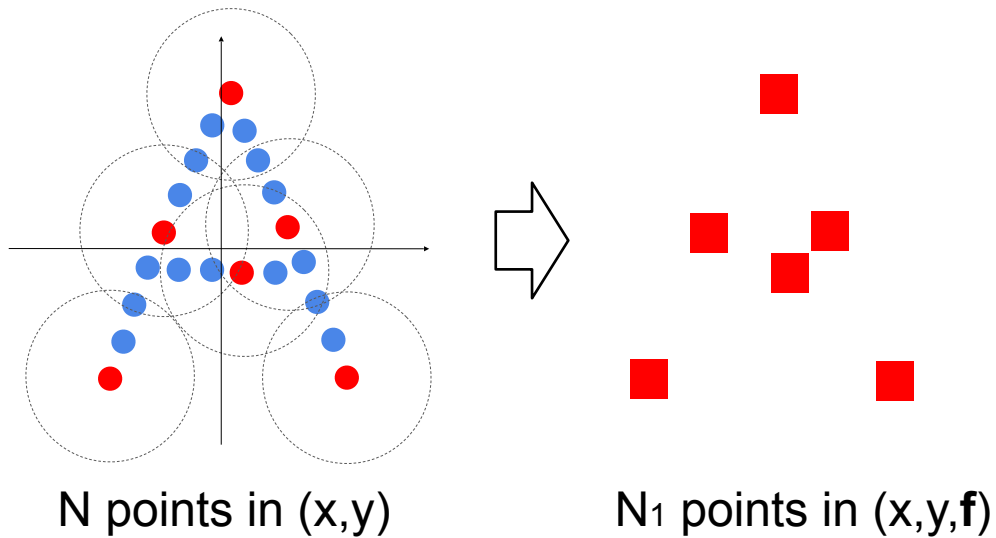
k local points in (x',y')

PointNet v2.0: Multi-Scale PointNet

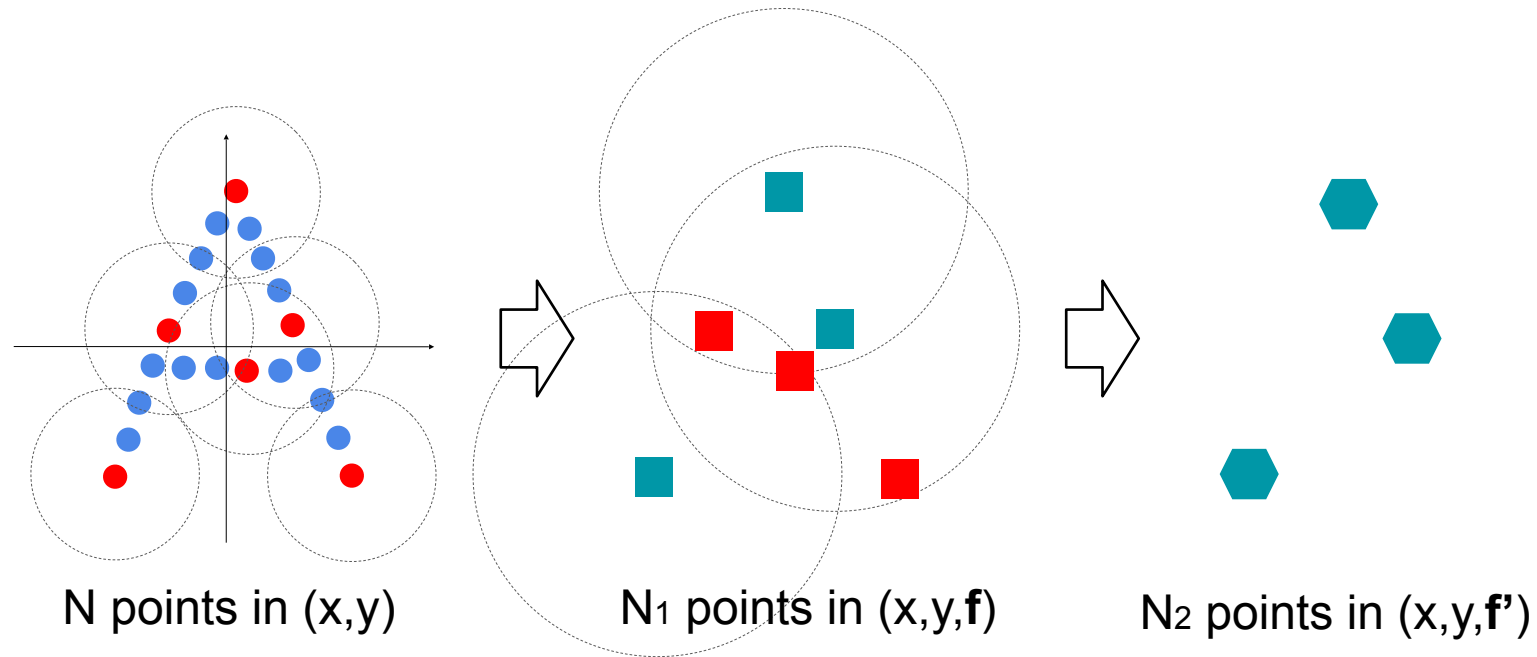


PointNet v2.0: Multi-Scale PointNet

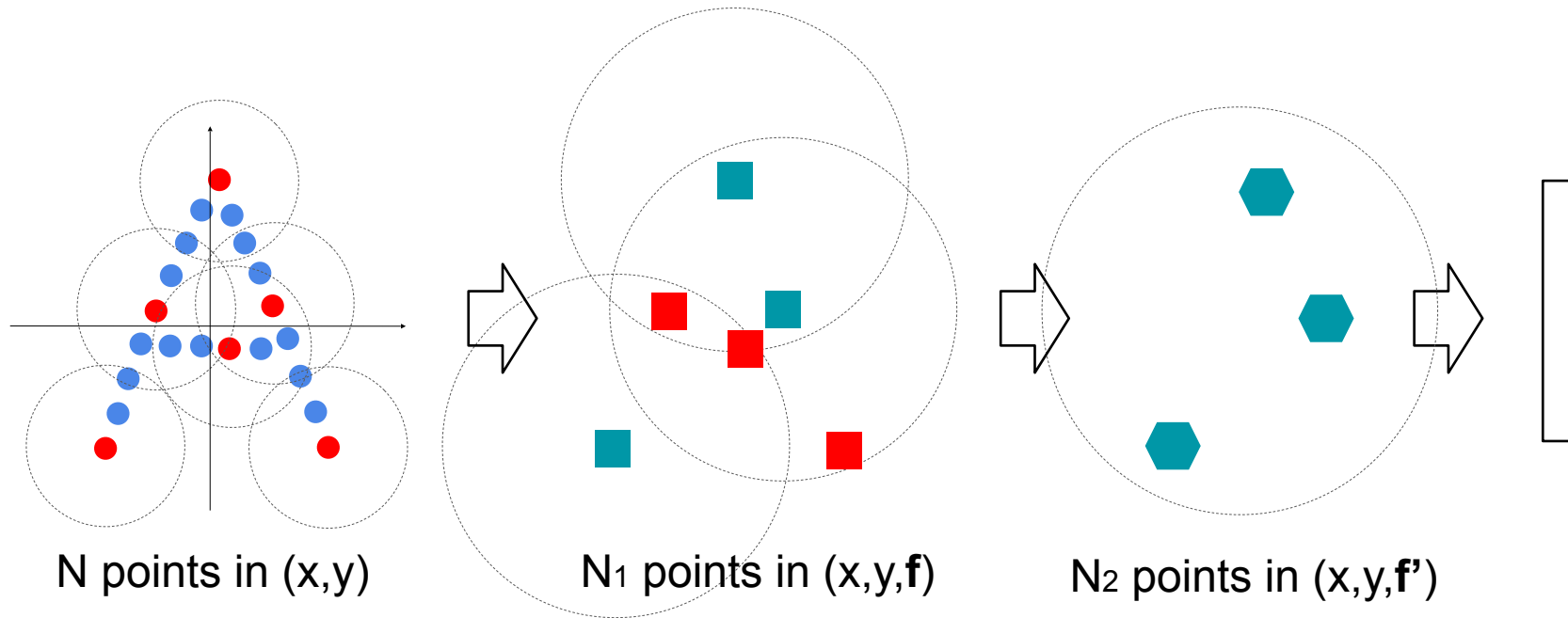
PointNet Module/Layer: Farthest Point Sampling + Grouping + PointNet v1.0



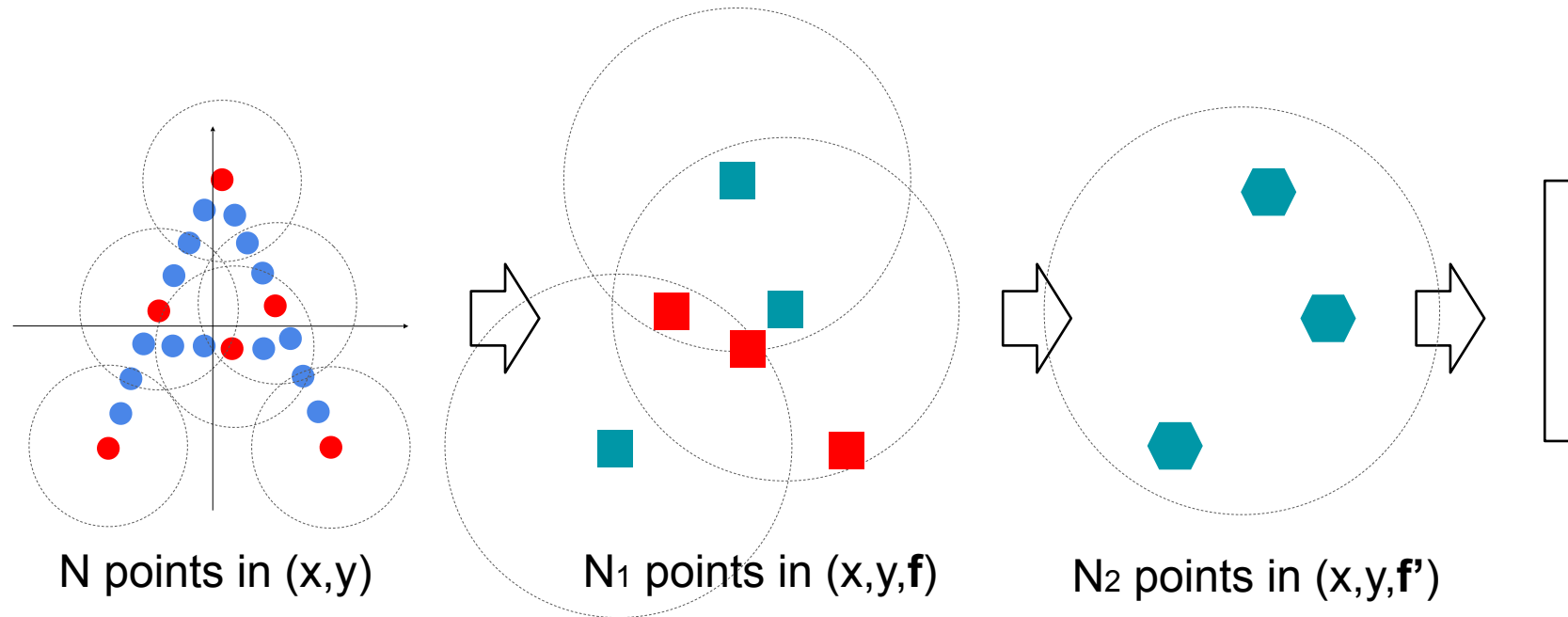
PointNet v2.0: Multi-Scale PointNet



PointNet v2.0: Multi-Scale PointNet



PointNet v2.0: Multi-Scale PointNet

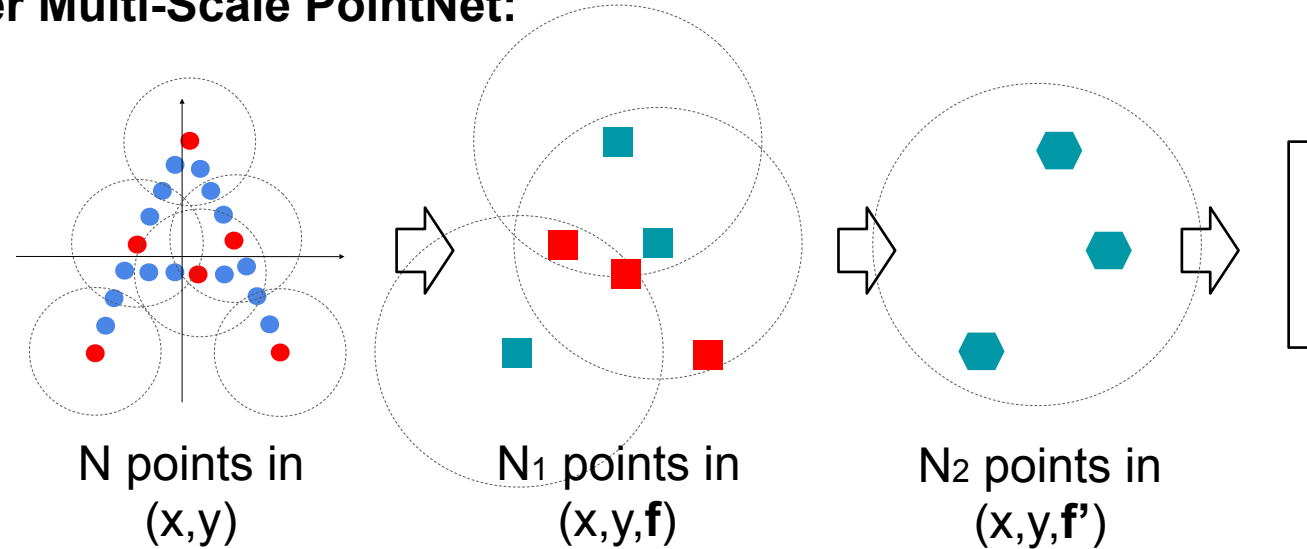


1. Larger receptive field in higher layers ✓
2. Less points in higher layers (more scalable) ✓
3. Weight sharing ✓
4. Translation invariance (local coordinates in local regions) ✓

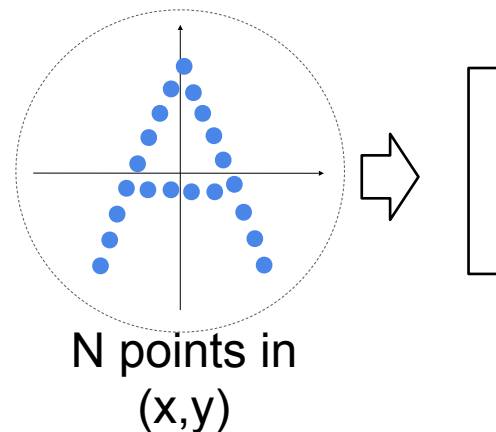
Discussions on Multi-Scale PointNet

Multi-Scale PointNet v.s. PointNet v1.0

Three-layer Multi-Scale PointNet:

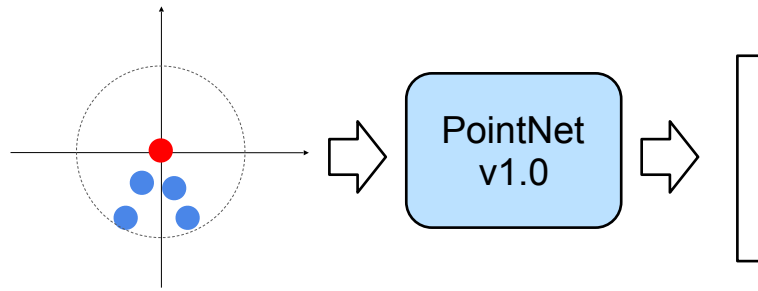


One-layer Multi-Scale PointNet \Leftrightarrow PointNet v1.0



PointNet Layer v.s. Convolution Layer

PointNet Layer



Input:

Point set

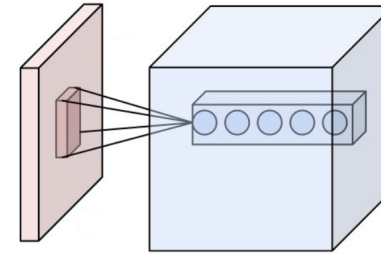
Operation:

MLP + max pooling

Neighbor
-hood:

Distance query

Convolution Layer



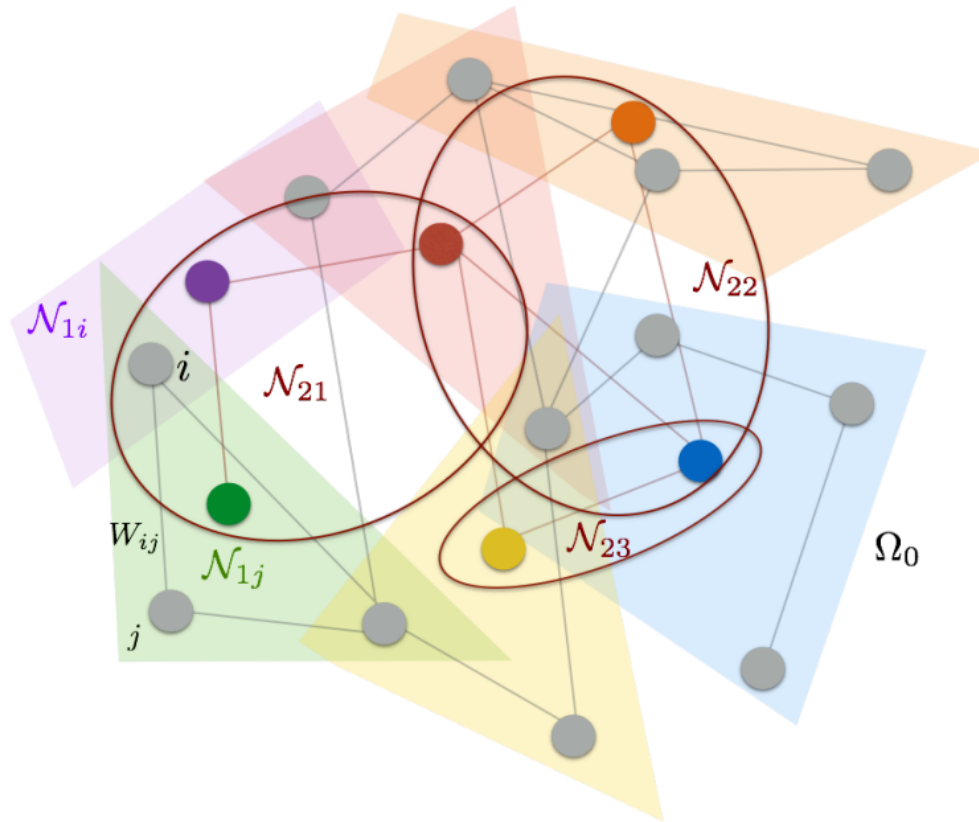
Dense array

Multiply and add

Array index

Multi-Scale PointNet v.s. Graph CNN

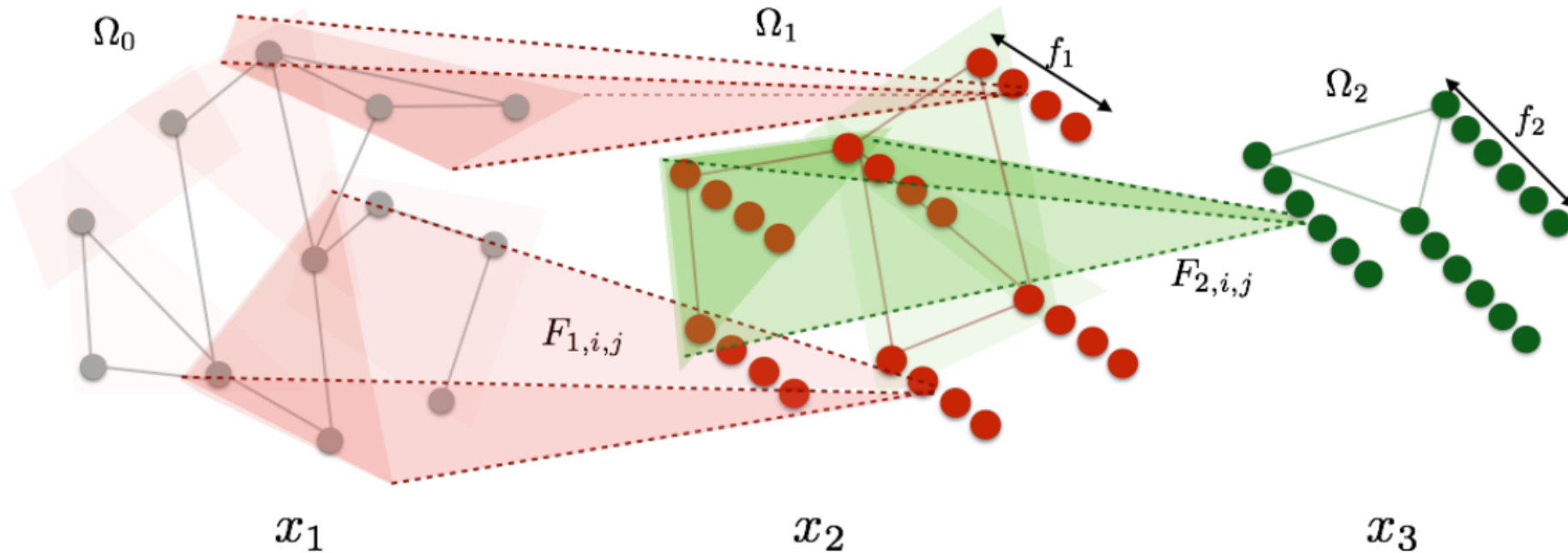
- Unexpectedly strong relation with Graph CNN:



Joan Bruna et al. Spectral Networks and Deep Locally Connected Networks on Graphs. ICLR 2014

Multi-Scale PointNet v.s. Graph CNN

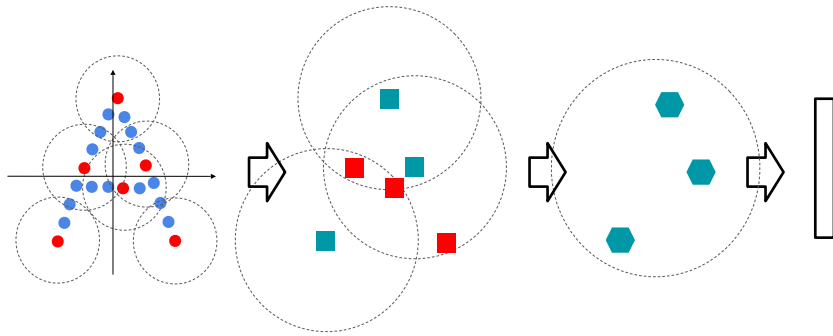
- Local feature extraction, graph coarsening, repeat..



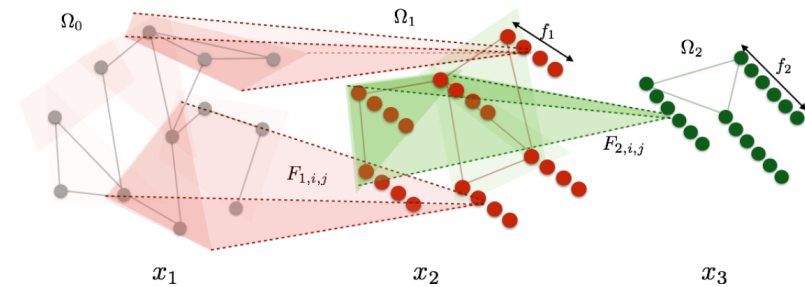
Joan Bruna et al. Spectral Networks and Deep Locally Connected Networks on Graphs. ICLR 2014

Multi-Scale PointNet v.s. Graph CNN

- In Graph CNN's perspective:
- Multi-Scale PointNet defines
 1. Graph connectivity through Euclidean distance
 2. Graph coarsening by farthest point sampling
 3. Local feature extraction with PointNet (v1.0)



Multi-scale PointNet

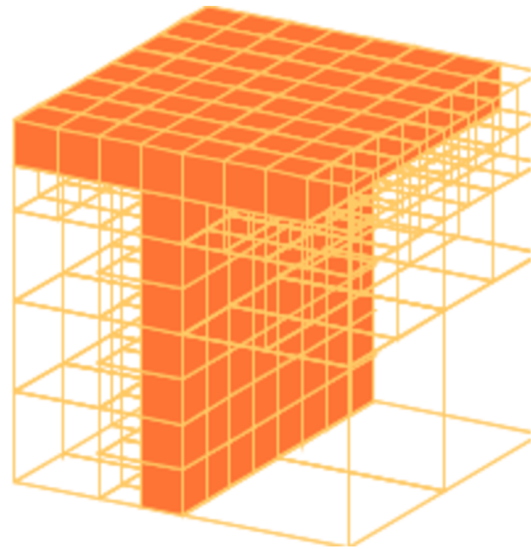


Graph CNN

Relations to OctNet (Octree based 3D CNN)

OctNet in Graph CNN's perspective:

1. Both connectivity and graph coarsening are defined by the Octree.
2. Local feature extraction by convolution layer.



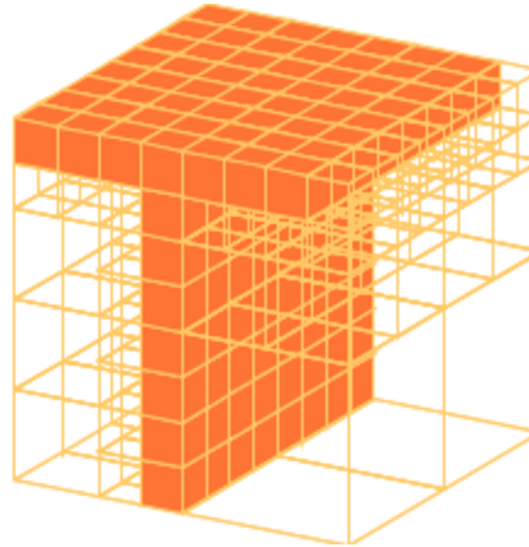
OctNet: Learning Deep 3D Representations at High Resolutions
Gernot Riegler, Ali Osman Ulusoy and Andreas Geiger

Relations to OctNet (Octree based 3D CNN)

OctNet in Graph CNN's perspective:

In Multi-Scale PointNet

1. Both connectivity and graph coarsening are defined by the Octree. By ground distance
2. Local feature extraction by convolution layer. By PointNet (v1.0)



OctNet: Learning Deep 3D Representations at High Resolutions
Gernot Riegler, Ali Osman Ulusoy and Andreas Geiger