

# Light and Color



Painting by Cheryl Yaney

## Topics

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### Physics of light

- Electromagnetic spectrum
- Fundamental operations: add, filter, measure

### Perception of color

- Trichromatic theory
- Luminance
- Color spaces

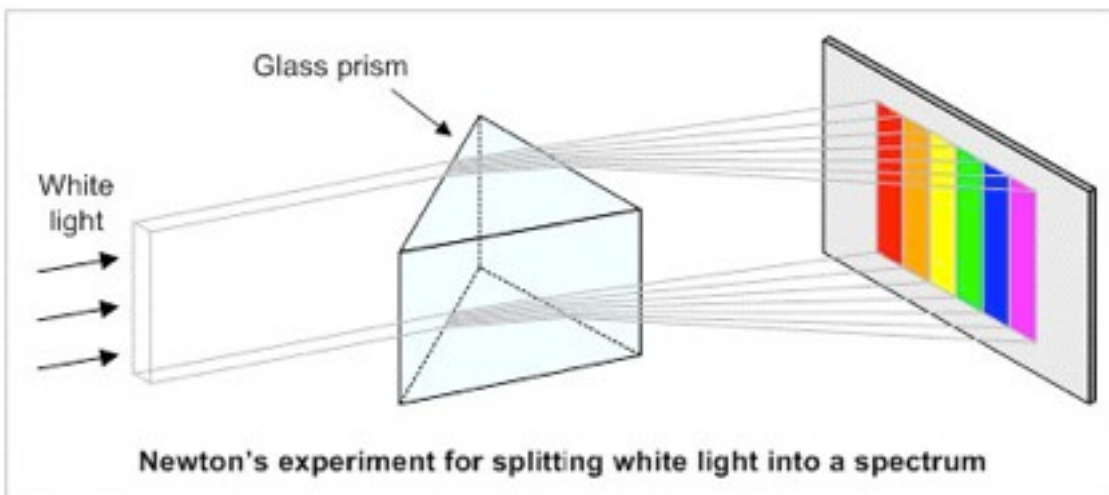
### Art

- Color terms
- Color wheels and intuitive color spaces

# Physics of Light

## Light

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**Image from Clive Maxfield**

# Electromagnetic Spectrum

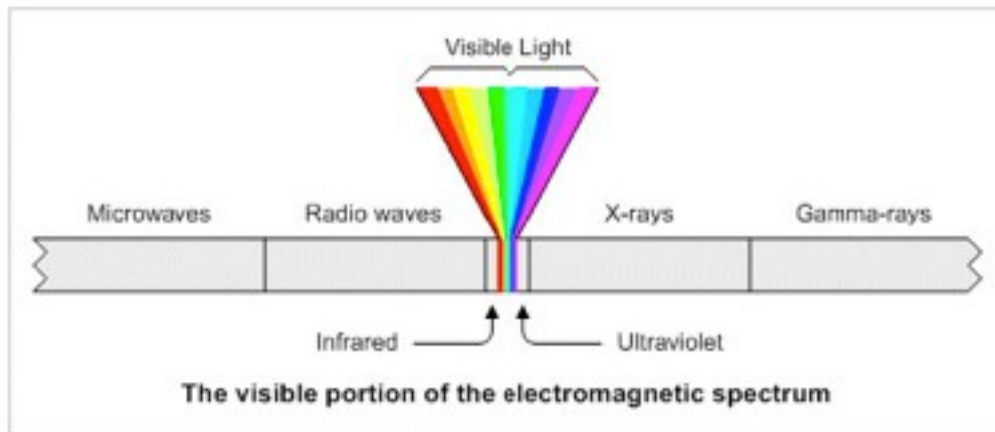
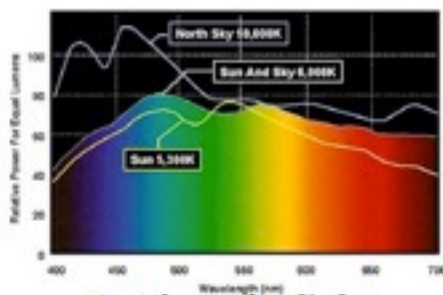
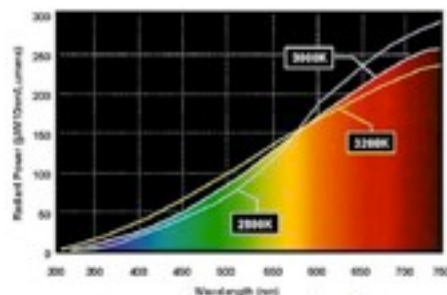


Image from Clive Maxfield

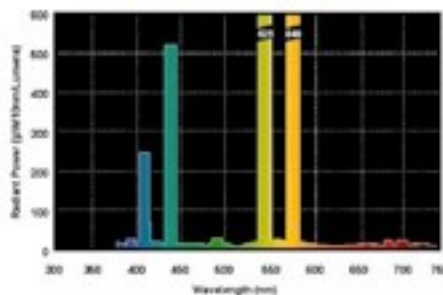
# Spectral Power Distribution of Lights



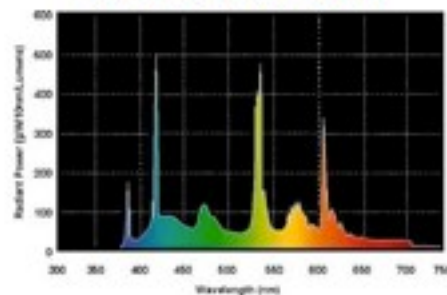
Outdoor daylight



Incandescent bulb

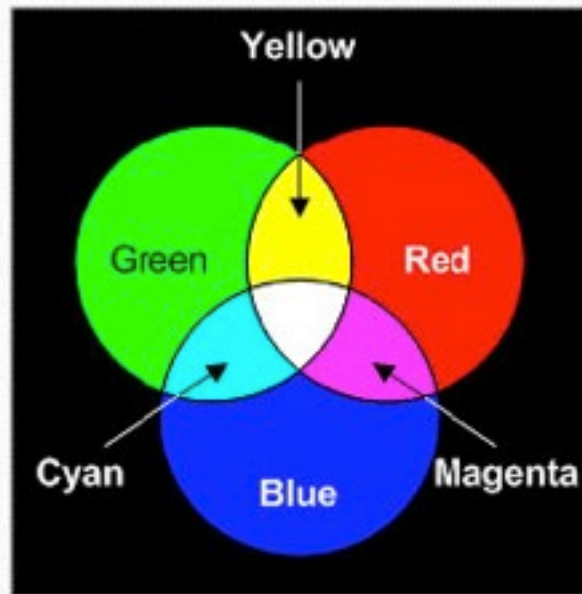


Mercury lamp



SP65 triphosphor fluorescent

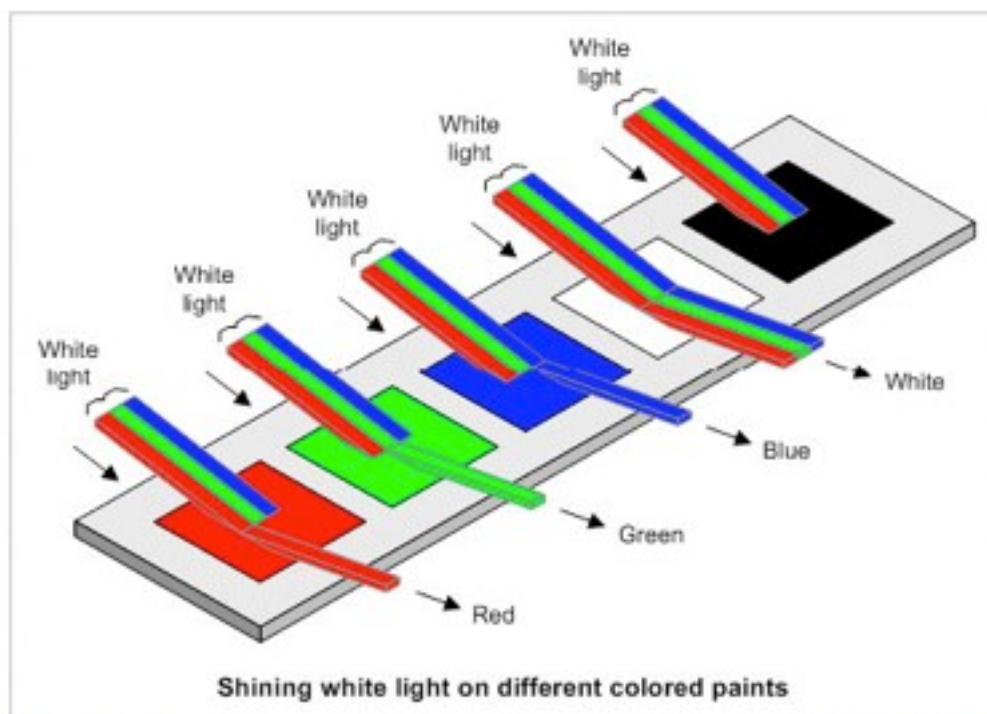
# Adding Light Energy



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# Reflecting Light



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# Light Operations

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**Add spectra**  $L(\lambda) = S_1(\lambda) + S_2(\lambda)$

$$R = R_1 + R_2$$

$$G = G_1 + G_2$$

$$B = B_1 + B_2$$

**Multiply spectra**  $L(\lambda) = T(\lambda)S(\lambda)$

$$R = R_1 R_2$$

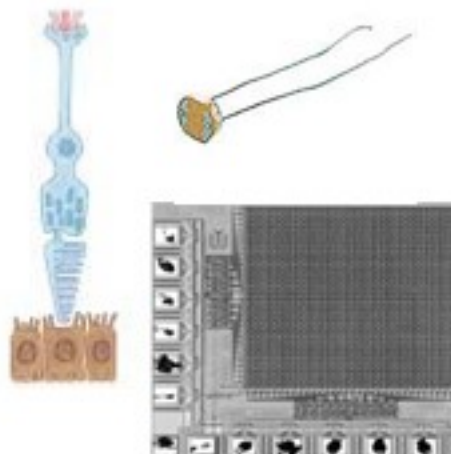
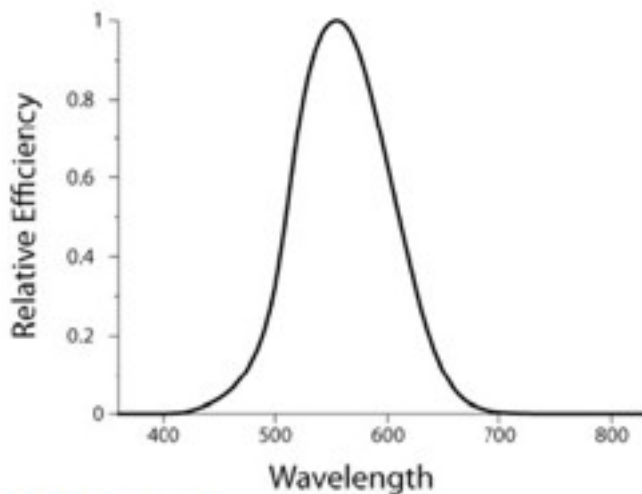
$$G = G_1 G_2$$

$$B = B_1 B_2$$

# Measuring Light

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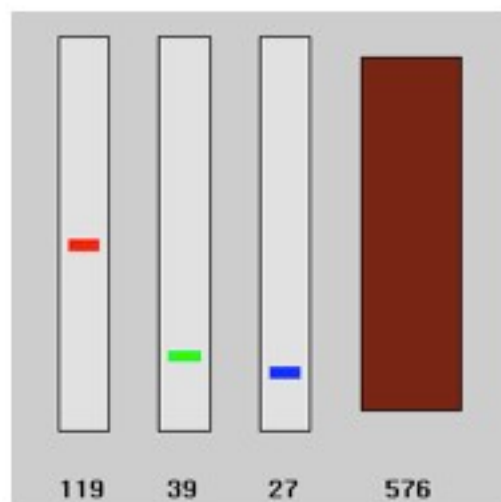
**Photon detector**  $R = \int R(\lambda)L(\lambda) d\lambda$



# Trichromatic Theory

## RGB Color

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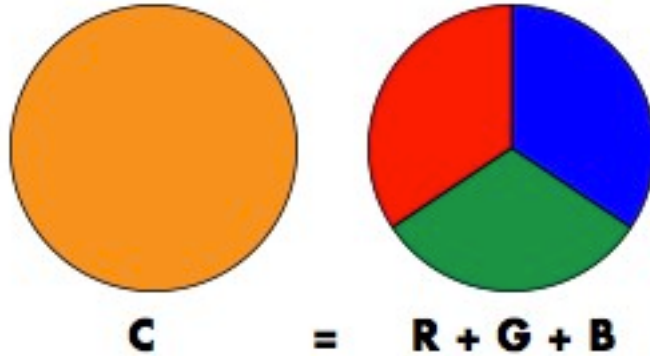
**Result: colors can be matched with three colors**

# Color Matching Experiment

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**Adjust brightness of three primaries**

**Lasers: R = 700 nm, G = 546 nm, B = 435 nm**  
**until it "matches" another color C**



**Result: all colors can be matched with three colors**  
**Therefore: humans have trichromatic color vision**

# Color Matching is Linear

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**Grassman's Laws**

**1. Scaling the color and the primaries by the same factor preserves the match**

$$2C = 2R + 2G + 2B$$

**2. To match a color formed by adding two colors, add the primaries that match each color**

$$C_1 + C_2 = (R_1 + R_2) + (G_1 + G_2) + (B_1 + B_2)$$

# Human Retina: Three Types of Cones

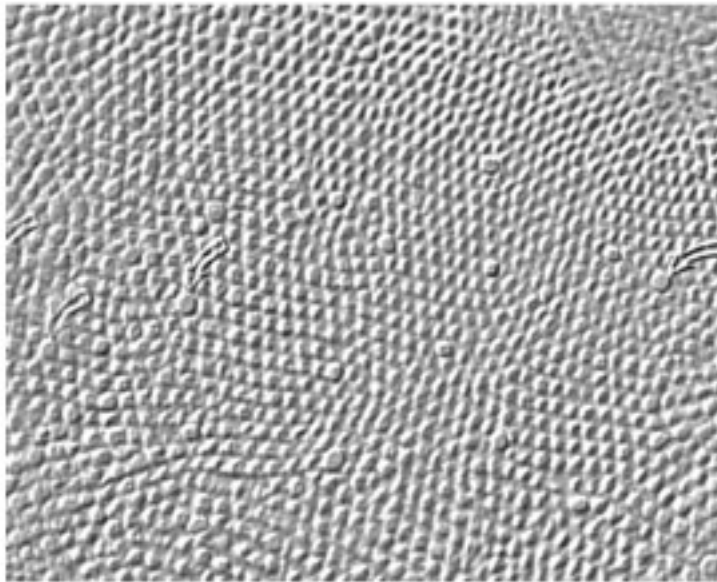


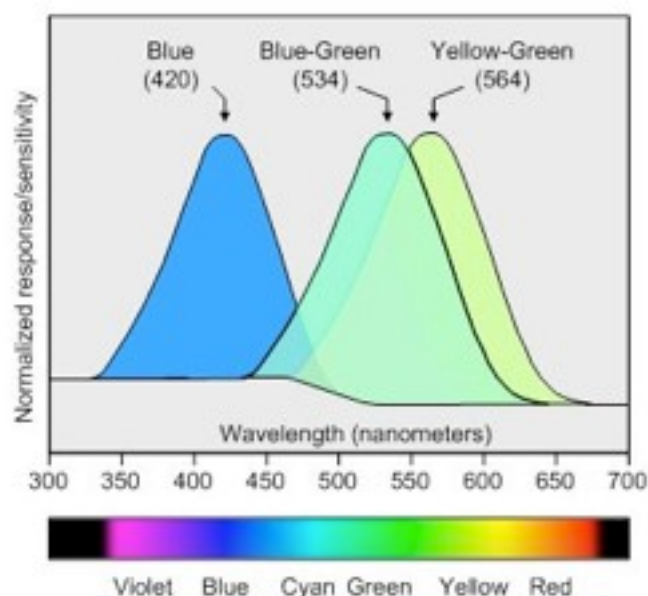
Fig. 13. Tangential section through the human fovea.  
Larger cones (arrows) are blue cones.

From <http://webvision.med.utah.edu/imageswv/fovmoswv.jpeg>

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# Response of Three Cones



Typical humans are trichromats  
(three color cone/pigment types – blue, blue-green, and yellow-green)

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# Cone Response

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## Three cones

**L (long)**  $L = \int L(\lambda)E(\lambda) d\lambda$

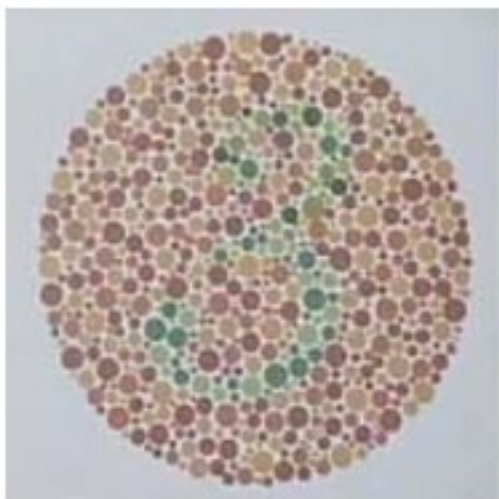
**M (medium)**  $M = \int M(\lambda)E(\lambda) d\lambda$

**S (short)**  $S = \int S(\lambda)E(\lambda) d\lambda$

**Metamerism: Different spectra, same color response**

# Color Blindness: Ishihara Test

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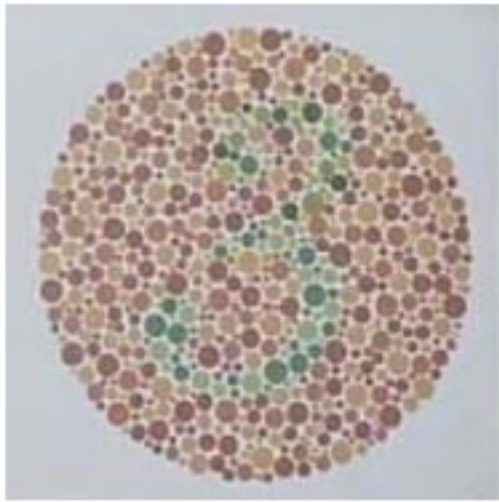


**Normal**

<http://www.toledo-bend.com/colorblind/Ishihara.html>

# Color Blindness: Ishihara Test

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**Normal**



**Deuteranopia**

<http://www.toledo-bend.com/colorblind/Ishihara.html>

# Types of Color Blindness

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**Dichromacy: missing pigment (10% M, 1% F)**

- **Protanopia** – missing L
- **Deuteranopia** – missing M (red-green)
- **Tritanopia** – missing S



**Normal**



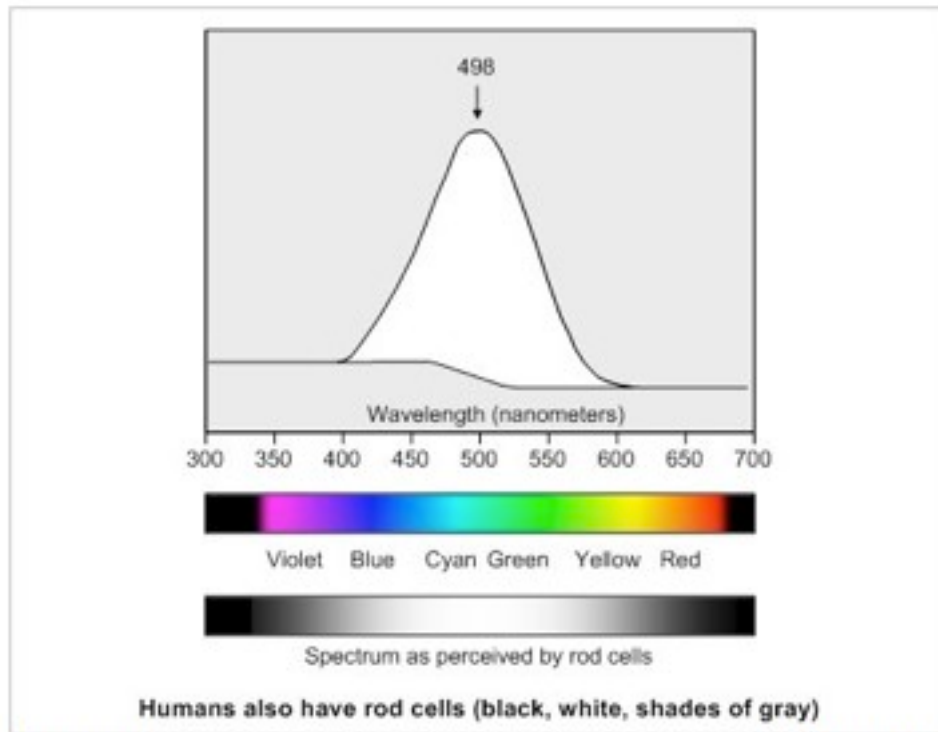
**Deuteranopia**



**Tritanopia**

[www.vischeck.com](http://www.vischeck.com)

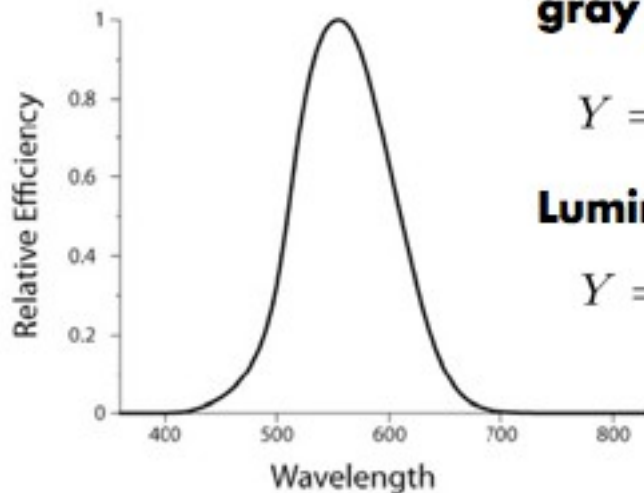
# Rod



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# Luminance



**Compare color to a gray source**

$$Y = \int V(\lambda)E(\lambda) d\lambda$$

**Luminance (B&W TV)**

$$Y = 0.30R + .59G + .11B$$

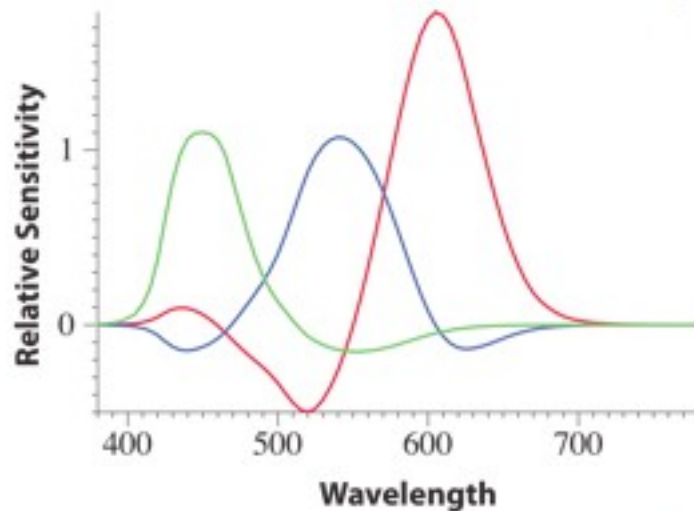
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# Spectral Matching Functions

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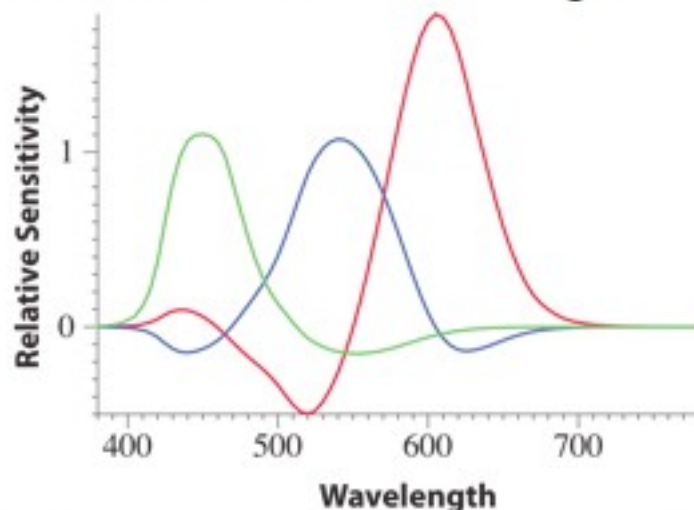
**Match each pure (monochromatic) color in the visible spectrum (rainbow) and record the color coordinates as a function of wavelength**



# Spectral Matching Functions

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**Gotcha! Sometime you have to add R to the color and then match it to a combination of B and G. This situation means that R is negative**



# CIE XYZ Space



## From RGB to XYZ

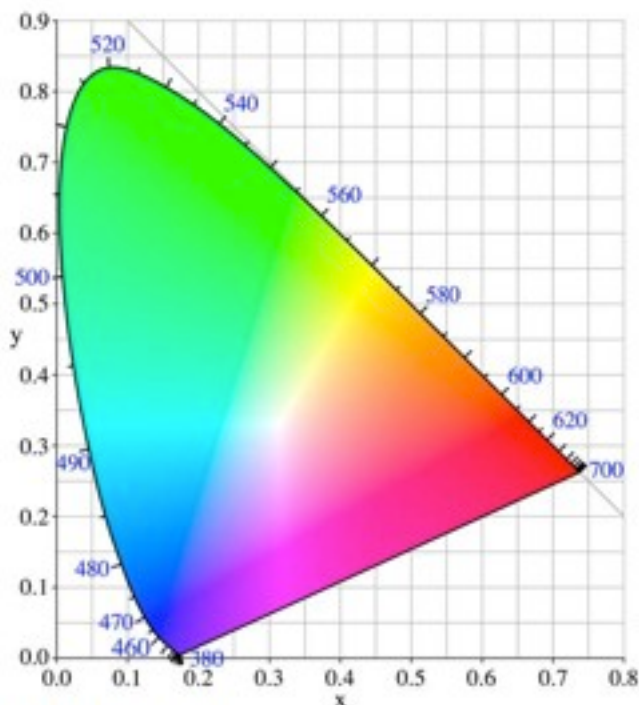
- Y is luminance
- Force X, Y and Z to be positive

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 2.77 & 1.75 & 1.13 \\ 1.00 & 4.59 & 0.06 \\ 0.00 & 0.57 & 5.59 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

Colors of the rainbow are on the outer horseshoe curve

All perceivable colors are inside the curve

# CIE XYZ Chromaticity Coordinates

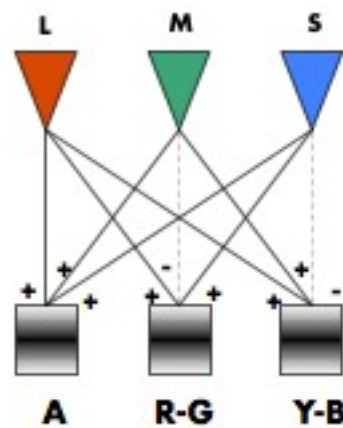


$$\begin{aligned} x &= X/(X + Y + Z) \\ y &= Y/(X + Y + Z) \\ z &= Z/(X + Y + Z) \end{aligned}$$

# Perceptual Models of Color

## Early Visual Processing

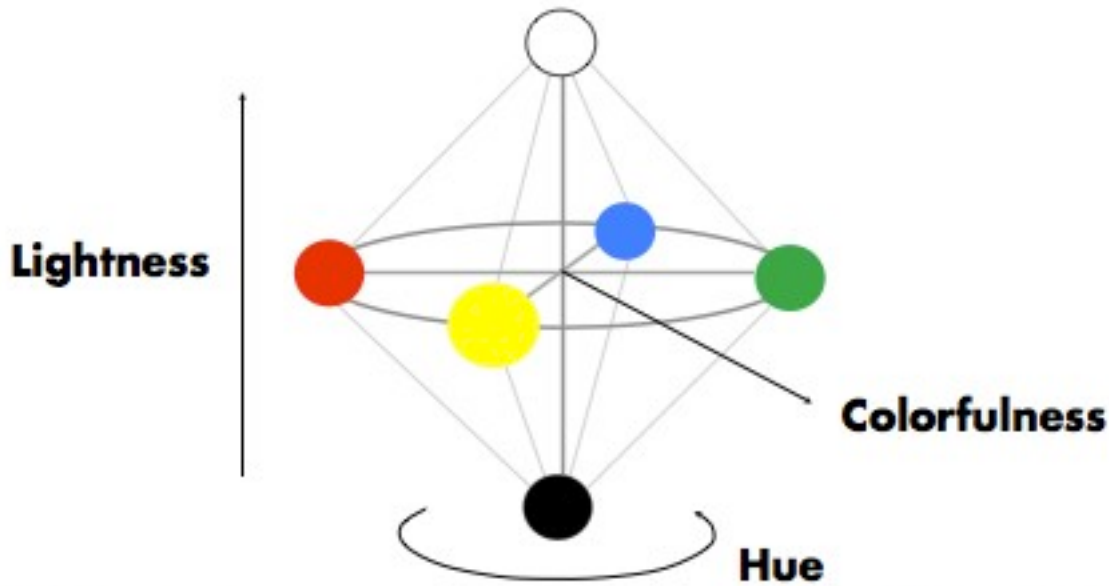
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$$A = R + G + B$$
$$(Y - B) = R + G - B$$
$$(R - G) = R - G$$

# Perceptual Organization

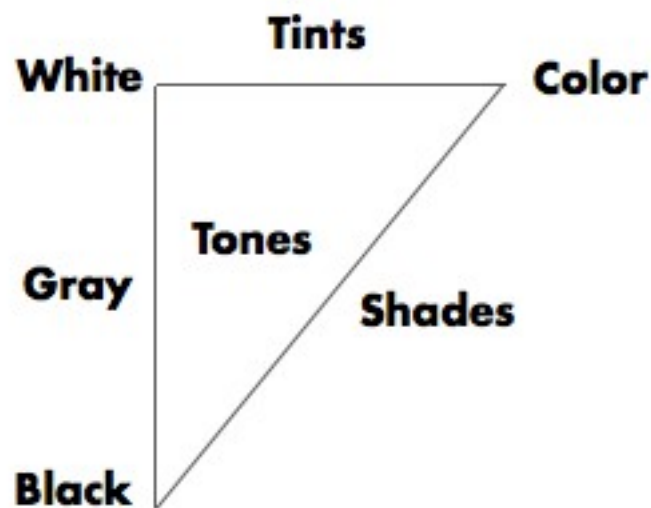
BW, RG, YB



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# Intuitive Color Space

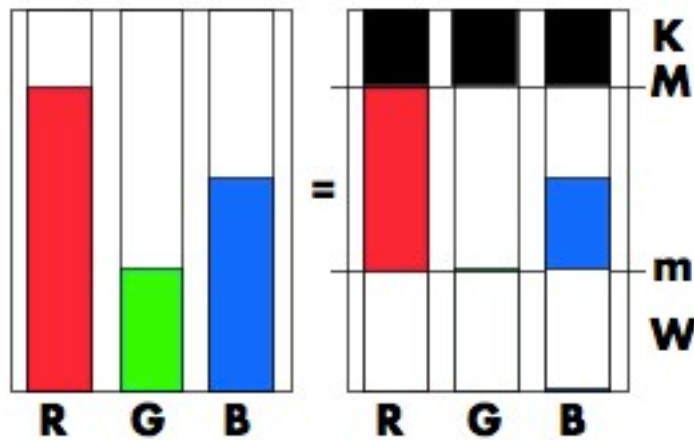


## MetaDesign Color Picker

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# HSV



$$M = \max(R, G, B)$$

$$m = \min(R, G, B)$$

$$r = (M - R) / (M - m)$$

$$g = (M - G) / (M - m)$$

$$b = (M - B) / (M - m)$$

$$V = M$$

$$S = (M - m) / M$$

$$\text{if}(M == R)$$

$$H = (6 + b - g) / 6$$

....

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## Things to Remember

### Physics of color

- Addition, transmission/reflection, measurement

### Perception of color

- Three colors will match another color
- Trichromatic because we have 3 cones
- Explains metamerism, color blindness
- Color matching is linear
- Perceptual organization in terms of BW, YB, RG
- Hue-Saturation-Value

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