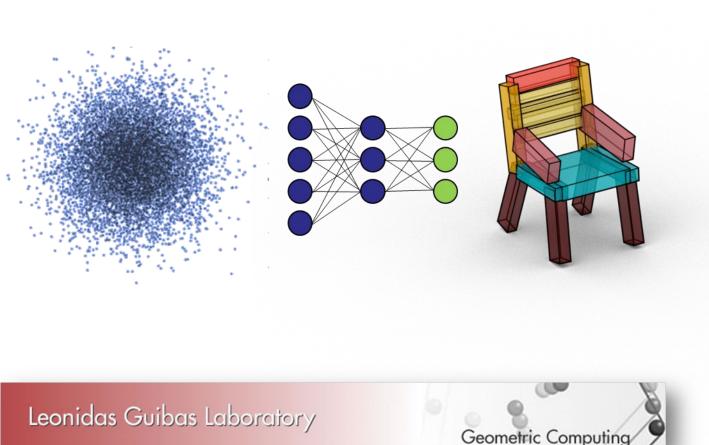
## CS348n: Neural Representations and Generative Models for 3D Geometry



Leonidas Guibas Computer Science Department Stanford University



02\_16\_DEFORM 1

#### **Class Logistics**

- Project proposals due today
- Next lecture (Wed, Feb 23) on NeRFs will be by Ben Mildenhall and Pratul P. Srinivasan, two of the authors of the original NeRF paper. It will still be virtual on Zoom.
- Because of the special guests, the student presentations for Feb 23 will be moved to Feb 28 (two sets of student presentation then)
- From Feb 28 the class will be physical, in Clark S361

## Last Time: Conditional Shape Generation Based on Image Data

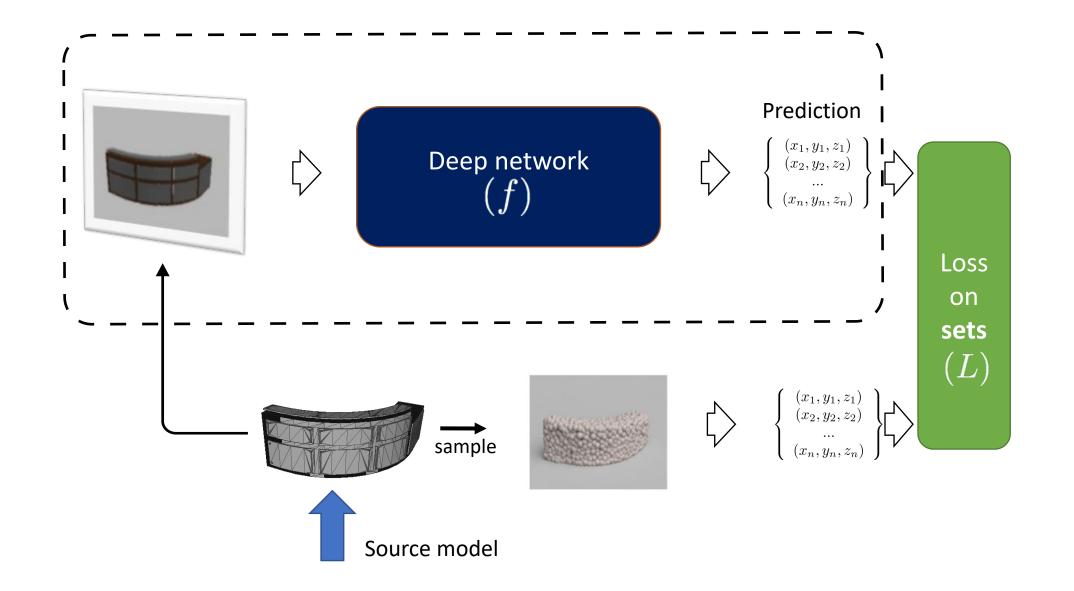
#### Point Cloud Synthesis from a Single Image



Input

#### Reconstructed 3D point cloud

#### **End-to-End Learning**



#### **Point Cloud Distance Metrics**

#### Worst case: Hausdorff distance (HD)

 $d_{\text{HD}}(S_1, S_2) = \max\{\max_{x_i \in S_1} \min_{y_j \in S_2} \|x_i - y_j\|, \max_{y_j \in S_2} \min_{x_i \in S_1} \|x_i - y_j\|\}$ 

Average case: Chamfer distance (CD)

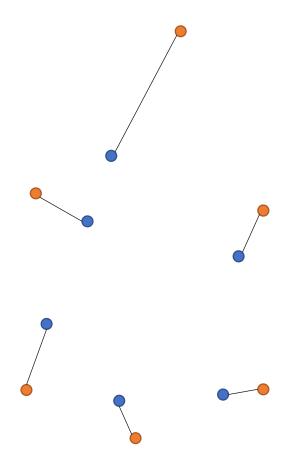
$$d_{CD}(S_1, S_2) = \frac{1}{n} \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2^2 + \frac{1}{m} \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2^2$$

Optimal case: Earth Mover's distance (EMD)

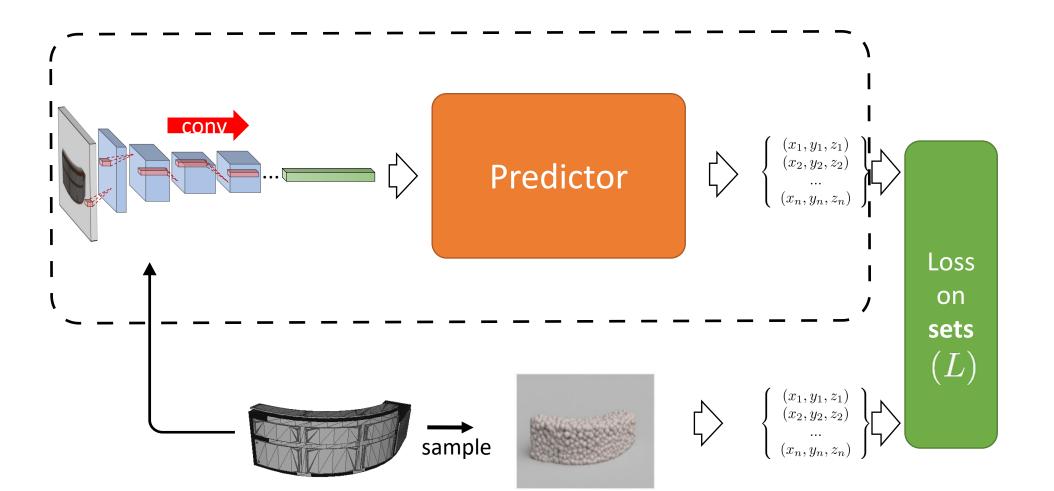
$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \to S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2$$

where  $\phi: S_1 \to S_2$  is a bijection.

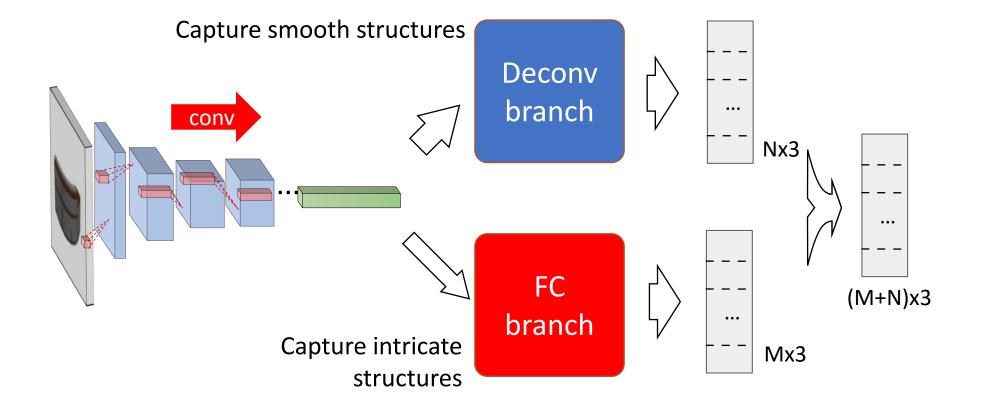
Solves the optimal transportation (bipartite matching) problem!



#### End-to-End Learning Architecture



#### **Two-Branch Architecture**



Set union by array concatenation

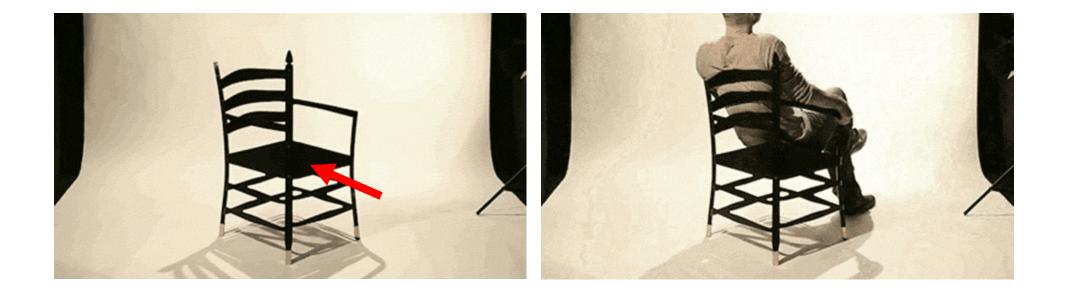
#### The Two Branches

blue: deconv branch - large, consistent, smooth structures
red: fully-connected branch - more intricate structures



#### Ambiguity in Object Views

• A fundamental issue: inherent ambiguity in prediction



 By loss minimization, the network tends to predict a "mean shape" that averages out uncertainty

### Canonical "Containers" for Object Categories



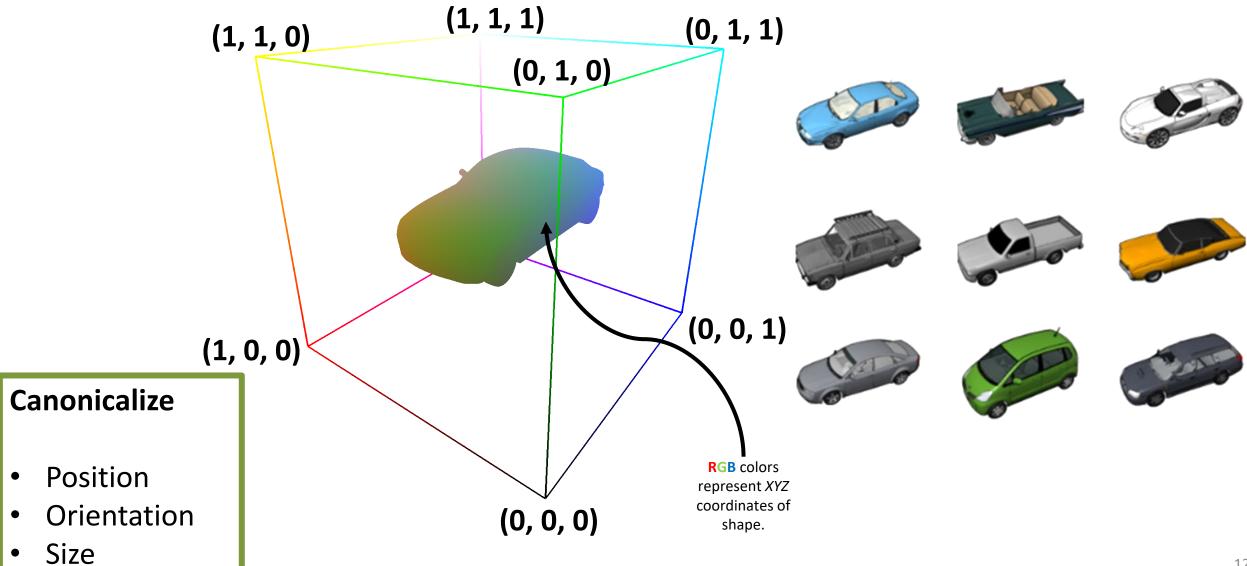


He Wang, Srinath Sridhar, Jingwei Huang, Julien Valentin, Shuran Song, Leonidas J. Guibas. *Normalized Object Coordinate Space for Category-Level 6D Object Pose and Size Estimation*. CVPR 2019.

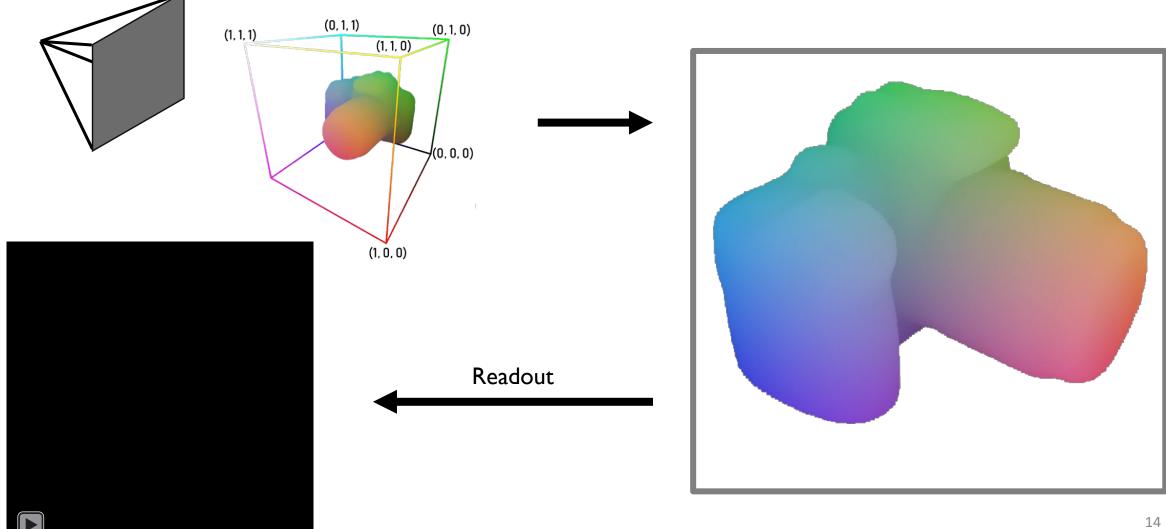




### Normalized Object Coordinate Spaces (NOCS)



### **NOCS Lifting Map**

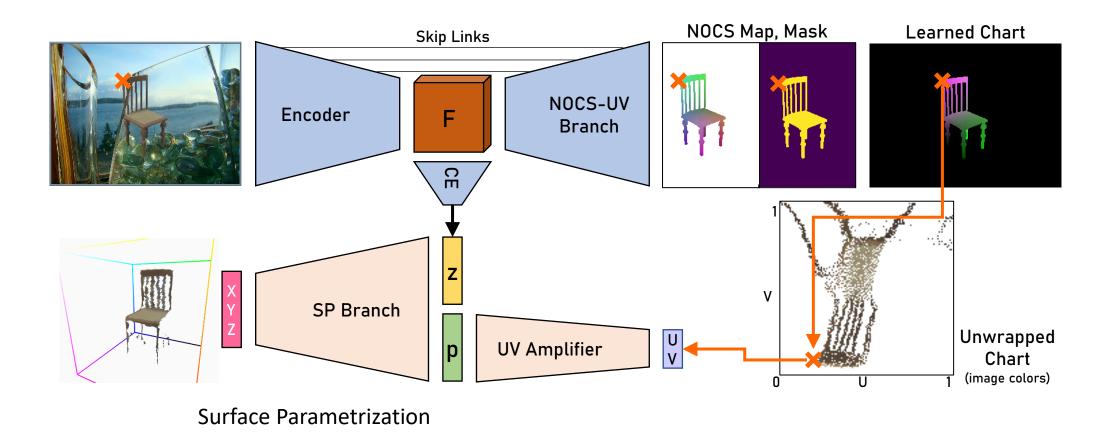


#### Multi-View NOCS Aggregation



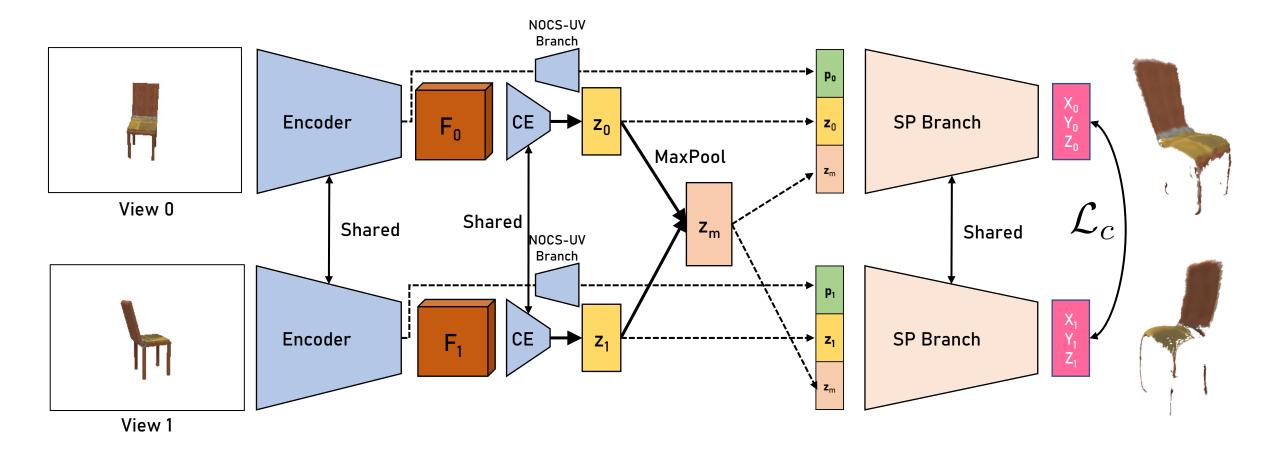
- Set union of
- No surface

## Pix2Surf: Single-View Single-Chart



Lei, J., Sridhar, S., Guerrero, P., Sung, M., Mitra, N. and Guibas, L.J. Pix2surf: Learning parametric 3D surface models of objects from images. ECCV 2020.

### Pix2Surf: Multi-View Atlas



Multi-View consistency loss  $L_c = \frac{1}{|P|} \sum_{(i,j)\in P} ||x_i - x_j||_2$ 

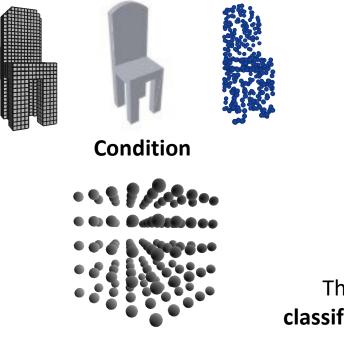
#### Pix2Surf: Single-View Single-Chart



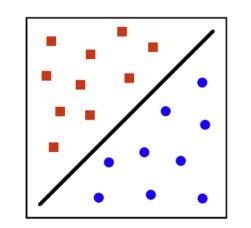
Lei, J., Sridhar, S., Guerrero, P., Sung, M., Mitra, N. and Guibas, L.J. Pix2surf: Learning parametric 3D surface models of objects from images. ECCV 2020.

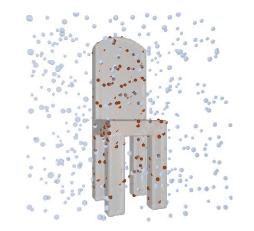
#### **Occupancy Networks**

- Key Idea:
  - Do not represent the 3D shape explicitly
  - Consider the surface implicitly, as **the decision boundary of a non-linear classifier**, parametrized by the neural network:



**3D Locations** 

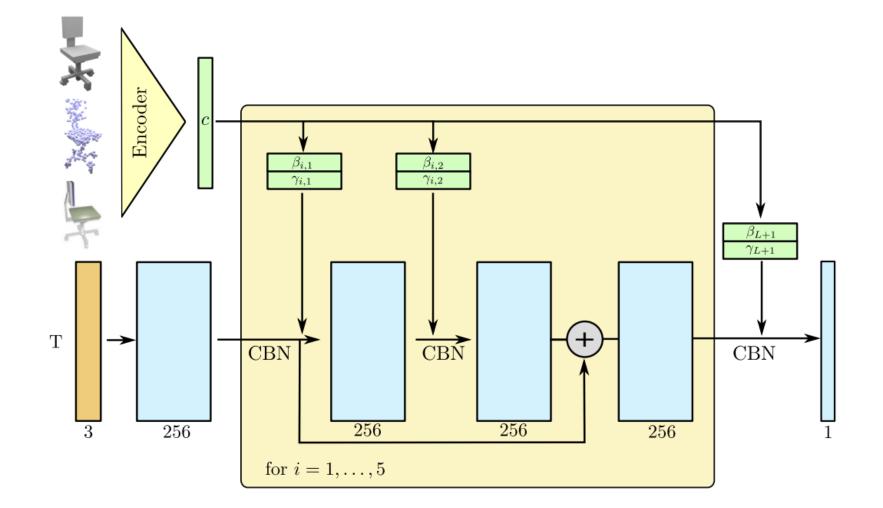




**Occupancy Probability** 

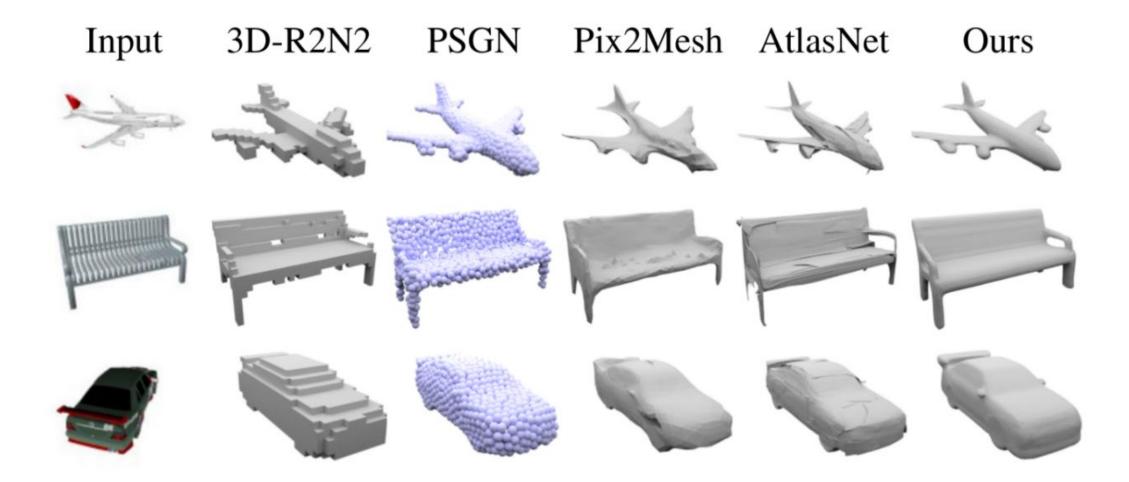
The decision boundary of the classifier models the occupancy field.

#### **Network Architecture**



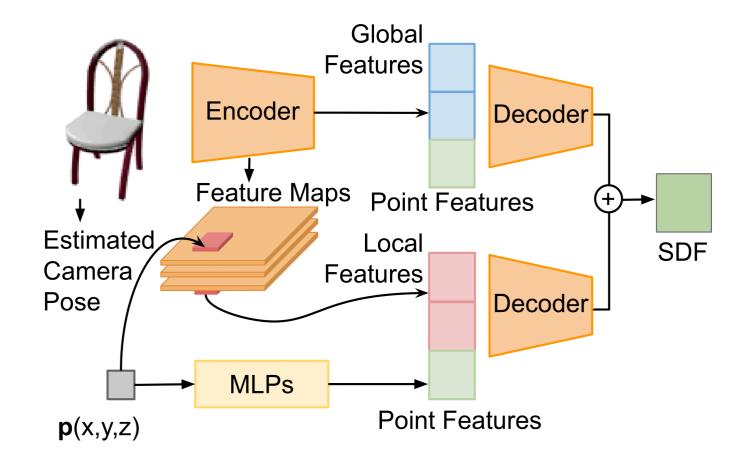
How can we train Occupancy Networks?

#### How well does it work?



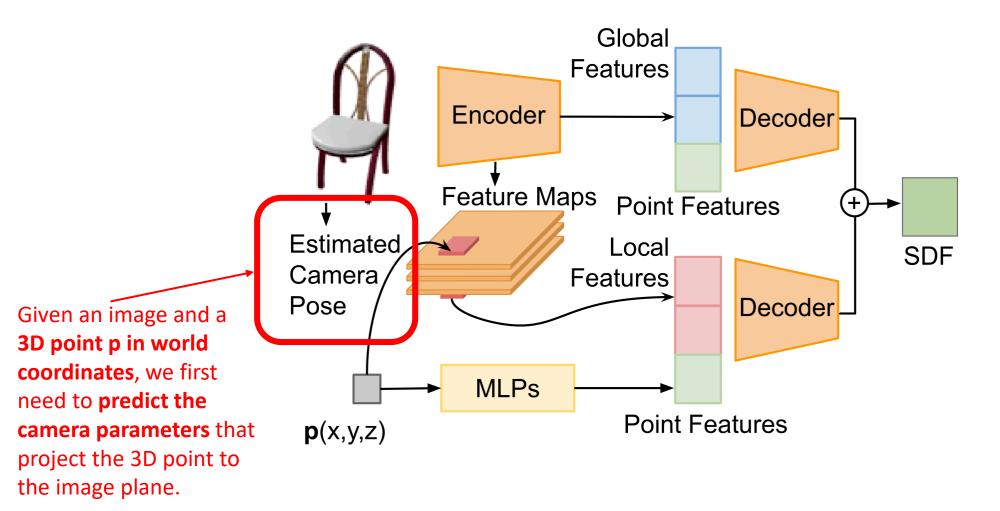
#### **DISN – Model Overview**

**Key Idea:** Use both global and local features for capturing both the overall shape and the fine-grained details.

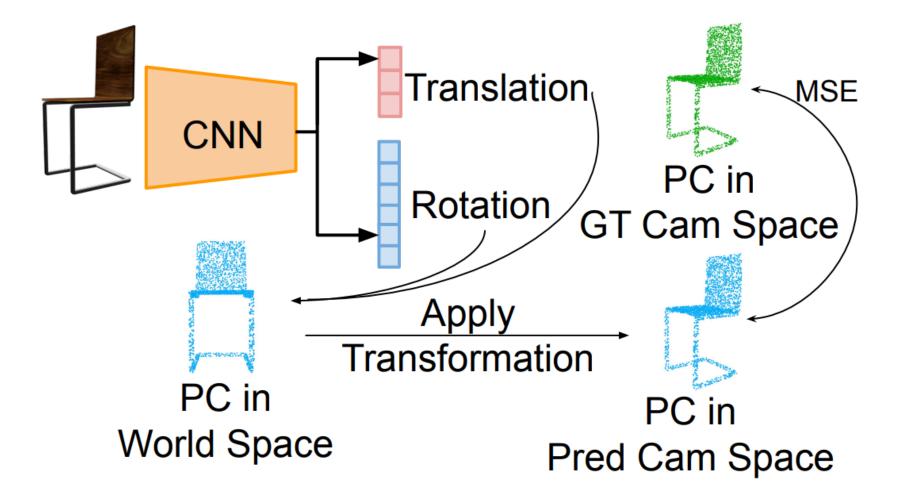


#### **DISN – Model Overview**

**Key Idea:** Use both global and local features for capturing both the overall shape and the fine-grained details.

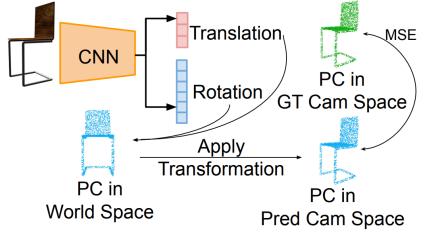


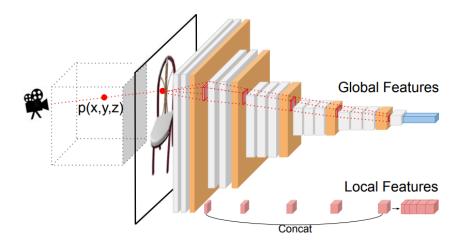
#### **DISN – Camera Pose Estimation**



#### **DISN – Model Overview**

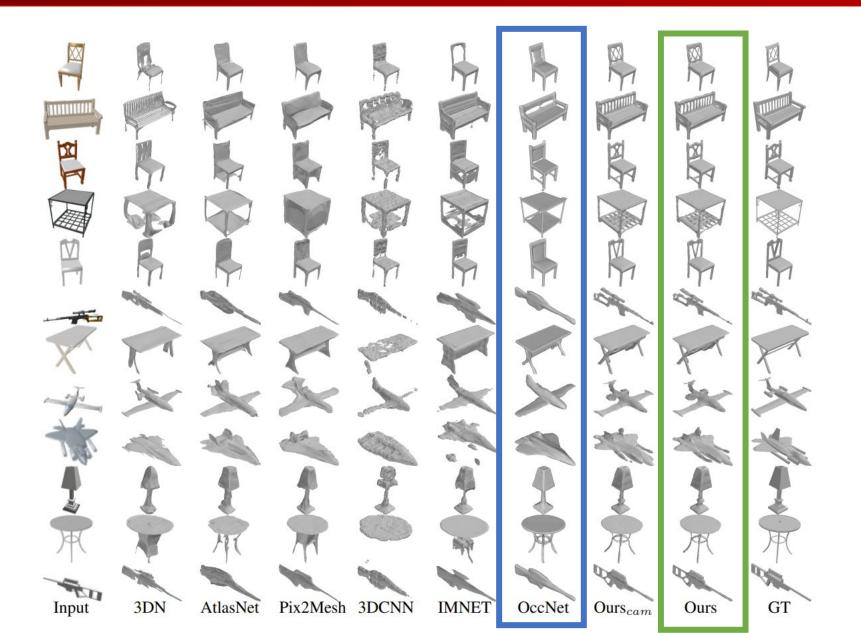
- **Camera Pose Network:** Estimate the camera pose, the 6 DoF transformation from the camera coordinate to world coordinate.
- Local Feature Extraction Network: Using the camera pose find a 3D point's 2D location on the image and extract local feature patches from multiple network layers.



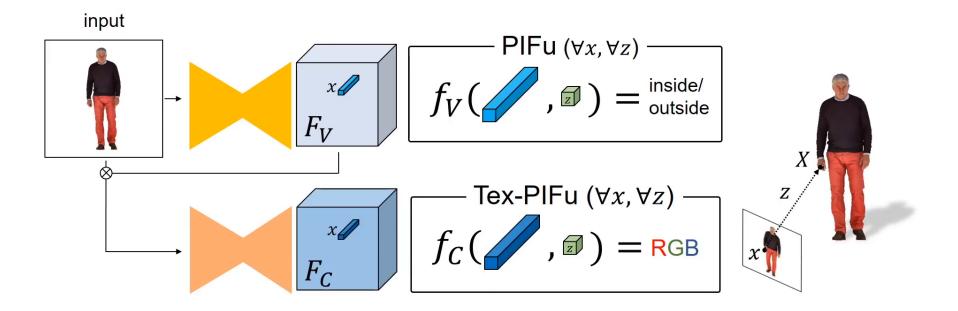


**Local Feature Extraction Network** 

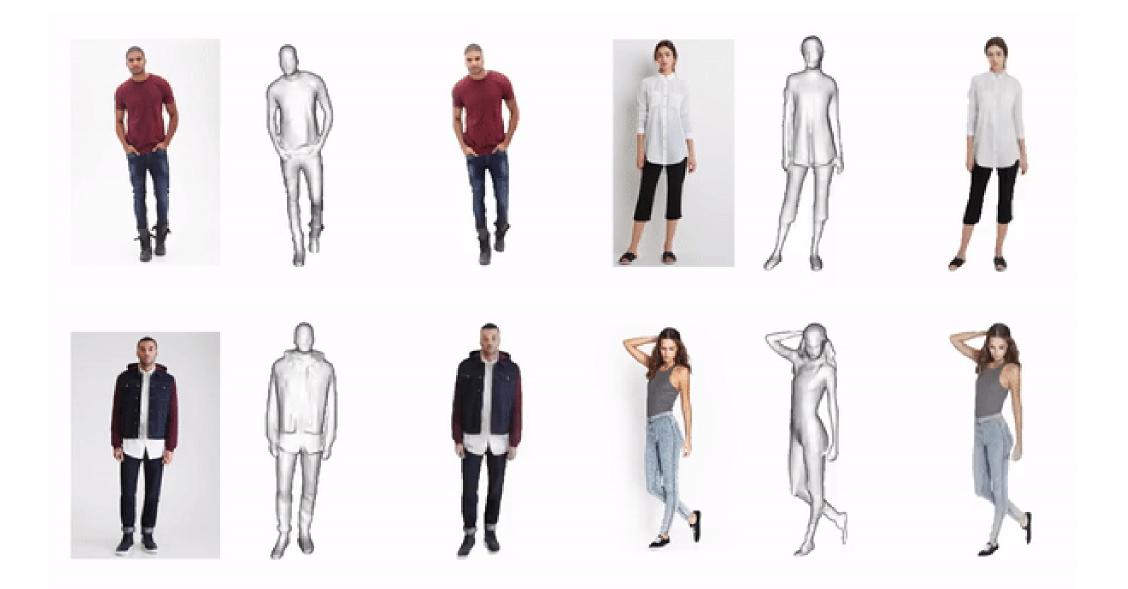
#### How well does it work?



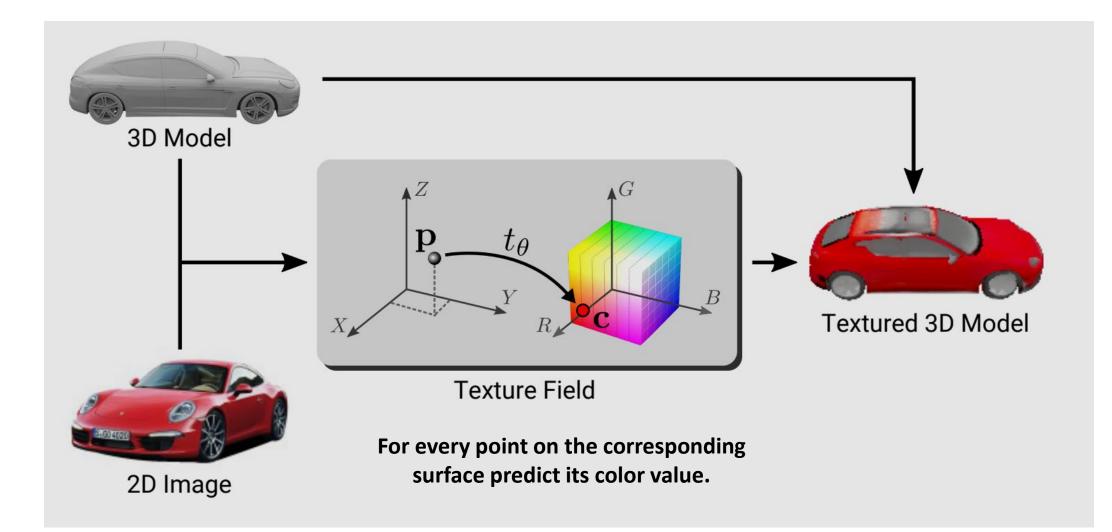
#### **PIFu: Pixel-Aligned Implicit Function**



#### What about Texture?



#### A Similar Idea: Texture Fields

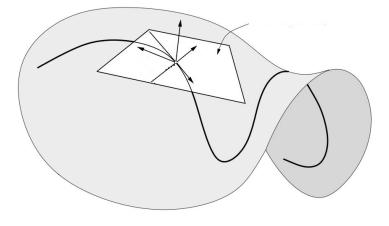


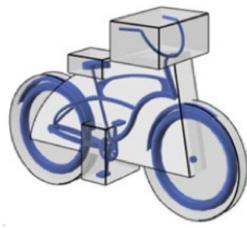
# Shape Deformations / Edits and Variation Generation

### Generative Models for Deformations / Edits

Learn possible variations of an input shape, meeting semantic constraints.

latent space







#### Motivation

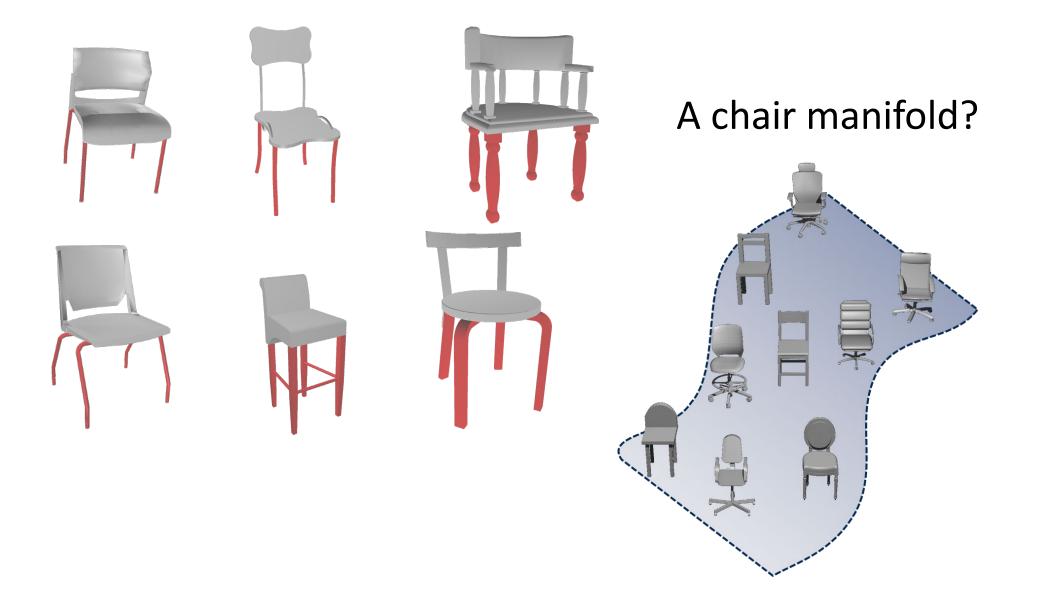
• Leverage on existing artist generated models



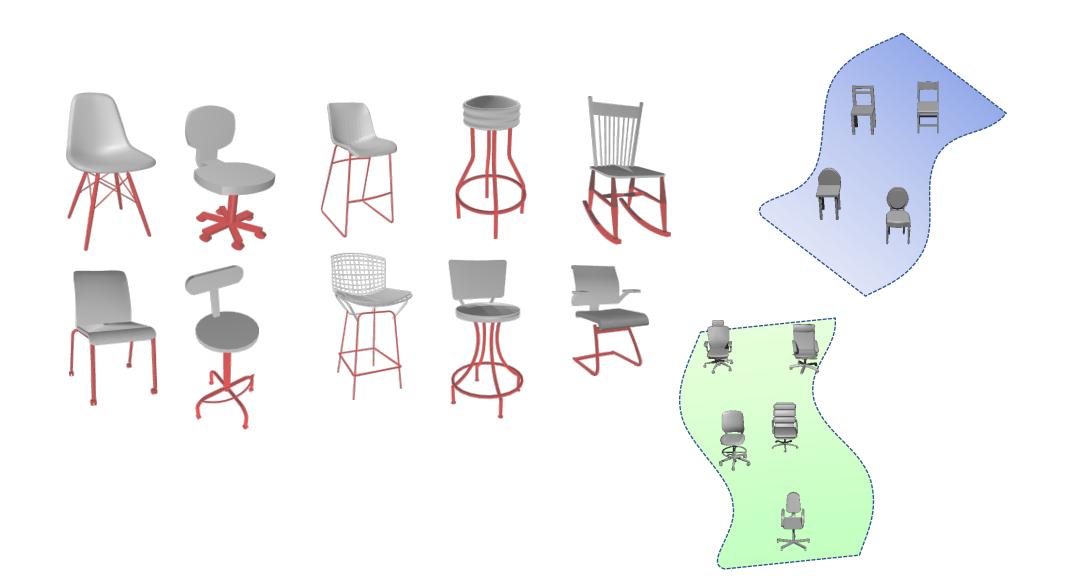
• Create new models through deformations and edits



#### **Continuous Shape Variability**

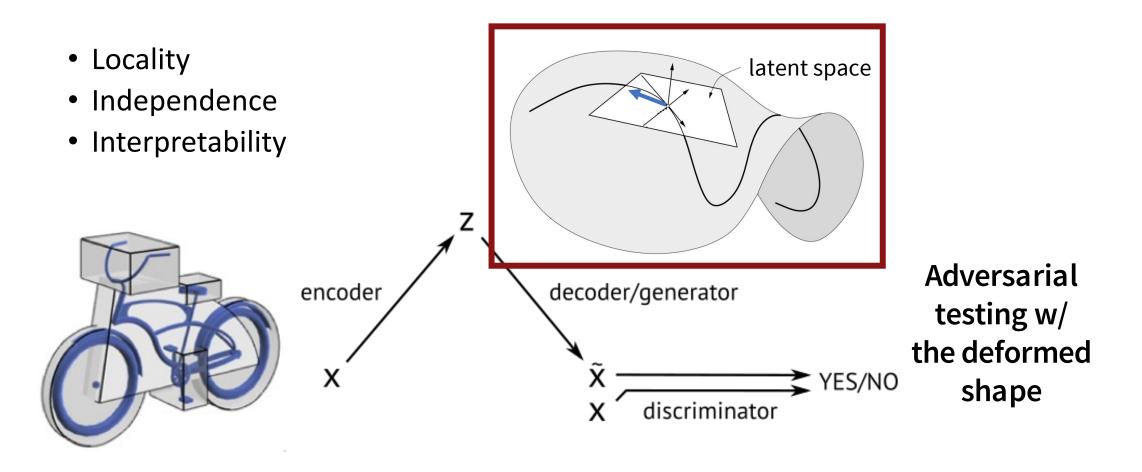


#### **Combinatorial or Discrete Variability**

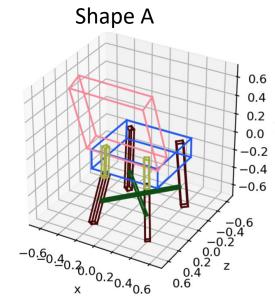


#### Shapes are often Over-Parametrized for Edits

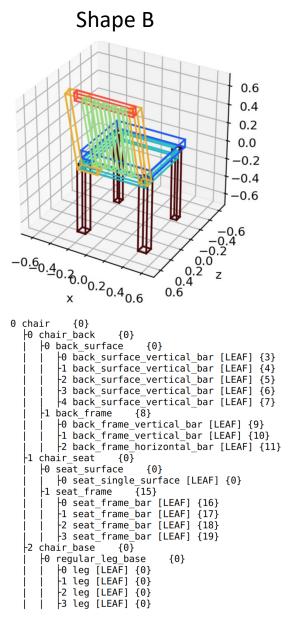
Learn a reduced parameter space and enforce that each learned parameter represents an <u>intuitive</u> deformation or change.



#### Shape Differences as First-Class Citizens



0 chair {0} -0 chair back  $\{1\}$ -0 back surface {2} -0 back\_single\_surface [LEAF] {3} -1 back connector [LEAF] {4} -2 back connector [LEAF] {5} -1 chair seat {6} -0 seat surface {7} -0 seat single surface [LEAF] {8} -2 chair base {9} -0 regular leg base {10} +0 leg [LEAF] {11} -1 leg [LEAF] {12} -2 leg [LEAF] {13} -3 leg [LEAF] {14} -4 bar stretcher [LEAF] {15} -5 bar stretcher [LEAF] {16}



#### Shape Diff

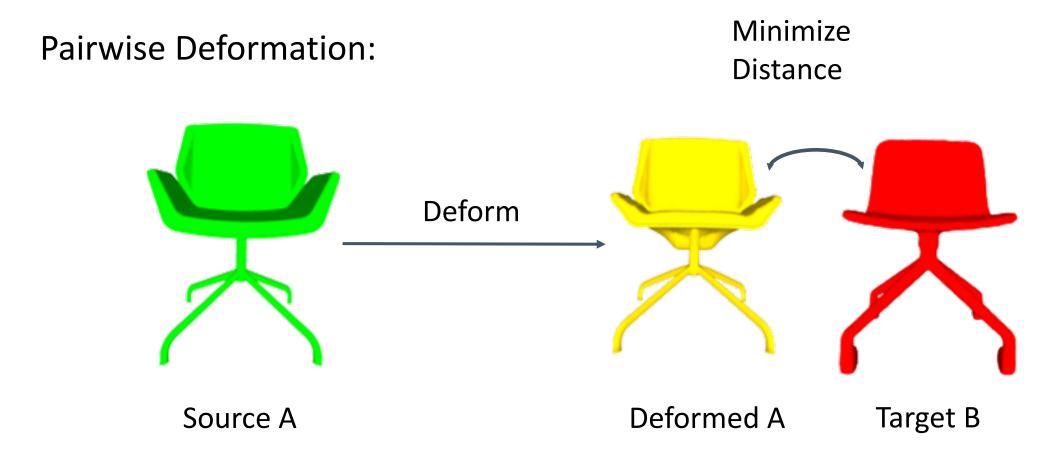
0	[DiffNode: SAME]			
	<b>⊦</b> 0	0 [DiffNode: SAME]		
		<u>+0</u>	[DiffNode: SAME]	
			-0 [DiffNode: DEL]	
			-1 [DiffNode: ADD]	
			+0 back_surface_vertical_bar [LEAF] {3}	
			-2 [DiffNode: ADD]	
			-0 back_surface_vertical_bar [LEAF] {4}	
			-3 [DiffNode: ADD]	
			+0 back_surface_vertical_bar [LEAF] {5}	
			-4 [DiffNode: ADD]	
			-0 back_surface_vertical_bar [LEAF] {6}	
			-5 [DiffNode: ADD]	
			+0 back_surface_vertical_bar [LEAF] {7}	
			[DiffNode: DEL]	
			[DiffNode: DEL]	
	ļ .	-3	[DiffNode: ADD]	
	!	ļ.	0 back_frame {8}	
	!	!	0 back_frame_vertical_bar [LEAF] {9}	
	!	!	-1 back_frame_vertical_bar [LEAF] {10}	
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	-1		ffNode: SAME]	
	!	<b>۳</b>	[DiffNode: SAME]	
	!	1	+0 [DiffNode: LEAF] [DiffNode: ADD]	
	!	LT.	0 seat frame {15}	
		!	+0 seat frame bar [LEAF] {16}	
		!	-1 seat frame bar [LEAF] {17}	
		!	-2 seat frame bar [LEAF] {17}	
	!	!	-3 seat_frame_bar [LEAF] {19}	
	-2	l [Di	ffNode: SAME]	
	12		[DiffNode: SAME]	
		10	0 [DiffNode: LEAF]	
	1	1	-1 [DiffNode: LEAF]	
		1		
	1	1	-2 [DiffNode: LEAF] -3 [DiffNode: LEAF]	
		1	-4 [DiffNode: DEL]	
	1	1	-4 [DiffNode: DEL] -5 [DiffNode: DEL]	
		1	1	

Continuous Shape Variations: Deformations

## Neural ODEs for Shape Deformation

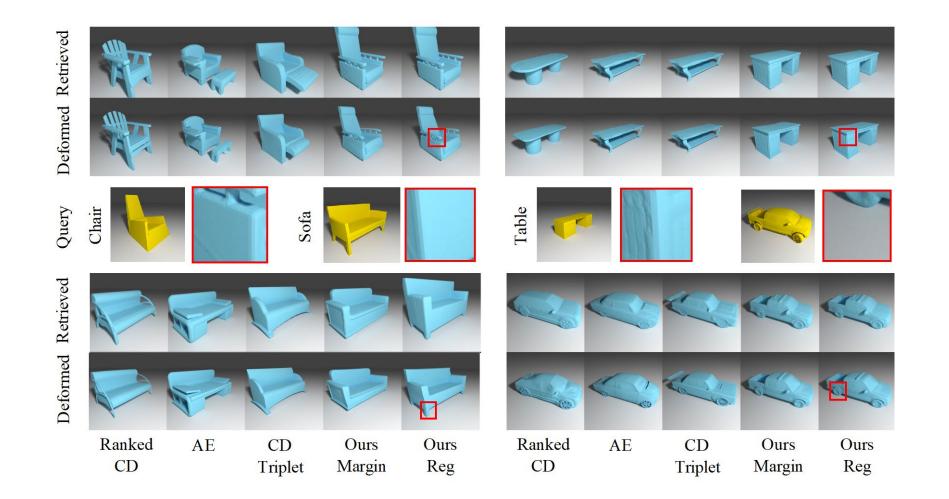
MeshFlow: A Robust and Scalable Shape Deformation Framework. Jingwei Huang, Max Jiang, Baiqiang Leng, Bin Wang, Leonidas Guibas.

### **Problem Setup: Semantic Deformation**

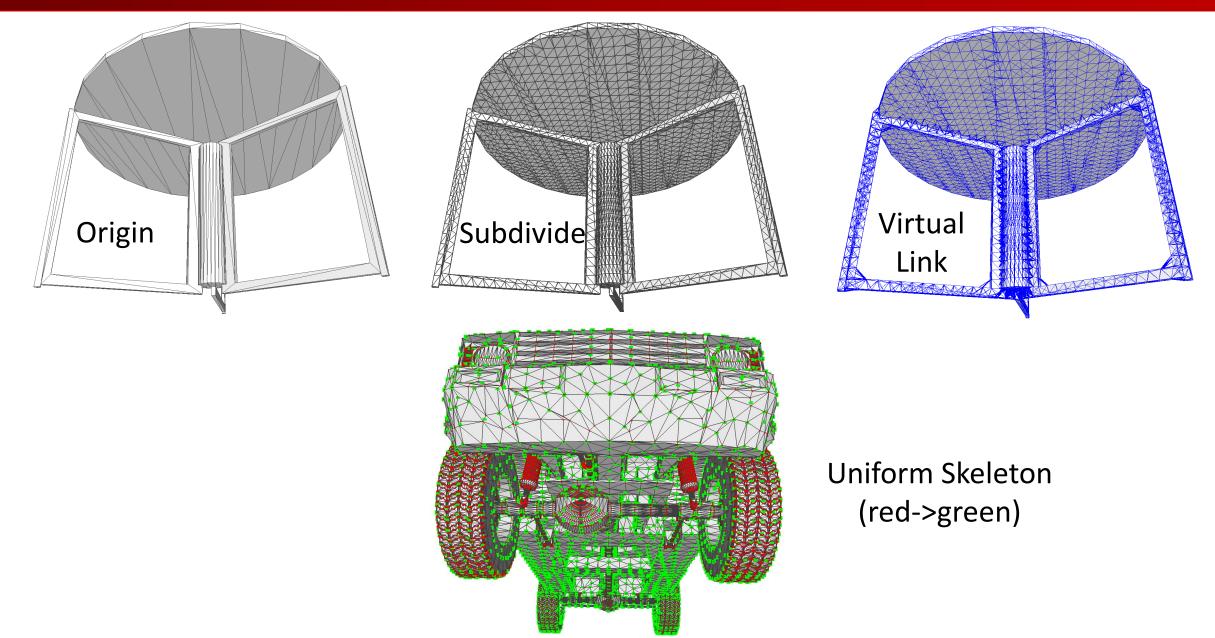


Source geometry provides "style" while target provides "pose". Geometric "style" transfer.

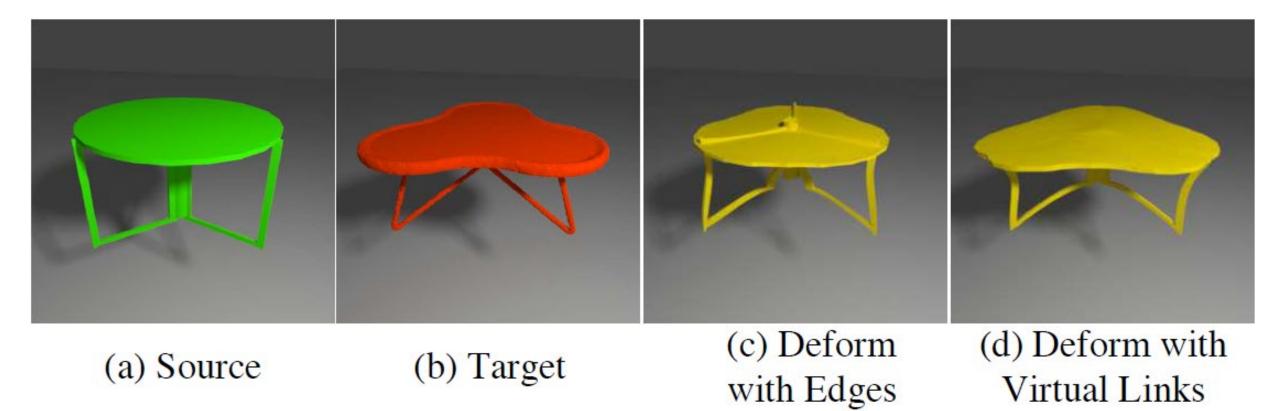
### "As Rigid As Possible" (ARAP) Deformations



### Remeshing: Mesh to Uniform Skeleton Graph



### **Uniform Skeleton Graph Representation**



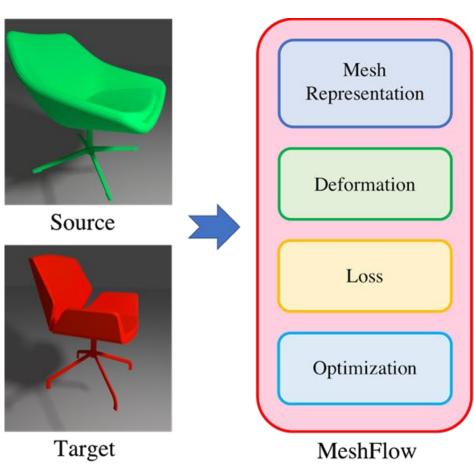
### Methodology

- A general interface for shape deformation optimization
  - Mesh representation to support effective Non-rigid ICP
  - Support general deformation functions

Fitness to destination + Preservation of constraints

- Deep flow-based method
  - A bijective mapping
  - No self-intersection
  - Encourages but does not rely on rigidity during optimization
  - Better alignment

### MeshFlow Key Modules





Shape Animation and Deformation



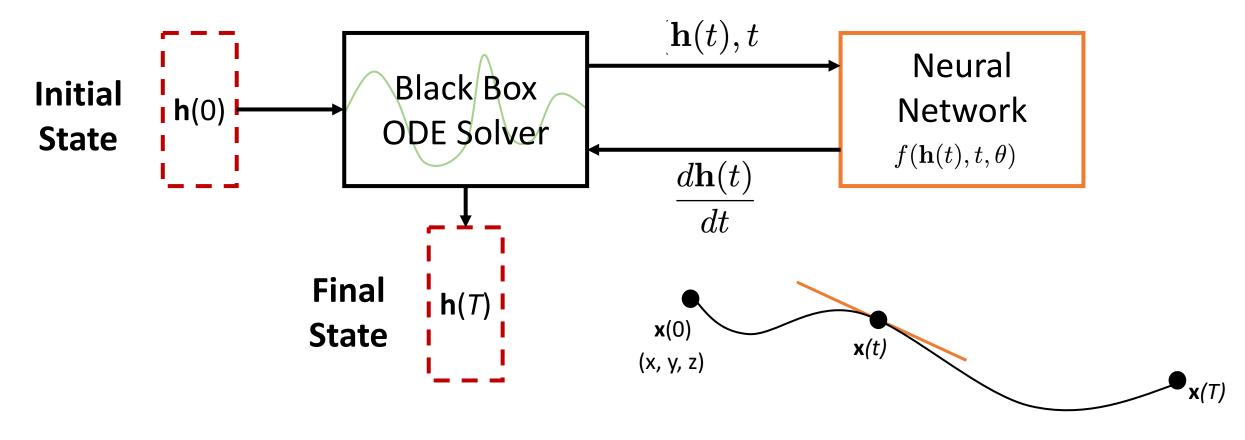
Fit Scan with CAD



**Texture Optimization** 

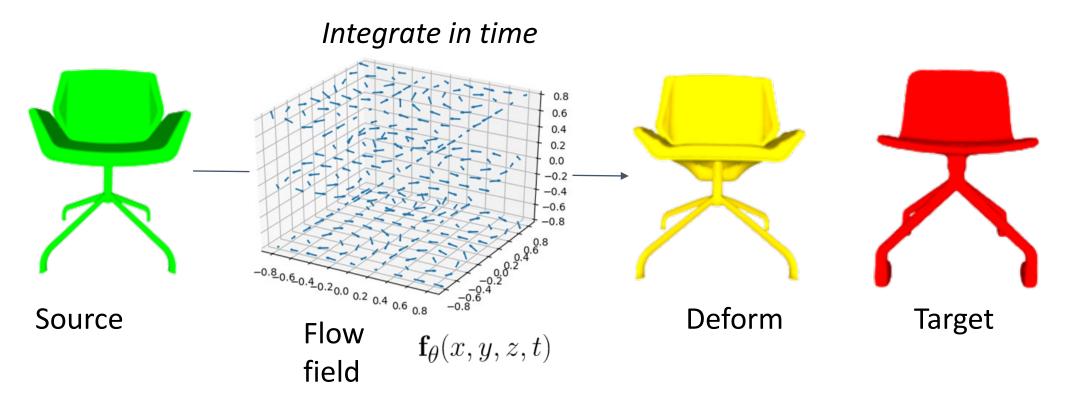
### **Neural Ordinary Differential Equations**

- Key idea: neural network gives derivative, ODE solver to integrate
- Gives "infinite depth" nets and continuous representation of time series



### **Deep Flow-Based Deformation**

Use Neural ODE + learned flow model to deform geometries.



Parameterize a learnable flow field  $\mathbf{f}_{\theta} : \mathbb{R}^4 \mapsto \mathbb{R}^3$  using a fully connected neural network that outputs three velocity components for every point at every time. Advecting the source shape by integrating an ODE produces the resulting deformed shape.

### **Deep Flow-Based Deformation**

Denote the mapping induced by convecting the geometry using Neural ODE as:

$$\Phi_{\theta}(\mathbf{X}_0) = \mathbf{X}_0 + \int_0^1 \mathbf{f}_{\theta}(\mathbf{X}(t), t) dt$$

The mapping is bijective since the inverse of the mapping can be easily acquired by inverting the integration order.

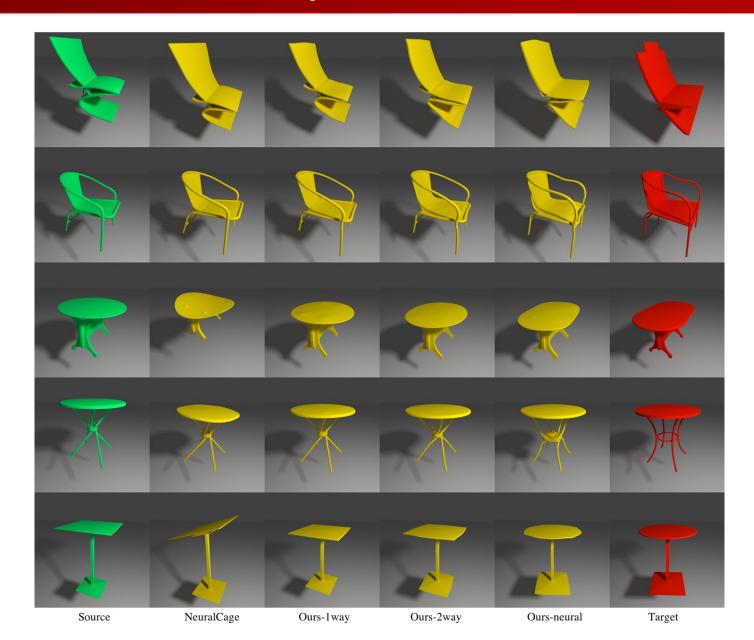
$$\Phi_{\theta}^{-1}(\mathbf{X}_1) = \mathbf{X}_1 + \int_1^0 \mathbf{f}_{\theta}(\mathbf{X}(t), t) dt$$

Therefore the deformation field between two shapes can be learned via optimizing for a symmetric deformation loss between the two shapes:

argmin 
$$\mathcal{L}(\theta) = \mathcal{C}(\Phi_{\theta}(\mathbf{X}_0), \mathbf{X}_1) + \mathcal{C}(\Phi_{\theta}^{-1}(\mathbf{X}_1), \mathbf{X}_0)$$

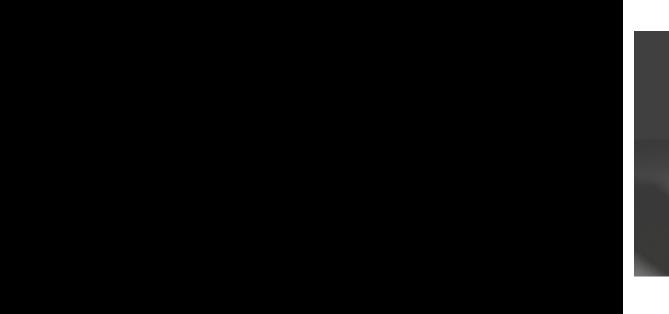
Here  ${\cal C}$  is a differentiable geometric loss. A simple choice is Chamfer loss.

### **Deformation Comparison**



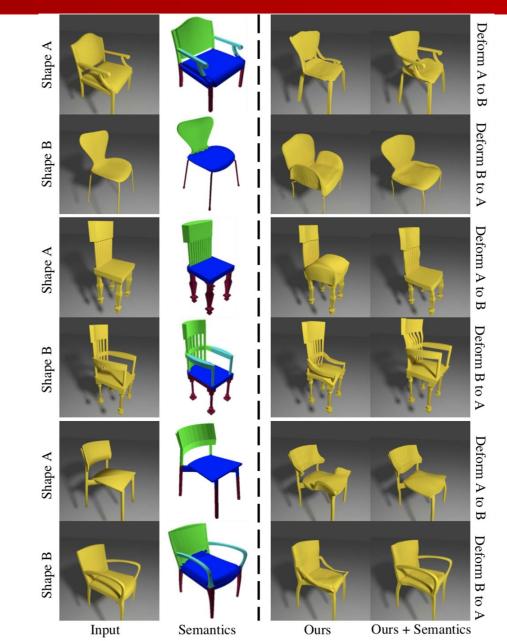
### **Deformation Video**





### Scan2CAD & Part Deformation









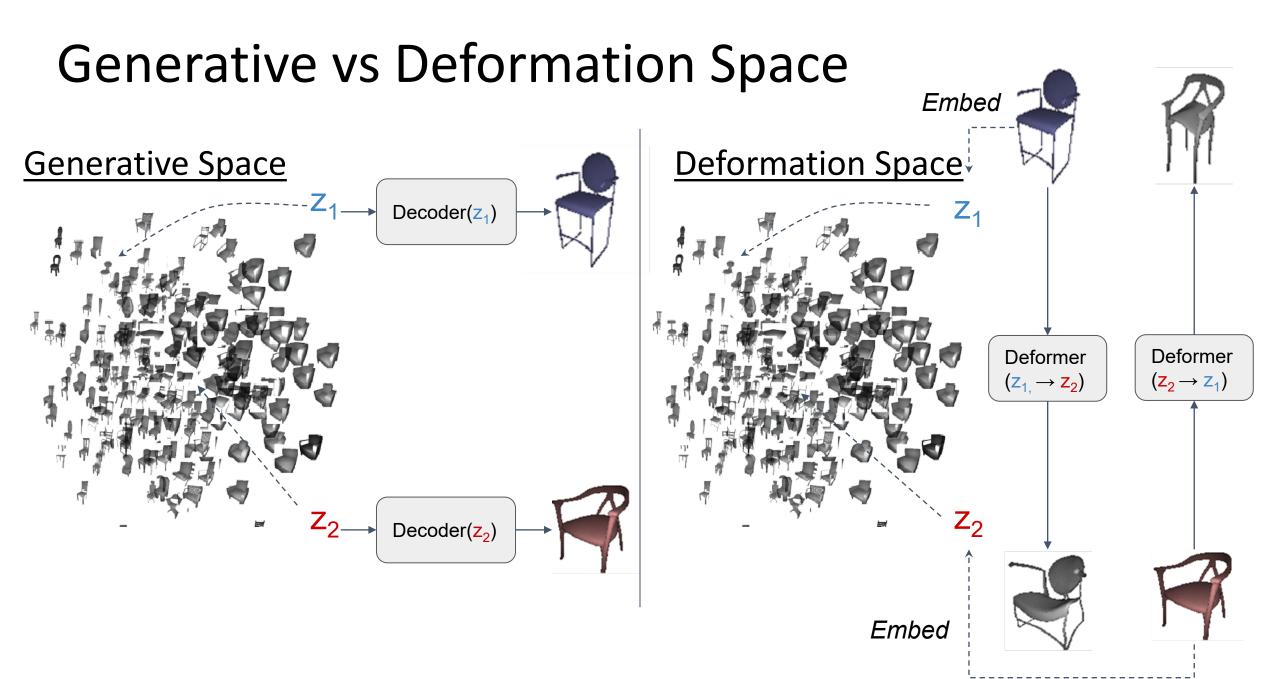
2020

## ShapeFlow

Learnable Deformations Among 3D Shapes

Chiyu "Max" Jiang <sup>1</sup>, Jingwei Huang <sup>2</sup>, Andrea Tagliasacchi <sup>3</sup>, Leonidas Guibas <sup>2</sup>

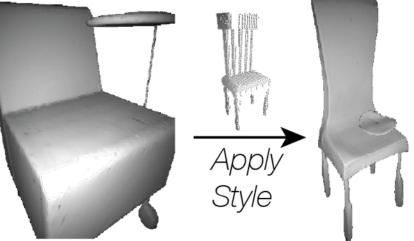
<sup>1</sup> UC Berkeley, <sup>2</sup> Stanford University, <sup>3</sup> Google Brain



### **Deformation Space**

A deformation space naturally allows the disentanglement of geometric style (coming from the source) and structural pose (conforming to the target).



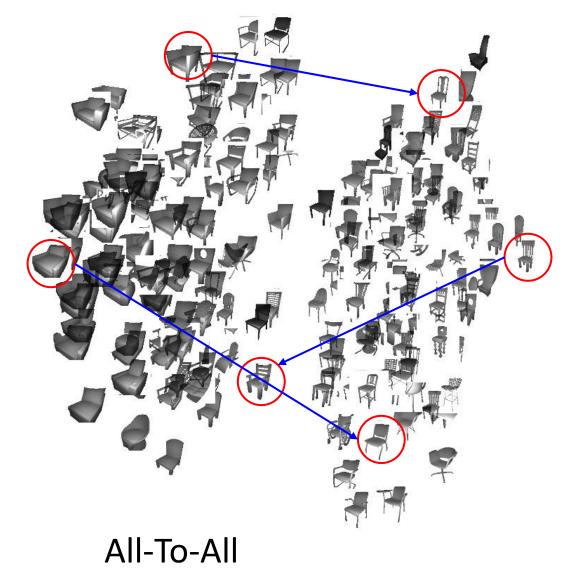


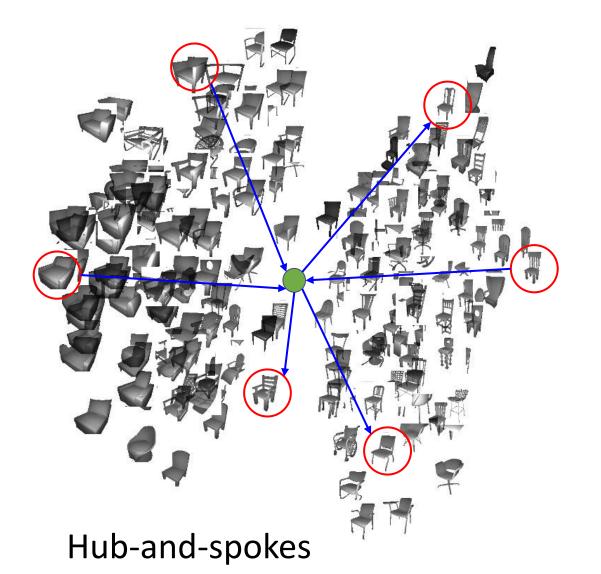
## **Regularizing Deformation Flows**

Furthermore, we can apply implicit and explicit flow regularization to ensure various desirable deformation properties.

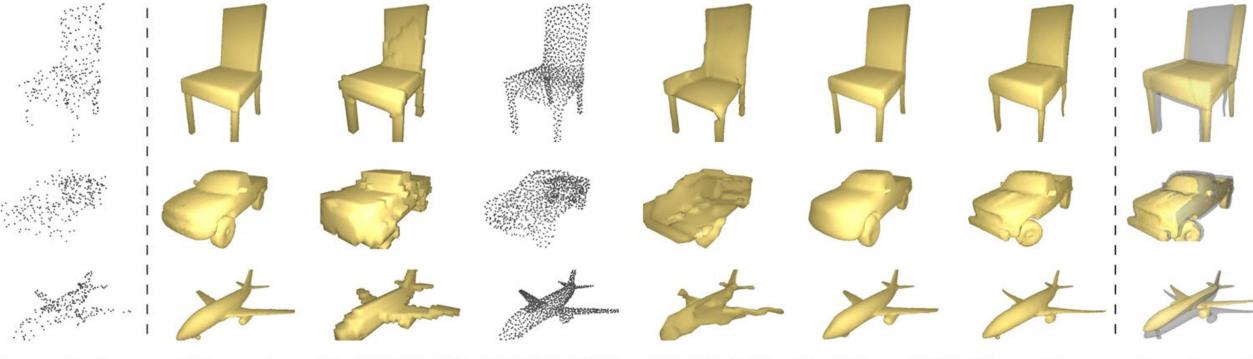
- Implicit regularization: volume conservation
- Implicit regularization: symmetries.
- Explicit regularization: surface metrics

### Hub-and-Spoke Deformation



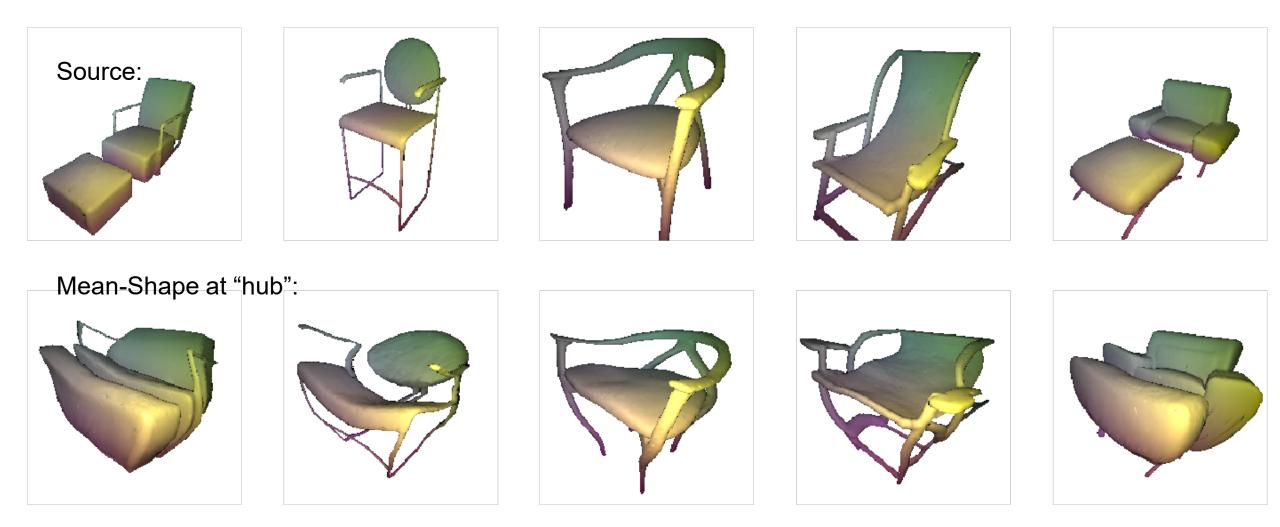


### **Experiment - Reconstruction via Deformation**



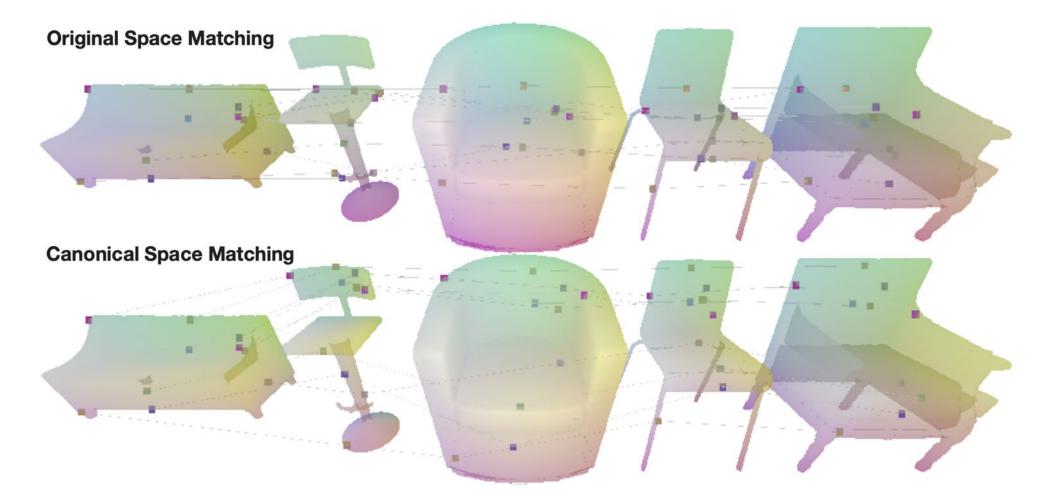
Input Points GT mesh 3D-R2N2 [5] PSGN [56] DMC [59] OccFlow [38] ShapeFlow Retrieved

### Deformation to "Mean Shape" in Canonical Space



Shapes naturally align when deformed to the common "hub" in an unsupervised manner.

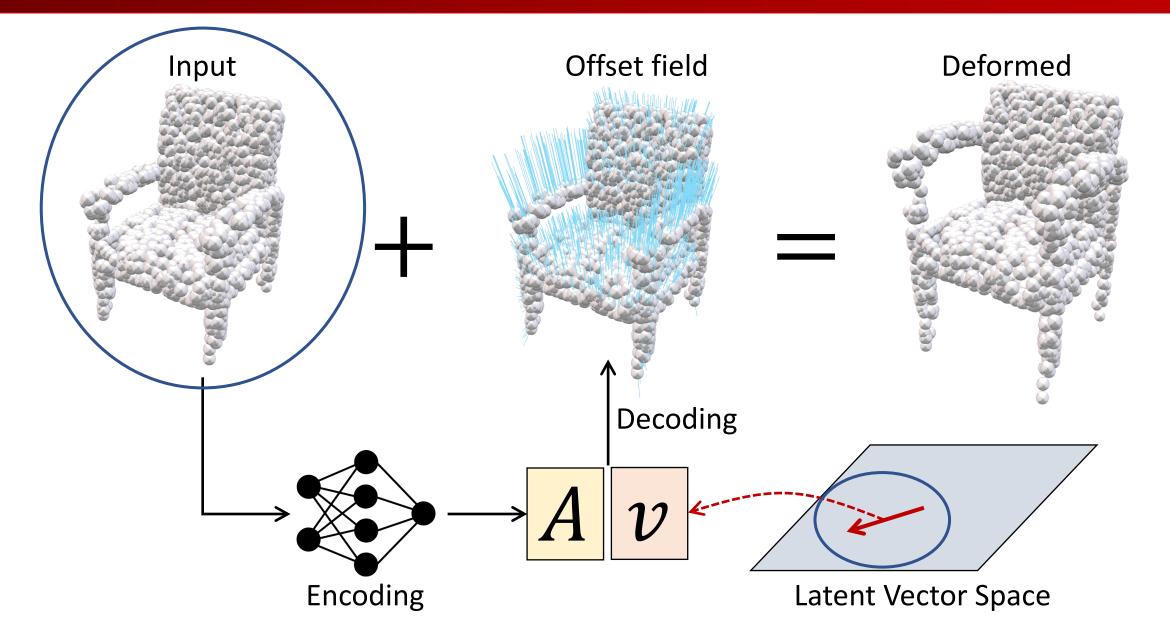
# Experiment: Unsupervised Shape Correspondences



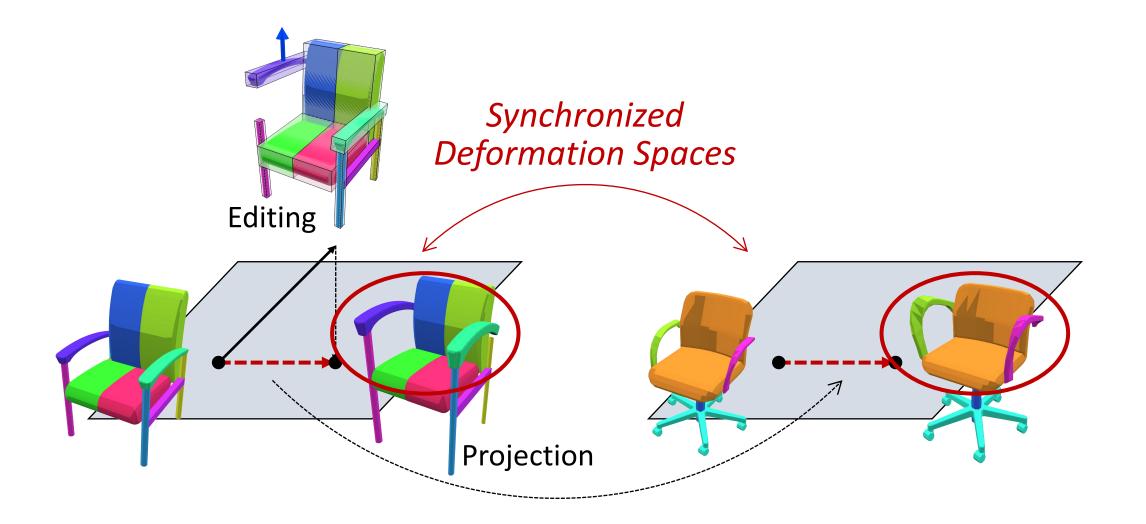
# DeformSyncNet

DeformSyncNet: Deformation Transfer via Synchronized Shape Deformation Spaces . Minhyuk Sung, Zhenyu Jiang, Panos Achlioptas, Niloy J. Mitra, and Leonidas J. Guibas. SIGGRAPH Asia 2020

### **Embedding Space for Deformations and Variations**



### Synchronized Shape Edit/Deformation Spaces



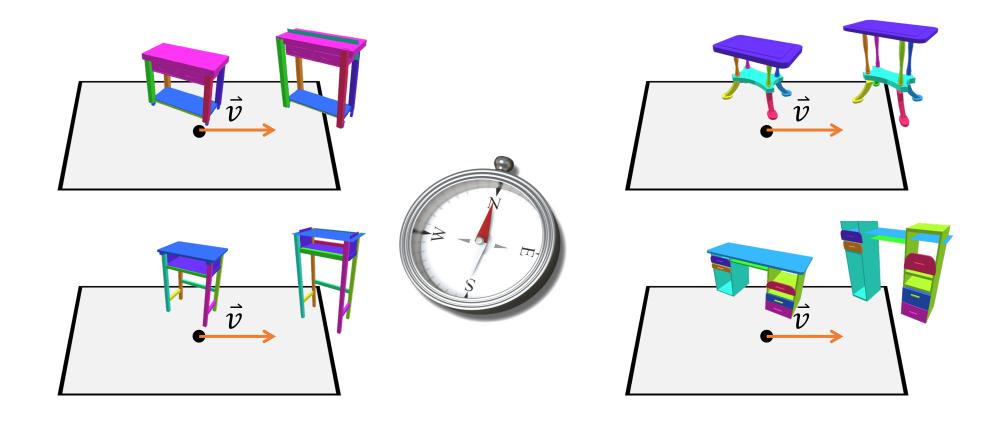
### Learning and Exploiting Correlations in Deformations

Transfer deformations across shapes without correspondences.



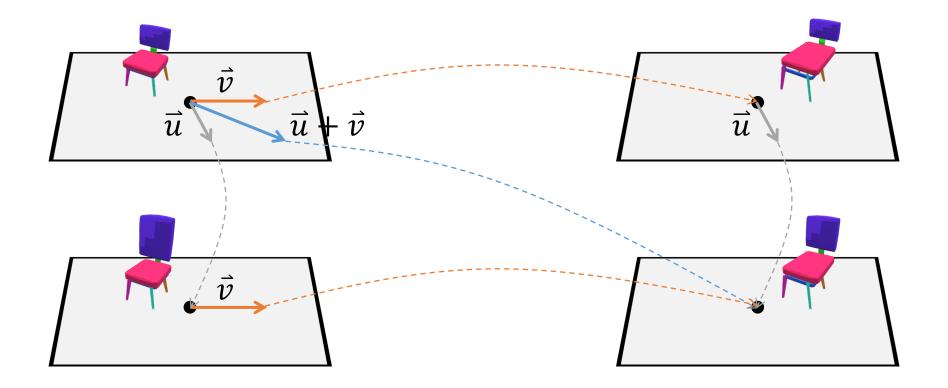
### Consistency

We aim to have a latent vector meaning the same thing everywhere: e.g.,  $\vec{v} = \langle 1, 0, \dots, 0 \rangle$  Indicates "elongate legs".

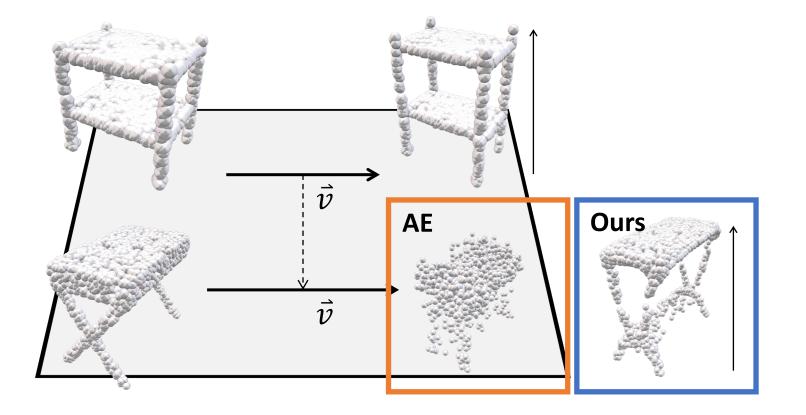


### Path Invariance

We want to reach to the same destination, no matter which route we choose.



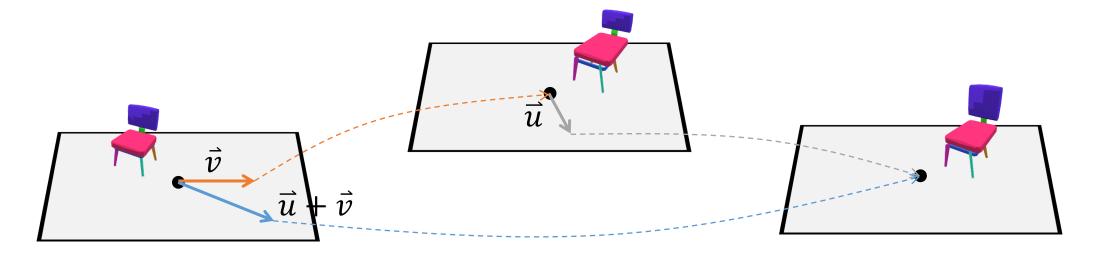
The axes of autoencoder latent spaces are not typically associated with semantically meaningful shape changes.



### A Latent Space for Deformations/Actions

An affine latent action space satisfies the following property:

Additive action:  $x \in X$ ,  $\vec{u}, \vec{v} \in V$ ,  $(x \oplus \vec{u}) \oplus \vec{v} = x \oplus (\vec{u} + \vec{v})$ .



### Autoencoder

An action defined with an antoencoder:

$$x \oplus \vec{v} \coloneqq \mathcal{D}(\mathcal{E}(x) + \vec{v}).$$

does not guarantee additivity and transitivity.

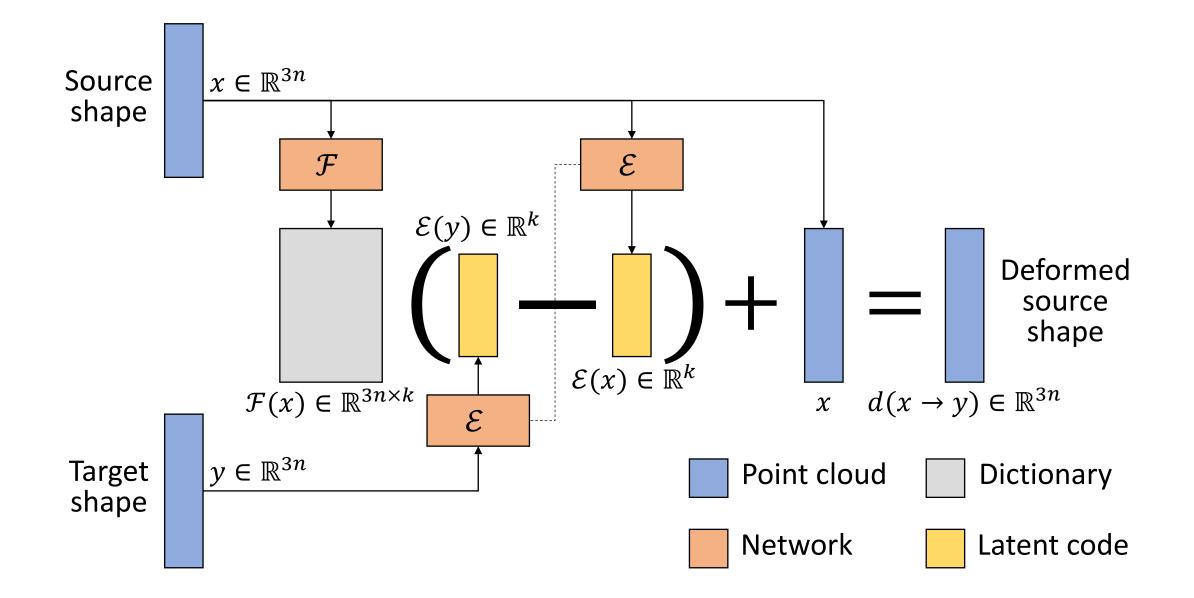
- A vector  $\vec{v}$  can act differently given the shape.
- Multiple vectors can be decoded to the same deformation.

We predict the deformation dictionary for each shape using another dictionary prediction network  $\mathcal{F} \in \mathbb{R}^{3n} \to \mathbb{R}^{3n \times k}$ .

The deformation  $d(x \rightarrow y)$  from shape x to y is computed as:

$$d(x \to y) = \mathcal{F}(x) \big( E(y) - E(x) \big) + x.$$

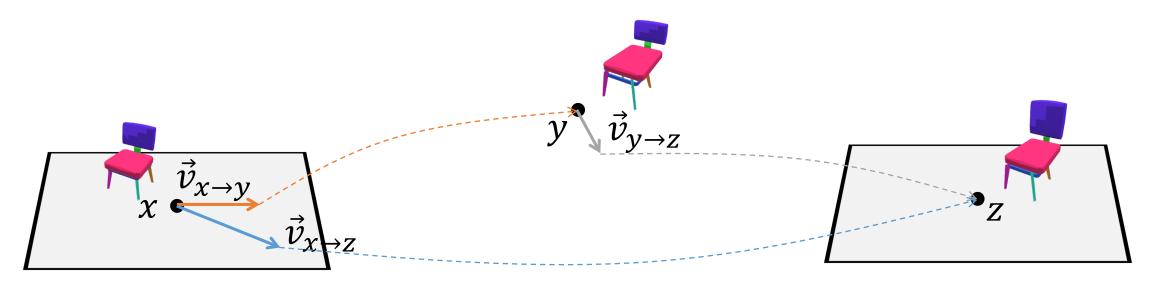
### Neural Network



### Path Invariance

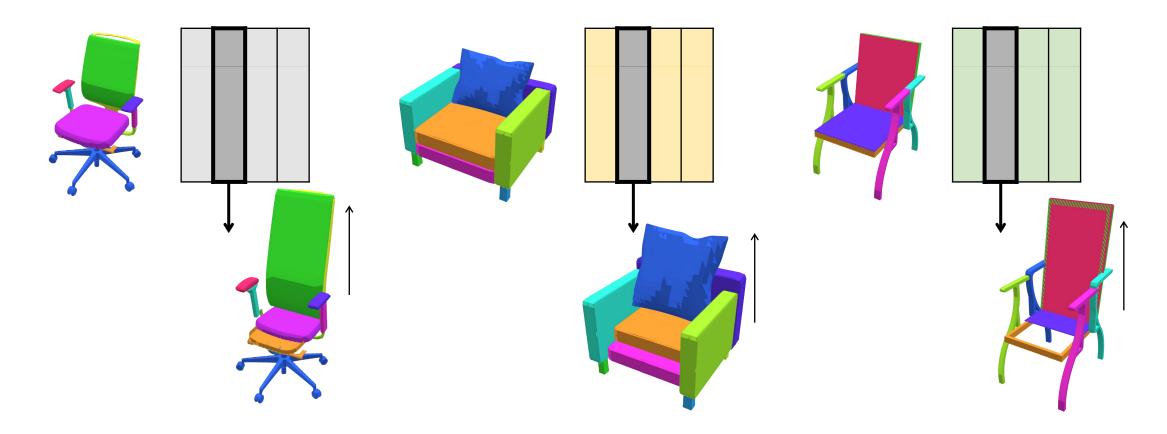
Reinforce consistency by imposing <u>path invariance</u>.

$$\vec{v}_{x \to y} + \vec{v}_{y \to z} = \vec{v}_{x \to z}$$



### Consistent Deformation Dictrionaries ${\mathcal F}$

Consistency across the deformation dictionaries **emerges** during training.



### **Deformation Dictionary**



#### Translating **seat** along the up/down direction.



### **Deformation Dictionary**

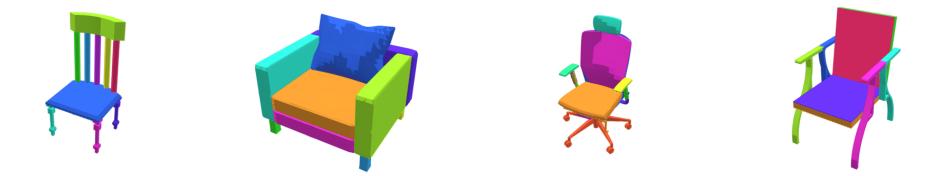


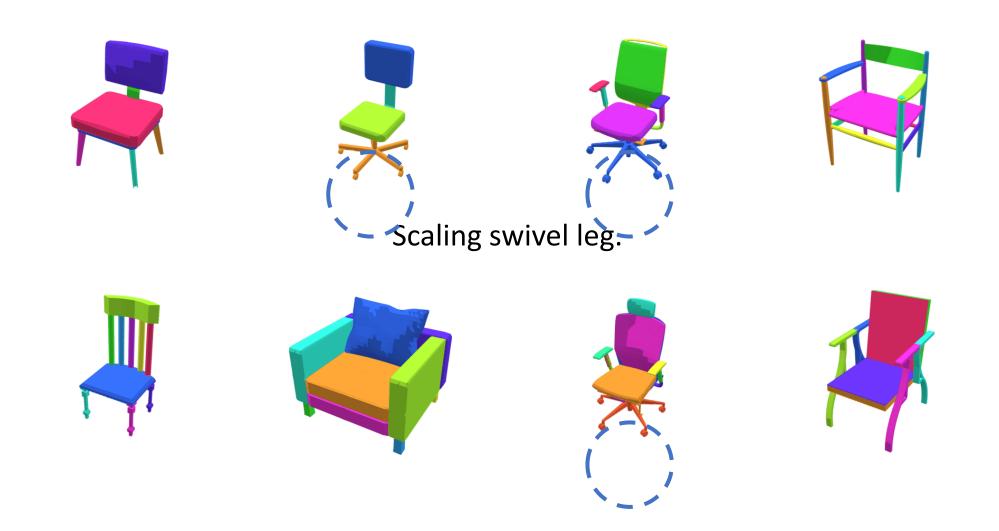
### Translating **back** along the front/back direction.

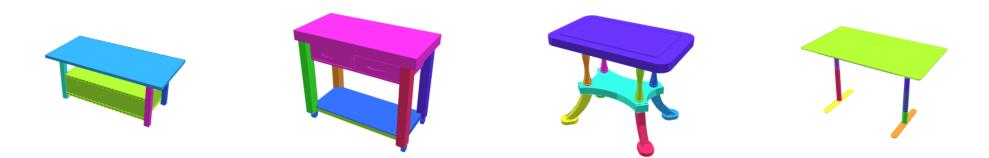




#### Scaling **back** along the up/down direction.

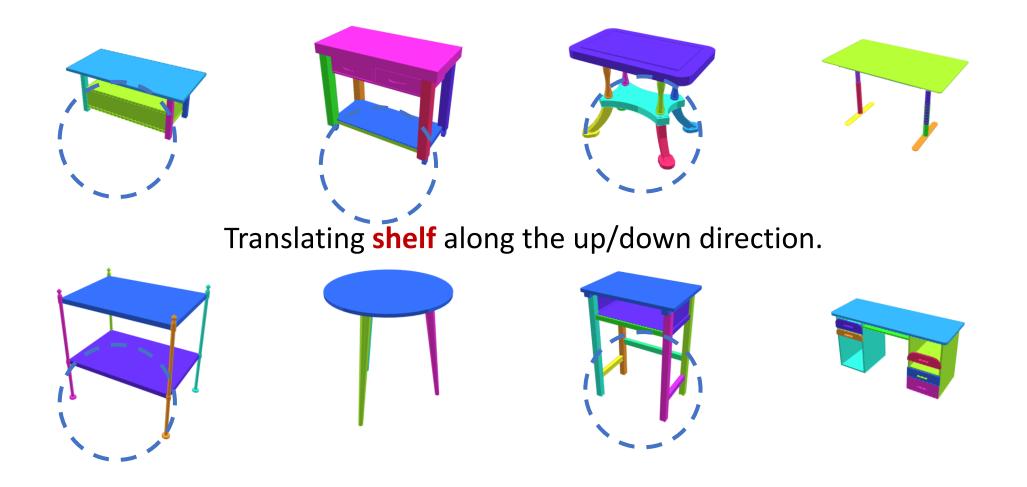


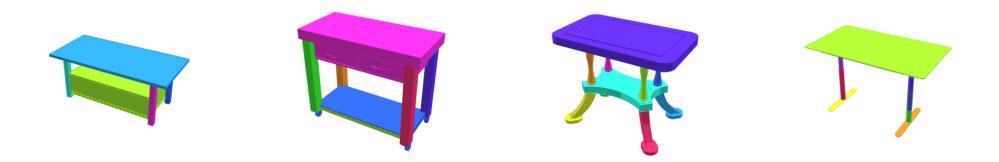




Scaling along the front/back direction.



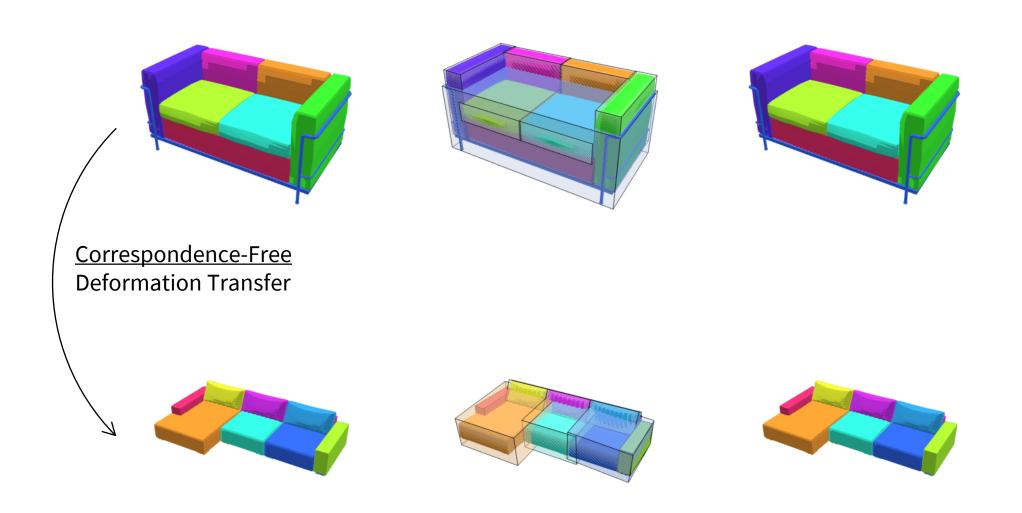




Translating **top** along the up/down direction.



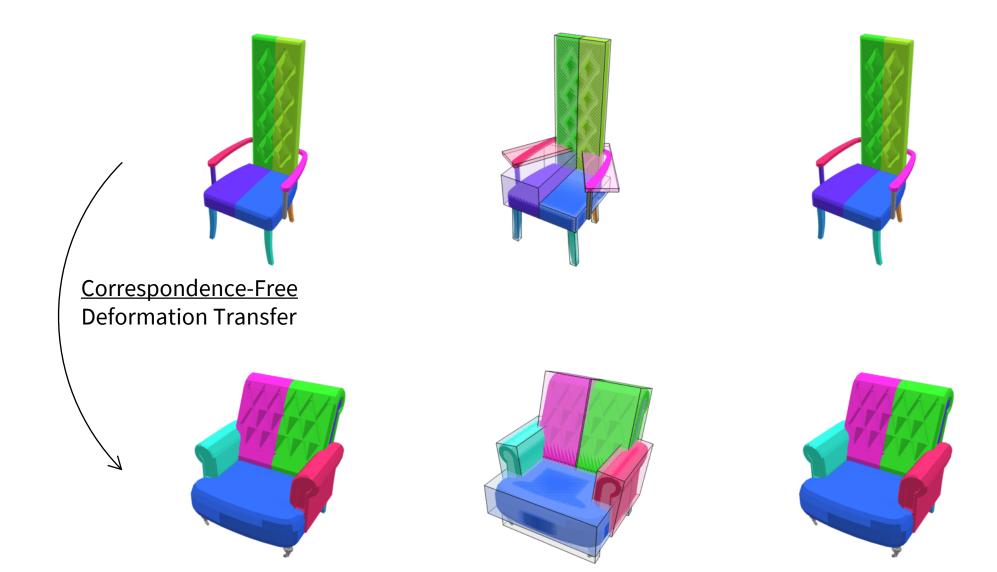
#### **Projection & Deformation Transfer**



#### **Projection & Deformation Transfer**

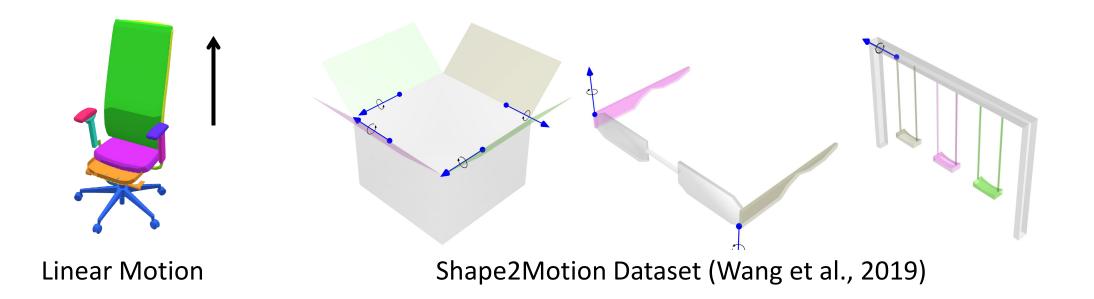


#### **Projection & Deformation Transfer**



#### **Extension to Circular Motion**

- Each item in the dictionary indicates a linear motion for each point.
- We change our formulation to predict a circular motion per point.



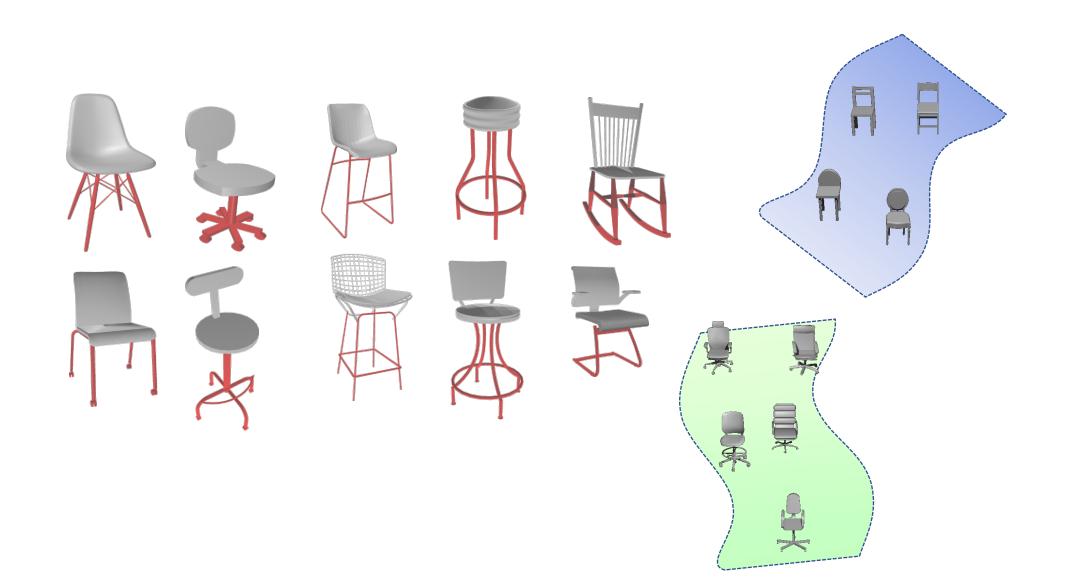
#### **Extension to Circular Motion**

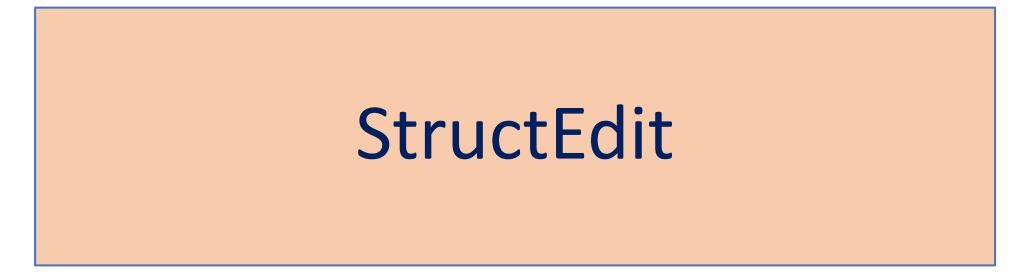
# 

**NOTE:** Transitivity is not guaranteed — there can exist multiple latent codes describing a specific deformation.

# **Discrete Shape Variations**

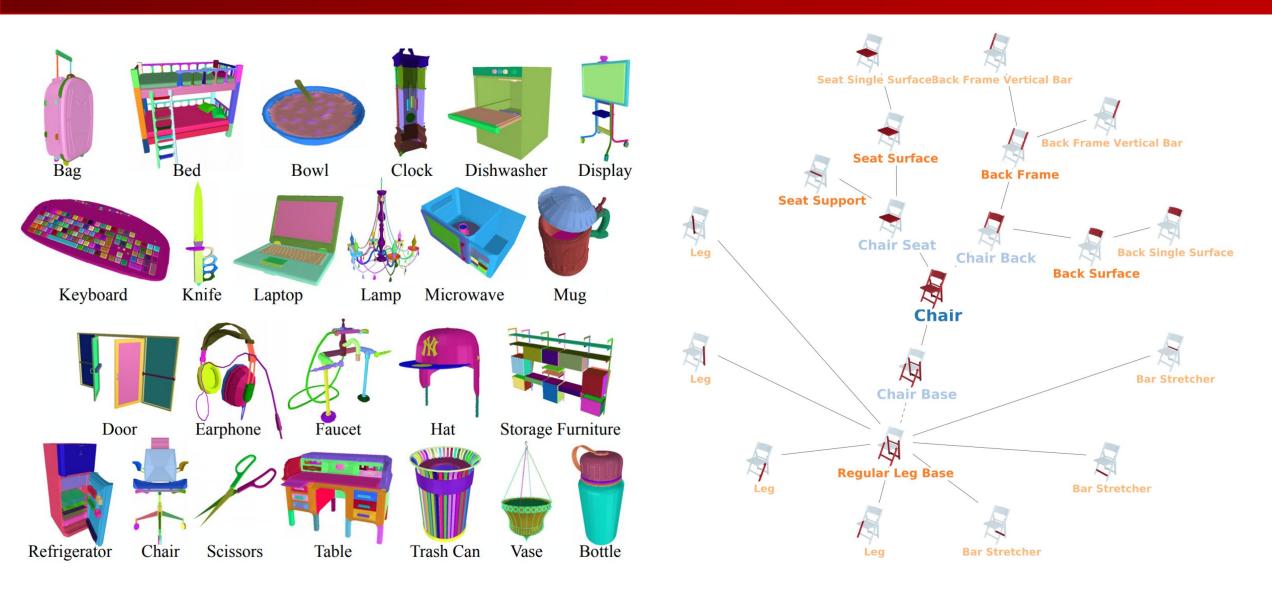
#### **Combinatorial or Discrete Variability**



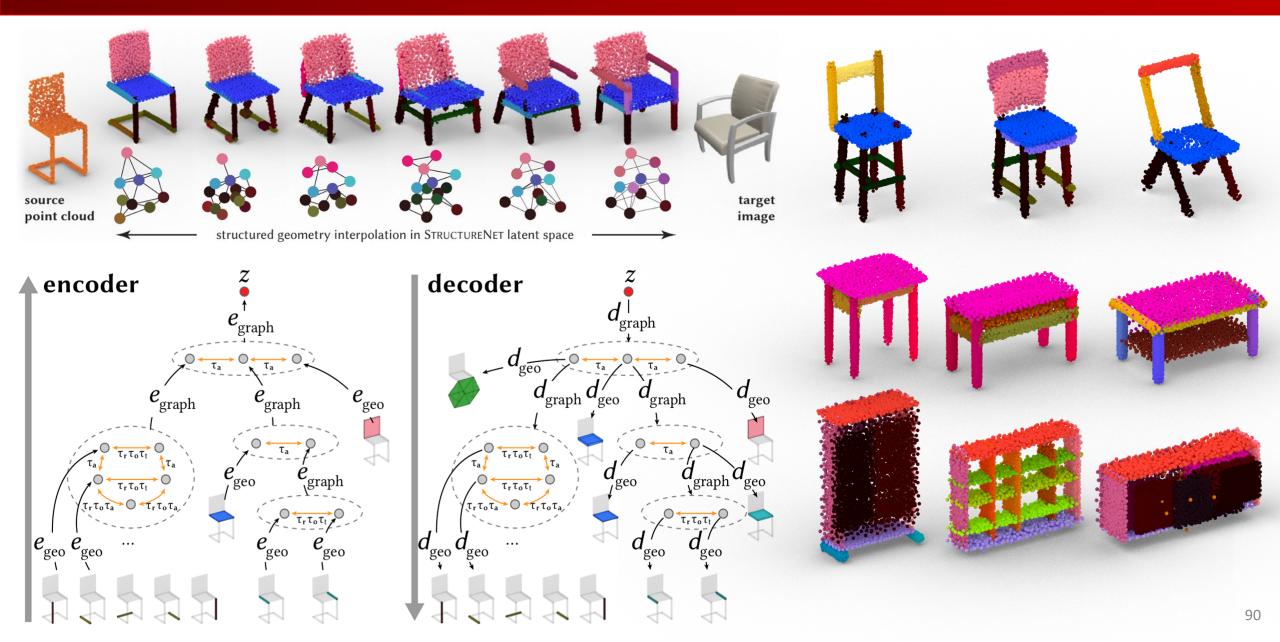


StructEdit: Learning Structural Shape Variations. Kaichun Mo, Paul Guerrero, Li Yi, Hao Su, Peter Wonka, Niloy Mitra, Leonidas J. Guibas. CVPR 2020.

#### Recap: PartNet (CVPR 2019)



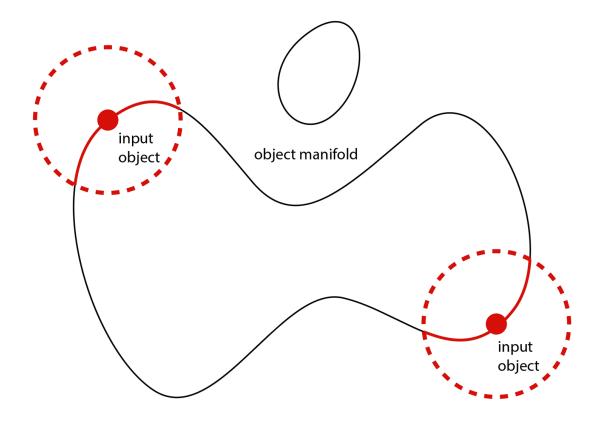
## Recap: StructureNet (Siggraph Asia 2019)



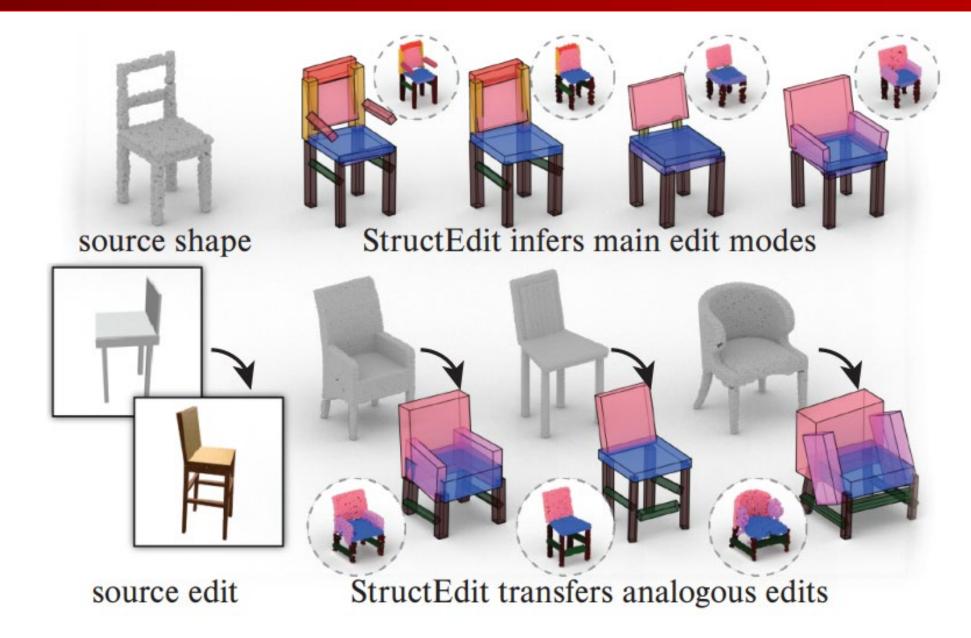
## Learn to Embed Local Shape Neighborhoods

#### <u>Learn a <mark>Structural</mark> Shape-diff Space, which is</u>

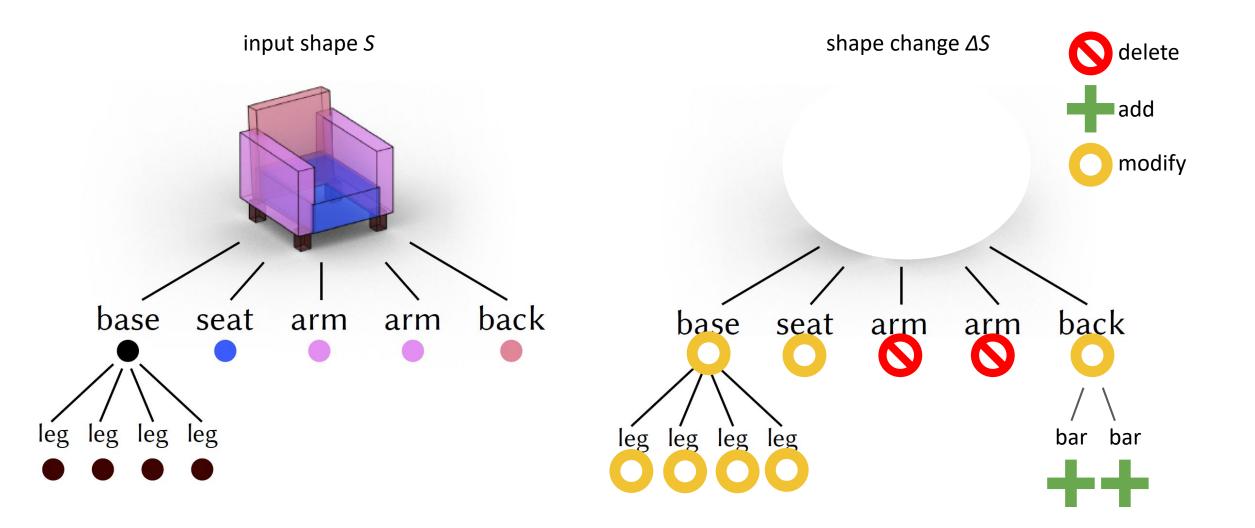
- **Unified**: learn one space that can be applied for any input shape
- **Specialized**: suggest different plausible shape-diff's for different input shapes
- Coherent: suggest similar plausible shapediff's for similar input shapes



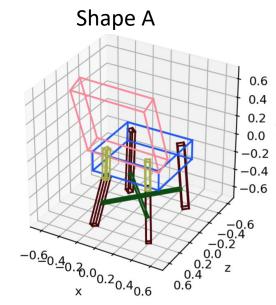
#### Learn Shape Structural Variations: StructEdit



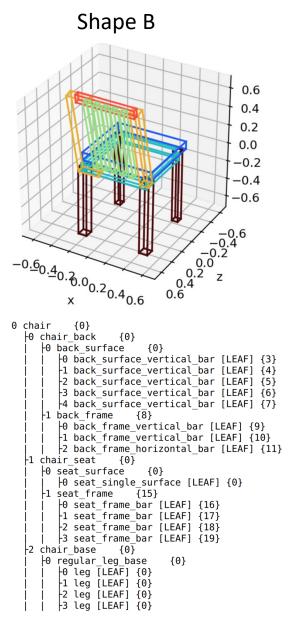
## Shape Difference (Structure + Deformation)



#### Shape Hierarchy Differences



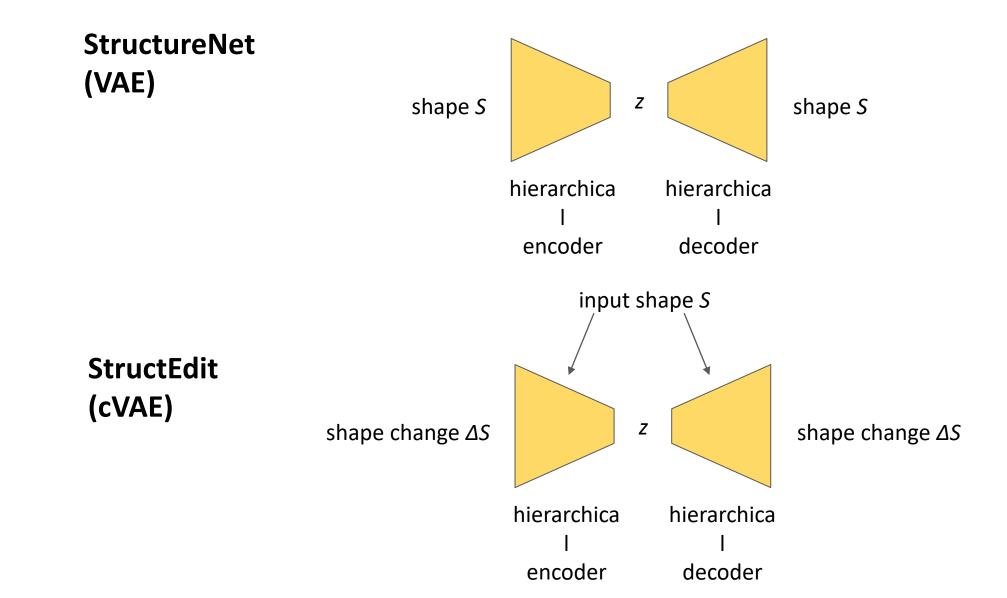
0 chair {0} -0 chair back  $\{1\}$ -0 back surface {2} -0 back\_single\_surface [LEAF] {3} -1 back connector [LEAF] {4} -2 back connector [LEAF] {5} -1 chair seat {6} -0 seat surface {7} | -0 seat single surface [LEAF] {8} -2 chair\_base {9} -0 regular leg base {10} +0 leg [LEAF] {11} -1 leg [LEAF] {12} -2 leg [LEAF] {13} -3 leg [LEAF] {14} -4 bar stretcher [LEAF] {15} -5 bar stretcher [LEAF] {16}



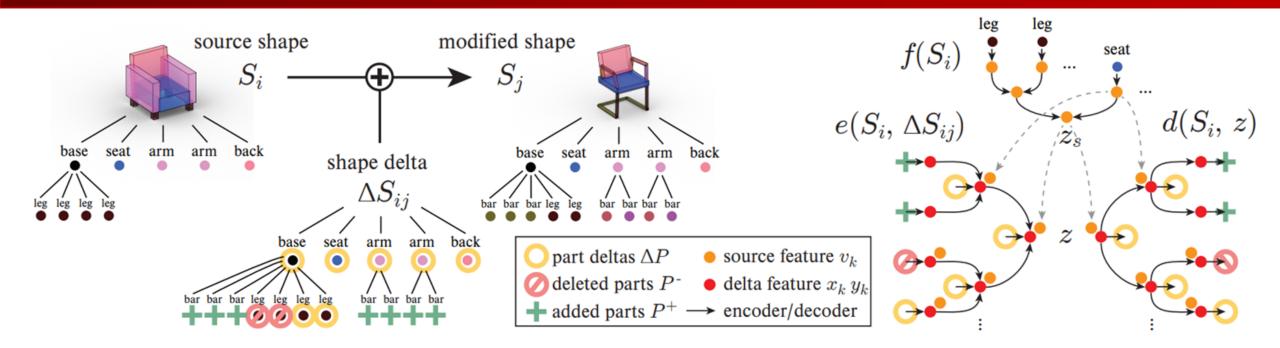
#### Shape Diff

0	[Di	ffN	ode: SAME]
	-0	[Di	ffNode: SAME]
	İ.	-0	[DiffNode: SAME]
	İ.	i	-0 [DiffNode: DEL]
	i	i	-1 [DiffNode: ADD]
	i	i	-0 back_surface_vertical_bar [LEAF] {3}
	i	i	-2 [DiffNode: ADD]
	i	i	0 back_surface_vertical_bar [LEAF] {4}
	İ	İ	-3 [DiffNode: ADD]
	Í	ĺ	0 back_surface_vertical_bar [LEAF] {5}
	Í	ĺ	-4 [DiffNode: ADD]
			-0 back_surface_vertical_bar [LEAF] {6}
			-5 [DiffNode: ADD]
			-0 back_surface_vertical_bar [LEAF] {7}
			[DiffNode: DEL]
		-3	·
			-0 back_frame {8}
	ļ		-0 back_frame_vertical_bar [LEAF] {9}
			<pre>1 back_frame_vertical_bar [LEAF] {10}</pre>
			<pre>  2 back_frame_horizontal_bar [LEAF] {11}</pre>
	F1		ffNode: SAME]
	!	<b>⊦</b> 0	[DiffNode: SAME]
	!		0 [DiffNode: LEAF]
	!	ĻΤ	[DiffNode: ADD]
	!	!	0 seat_frame {15}
	!		-0 seat_frame_bar [LEAF] {16}   -1 seat frame bar [LEAF] {17}
	!		-2 seat frame bar [LEAF] {17}
	!		-3 seat_frame_bar [LEAF] {19}
	-2	l [Di	ffNode: SAME]
	!		0 [DiffNode: LEAF]
	1	ł	-1 [DiffNode: LEAF]
	1	1	-2 [DiffNode: LEAF]
	1	1	-3 [DiffNode: LEAF]
	1	i i	-4 [DiffNode: DEL]
	1	i i	-5 [DiffNode: DEL]
	1		1

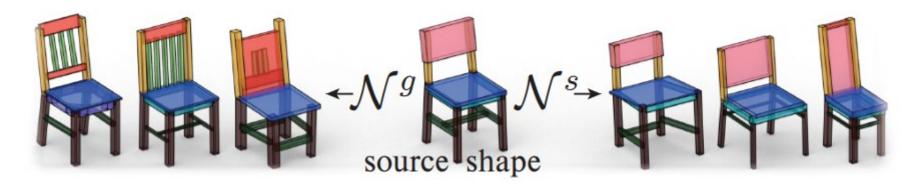
#### **Network Architecture**



## **Network Architecture**



#### **Two Types of Shape Neighborhood**

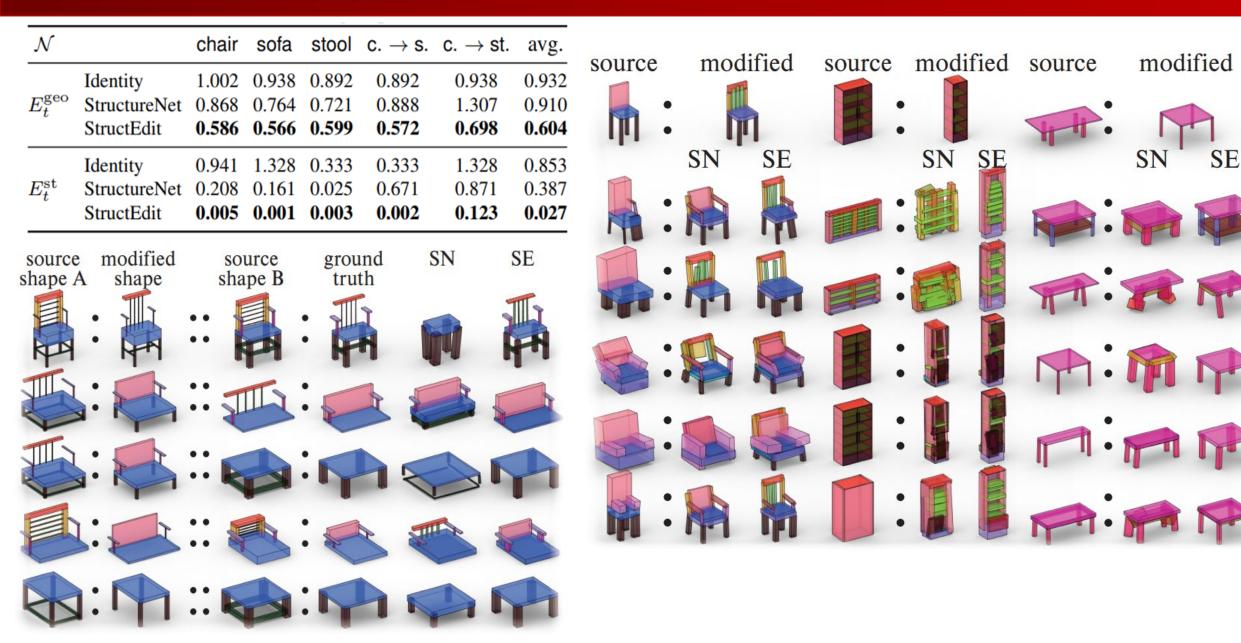


#### **Experiment: Edit Generation**

		$\mathcal{N}^{g}$				$\mathcal{N}^{s}$				source shape	ge	generated modifications			
		chair	table	furn.	avg.	chair	table	furn.	avg.						
	ID			1.684		1.629	1.479	1.446	1.518	$\mathcal{N}^{g}$				K	
	$SN_{0.2}$			1.626		1.308		1.243						•	
-				1.558		1.241		1.135							
	$SN_{1.0}$						1.057			$\mathcal{N}^{s}$					
	SE	1.593	1.655	1.561	1.603	1.218	1.000	1.015	1.078						
	ID	1.281	1.215	1.288	1.261	1.437	1.303	1.442	1.394						
	$\mathrm{SN}_{0.2}$	1.081	0.878	1.015	0.991	1.466	3.484	1.414	2.121						
90	$\mathrm{SN}_{0.5}$						3.300			$\mathcal{N}^{g}$			A A	K	
	$\mathrm{SN}_{1.0}$						3.622			$\mathcal{N}^{g}$					
	SE	0.559	0.524	0.741	0.608	0.609	0.451	0.676	0.579			A			
ource	e shape	i.		gene	erated n	nodifica	tions				To be	The state	the	A	
F	2									$\Lambda$				N	
		$\mathcal{N}^{g}$								<i></i>					
	-							M							
				J.											
		$\Lambda \int s$			FT	ST		1				Sec.		T	
										$\mathcal{N}^{s}$				T	
						SIL									
		$\Lambda \int g$		AS									-		
	~		1			UPL		-							

. .

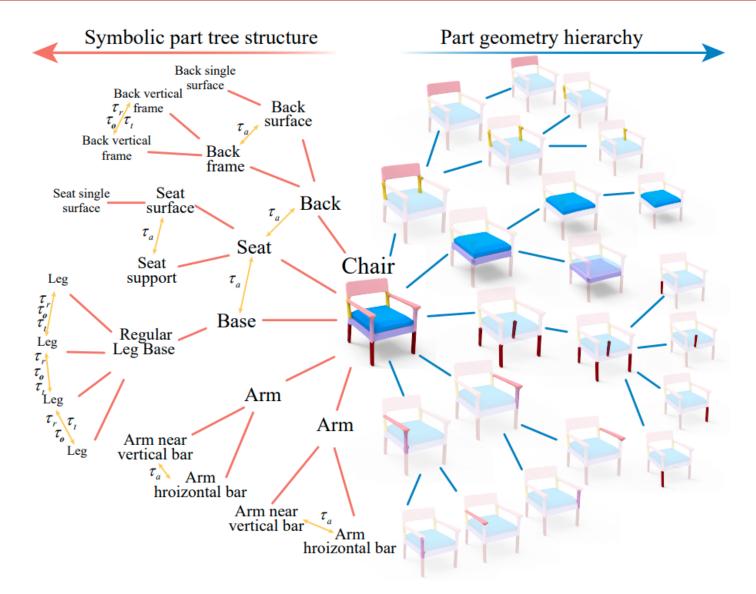
#### **Experiment: Edit Transfer**





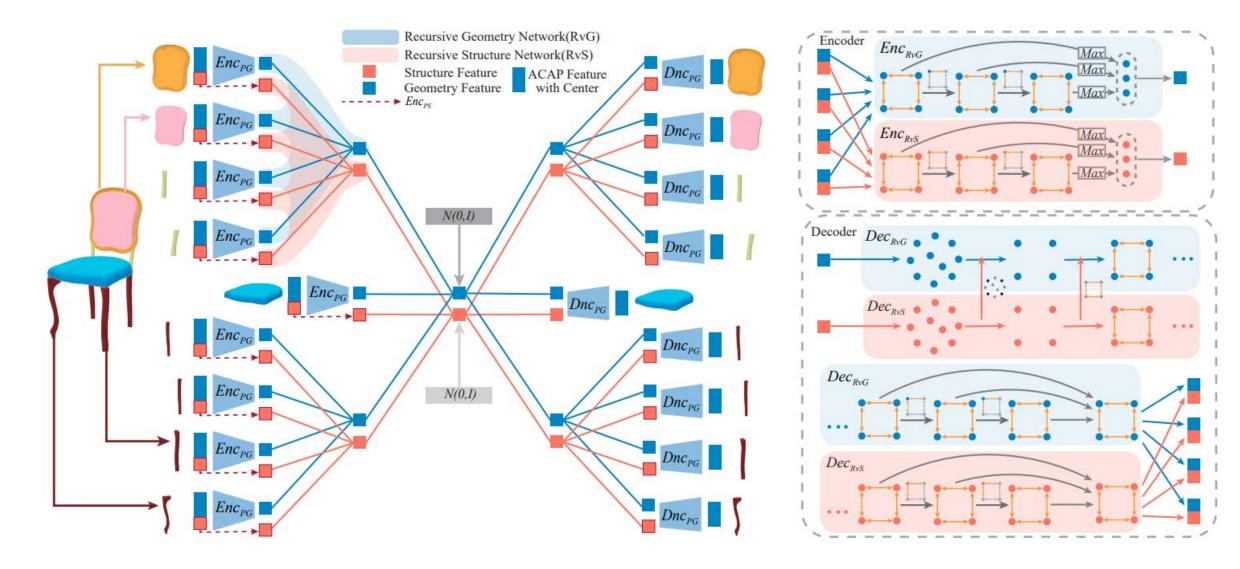
DSG-Net: Learning Disentangled Structure and Geometry for 3D Shape Generation. Jie Yang, Kaichun Mo, Yu-Kun Lai, Leonidas J. Guibas, Lin Gao

#### DSM-Net: Disentangled Tightly-Coupled Hierarchies



[Jie Yang, Kaichun Mo, Yu-Kun Lai, Leonidas J. Guibas, Lin Gao, 2020]

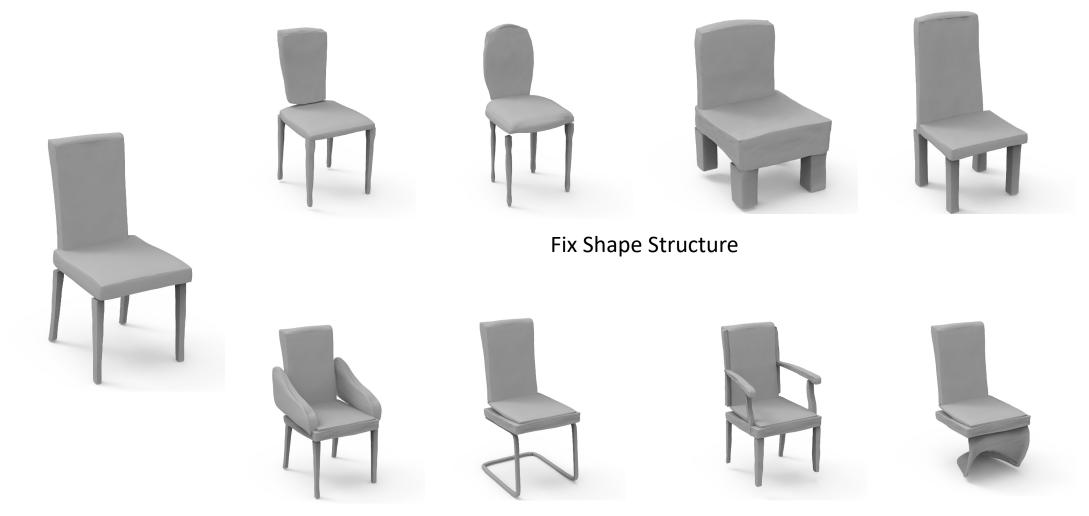
## **Coupled Network Architecture: Double-VAEs**



#### Shape Generation



#### **Disentangled Shape Generation**

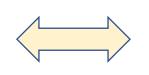


Fix Shape Geometry

#### Variation Generation

## Learning to Vary

- Re-use what we already have
- Populate sparsely sampled regions

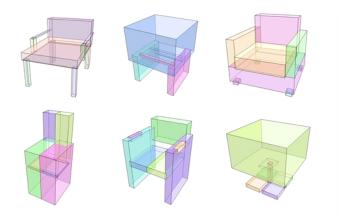


Geometry, Arrangement, Appearance, Motion

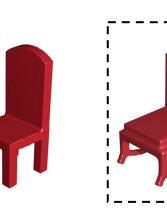
for Objects and Scenes

# Varying to Learn

- Provide generation diversity
- Create training data tailored for hard concepts









#### Motivation

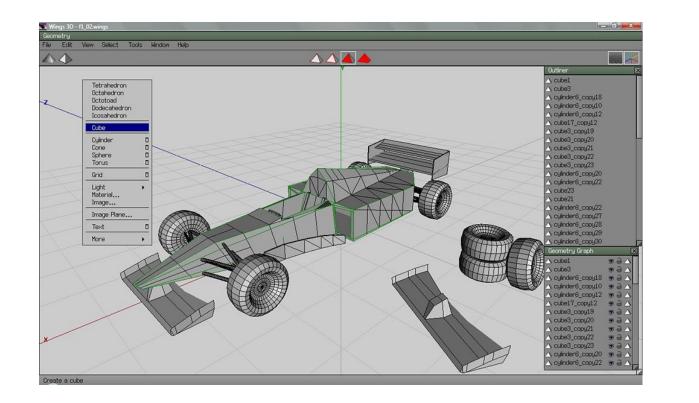




Photo taken from DeefSDF



Photo taken from Pixel2Mesh++

[1] DeepSDF: Learning Continuous Signed Distance Functions for Shape Representation. Park, et. al., CVPR 2019.

[2] Pixel2Mesh++: Multi-View 3D Mesh Generation via Deformation. Wen, et. al., ICCV 2019.

#### Motivation

• Leverage on existing (discrete) artist generated models



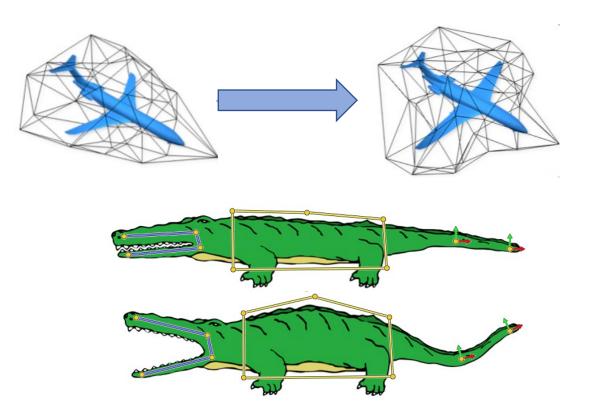
• Create new models through (continuous) variations/deformations



#### **Deformation Models**

- Leverage classical geometry techniques to define deformation.
  - Preserves local geometric features
  - In other words, ensures the quality of the output

- Cage-based deformation
  - Neural Cages (CVPR 2020)
- Control point-based / biharmonic coordinates
  - DeepMetaHandles (CVPR 2021)

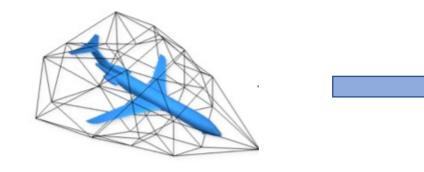


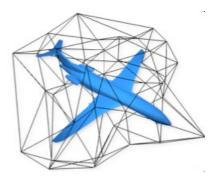
# Neural Cages for Detail-Preserving 3D Deformations

Wang Yifan, Noam Aigerman, Vladimir Kim, Siddhartha Chaudhuri, Olga Sorkine-Hornung (CVPR 2020)

### Key Idea

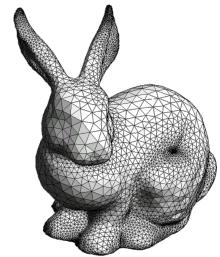
- Warp the source shape to match the general structure of the target while preserving surface details of the source
- Source shape is enclosed by a coarse control mesh  $\rightarrow$  cage
- Neural network learns to optimize both the position of the cage around the source and the deformation of the cage to match the target



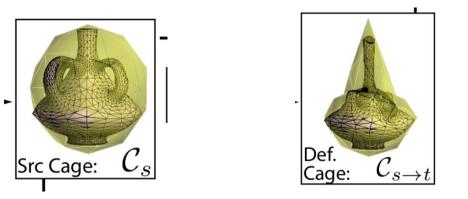


### Deformation

- Competing objectives
  - 1. Alignment with the target
  - 2. Quality: minimize distortion, preservation of geometric features
- Cage-based deformation enforces constraints to preserve local geometric features



## Cage-based Deformation (CBD)

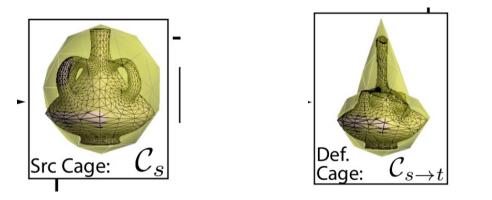


- CBD controls the warping of source S by enclosing it with a coarse triangular mesh C (cage), and warping this cage instead
- Any point *p* in ambient space is encoded via a generalized barycentric coordinate: weight average of cage vertices:

$$\mathbf{p} = \sum \phi_j^{\mathcal{C}} \left( \mathbf{p} \right) \mathbf{v}_j$$

- Weight functions  $\{\phi_j^{\mathcal{C}}\}$  depend on the relative position of p wrt the cage vertices

# Cage-based Deformation (CBD)



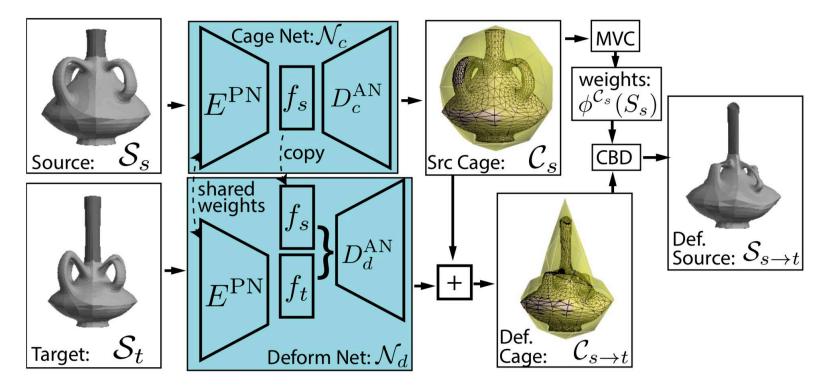
- We then only deform the cage vertices and use the pre-computed weights  $\left\{\phi_j^{\mathcal{C}}\right\}$
- The deformation of any point in ambient space is then given by

$$\mathbf{p}' = \sum_{0 \le j < |V_{\mathcal{C}}|} \phi_j^{\mathcal{C}}\left(\mathbf{p}\right) \mathbf{v}'_j$$

• Use mean value coordinates (MVC) [1] to obtain weight functions  $\{\phi_j^C\}$ : simple and differentiable

[3] Tao Ju, Scott Schaefer, and Joe Warren. Mean value coordinates for closed triangular meshes. TOG 2004

#### Learning cage-based deformation

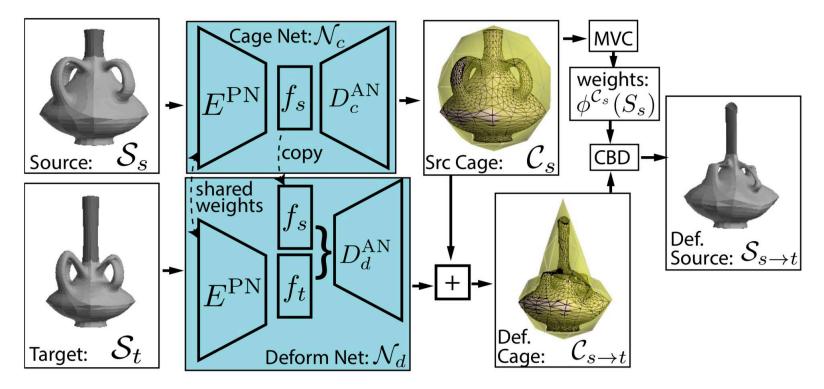


• Train a network to predict both source and target cages

$$C_s = \mathcal{N}_c \left( \mathcal{S}_s \right) + \mathcal{C}_0, \qquad C_{s \to t} = \mathcal{N}_d \left( \mathcal{S}_t, \mathcal{S}_s \right) + \mathcal{C}_s$$

• Initial template cage is a 42-vertex sphere  $C_0$ 

#### Learning cage-based deformation



- Both branches of encoder and decoder only predict the cage; they don't rely on detailed geometric features of the input
- Network does not require high resolution

#### Losses

- Cage loss:
  - Encourage positive MVC (weights of the cage)
  - Negative weights occur when the source cage is <u>highly concave</u>, <u>self-overlapping</u> or when <u>points lie outside the cage</u>

- Alignment loss:
  - Chamfer distance / L2 distance or deformed source to target

#### Losses

- Shape Loss
  - Basically to ensure good quality of the output shape
  - Modified Laplacian:

$$\mathcal{L}_{p2f} = \frac{1}{|\mathcal{S}_s|} \sum_{i=1}^{|\mathcal{S}_s|} ||d_i - d'_i||^2$$

<u>PCA normals</u>:

$$\mathcal{L}_{\text{normal}} = rac{1}{|\mathcal{S}_s|} \sum_{i}^{|\mathcal{S}_s|} (1 - \mathbf{n}_i^T \mathbf{n}_i')$$

• <u>Symmetry</u> loss

• Total Shape loss

: 
$$\mathcal{L}_{shape} = \mathcal{L}_{p2f} + \mathcal{L}_{normal} + \mathcal{L}_{symm}$$

• Total loss:  $\mathcal{L} = \alpha_{\text{MVC}} \mathcal{L}_{\text{MVC}} + \mathcal{L}_{\text{align}} + \alpha_{\text{shape}} \mathcal{L}_{\text{shape}}$ 

#### Experiments



Figure 4: Comparison of our method with other non-homogeneous deformation methods. Our method achieves superior detail preservation of the source shape in comparison to optimization-based [10] and learning-based [6,9,28] techniques, while still aligning aligning output to the target.



Figure 5: Comparison of our method with anisotropic scaling. Our method better matches corresponding semantic parts.

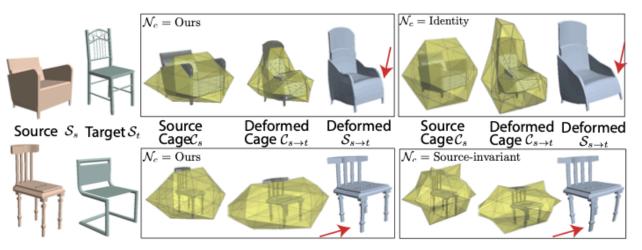


Figure 14: The effect of source-cage prediction. We compare our perinstance prediction of  $\mathcal{N}_c$  with (1) a static spherical cage (top right) and (2) a single optimized cage prediction over the entire training set (bottom right). Our approach achieves better alignment with the target shape. DeepMetaHandles: Learning Deformation Meta-Handles of 3D Meshes with Biharmonic Coordinates

> Minghua Liu, Minhyuk Sung, Radomir Mech, Hao Su (CVPR 2021)

# Key Idea

- Conditional generative model based on mesh deformation
- Able to generate variations of a shape without a specific target shape (as in Neural Cages)



• Deformations represented as a combination of given handles

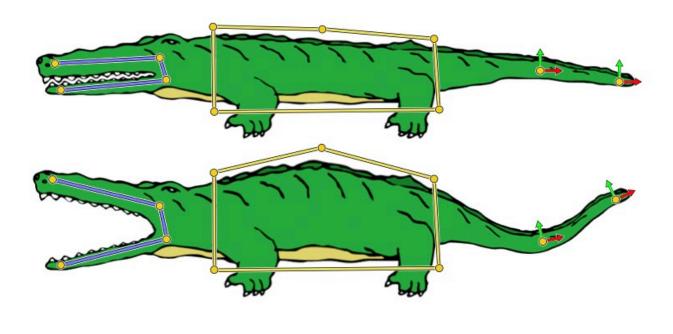
#### Control points / handles

• Bounded biharmonic weights

$$\mathbf{p}' = \sum_{j=1}^m w_j(\mathbf{p}) \, T_j \mathbf{p},$$

$$\underset{w_{j}, \ j=1,...,m}{\arg\min} \sum_{j=1}^{m} \frac{1}{2} \int_{\Omega} \|\Delta w_{j}\|^{2} dV$$
(2)

subject to:  $w_j|_{H_k} = \delta_{jk}$  (3)  $w_j|_F$  is linear  $\forall F \in \mathcal{F}_C$  (4)  $\sum_{j=1}^m w_j(\mathbf{p}) = 1$   $\forall \mathbf{p} \in \Omega$  (5)  $0 \le w_j(\mathbf{p}) \le 1, \ j = 1, \dots, m, \ \forall \mathbf{p} \in \Omega,$  (6)



[4] Alec Jacobson, et al. Bounded biharmonic weights for real-time deformation. TOG 2011

#### Metahandles

- Given:
  - Mesh vertices:  $\mathbf{V} \in \mathbb{R}^{n \times 3}$
  - Control points:  $\mathbf{C} \in \mathbb{R}^{c \times 3}$ ,



• Linear map:  $\mathbf{W} \in \mathbb{R}^{n \times c}$ , pre-computed "biharmonic coordinates"

 $\mathbf{V} = \mathbf{W}\mathbf{C}$ 

• Naive deformation: f :  $\mathbb{R}^{c imes 3}$  ightarrow  $\mathbb{R}^{n imes 3}$  ,

$$f(\mathbf{C}) = \mathbf{W}\mathbf{C}$$
 has 3c DoF!

• A metahandle is represented as a set of offsets over the c control points

$$\mathbf{M}_i = [ec{t}_{i1}, \cdots, ec{t}_{ic}]^T$$

• Deformation function is defined as a linear combination of metahandles

$$g(\mathbf{a}; {\mathbf{M}_i}_{i=1\cdots m}) = \mathbf{W}(\mathbf{C}_0 + \sum_{i=1}^m a_i \mathbf{M}_i),$$

#### **Network Architecture**

#### • Predict set of metahandles and ranges

c : num control points m : num metahandles

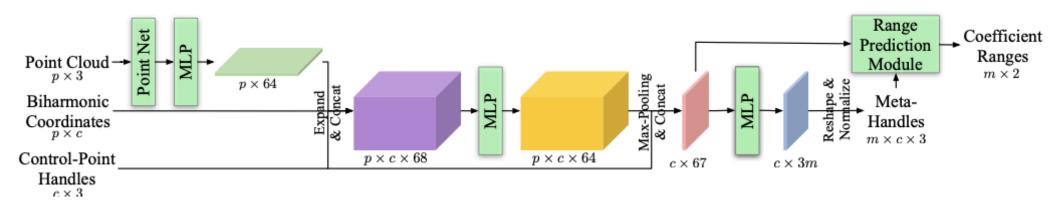


Figure 3: Architecture of MetaHandleNet: it incorporates the information from the shape (point cloud), control-point handles, and biharmonic coordinates by building a 3D tensor, and predicts a set of meta-handles with the corresponding coefficient ranges for the shape.

#### **Network Architecture**

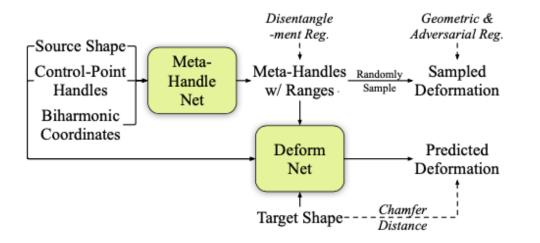


Figure 4: Overview of our method. We learn the meta-handles in an unsupervised fashion.

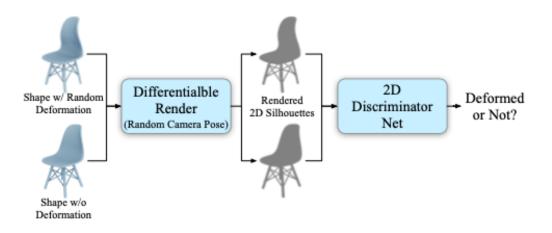


Figure 5: We utilize a soft rasterizer [24] and a 2D discriminator network to penalize unrealistic deformations.

$$\mathcal{L} = \mathcal{L}_{fit} + \mathcal{L}_{geo} + \mathcal{L}_{adv} + \mathcal{L}_{disen}.$$

$$\mathcal{L}_{geo} = \mathcal{L}_{symm} + \mathcal{L}_{nor} + \mathcal{L}_{Lap},$$

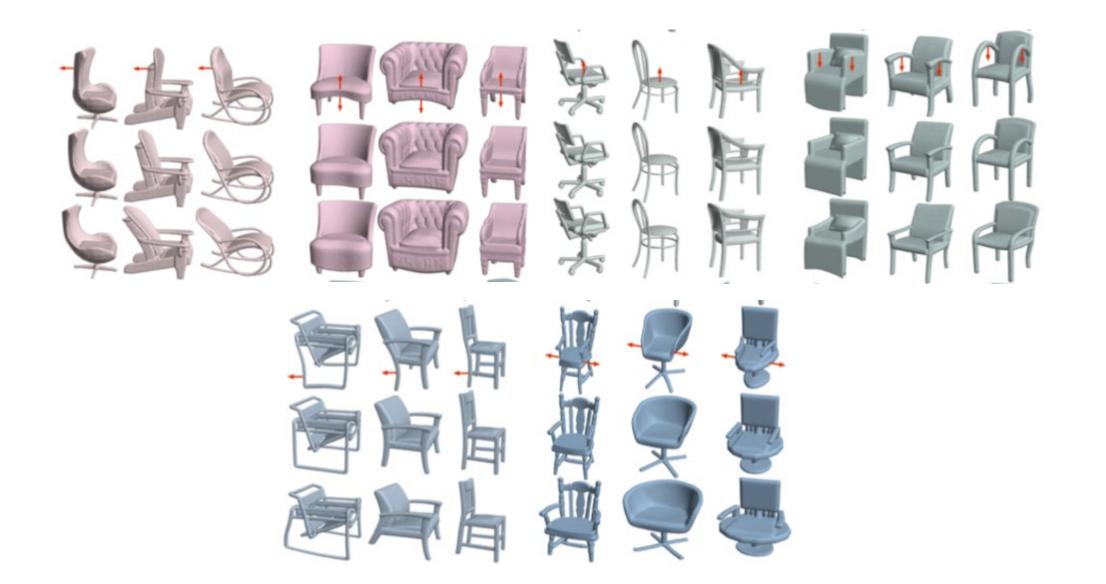
$$\mathcal{L}_{disen} = \mathcal{L}_{sp} + \mathcal{L}_{cov} + \mathcal{L}_{ortho} + \mathcal{L}_{SVD}.$$

#### Experiments



Figure 6: Qualitative comparison of our method with other deformation methods [13, 39, 10, 46]. Our method allows flexible deformation and fine-grained detail preservation. Our results are also more plausible, especially when the source-target pairs do not share the same structures (see the second and the fourth columns). Please zoom in for details.

#### Experiments



# **Deformation-Aware Retrieval**

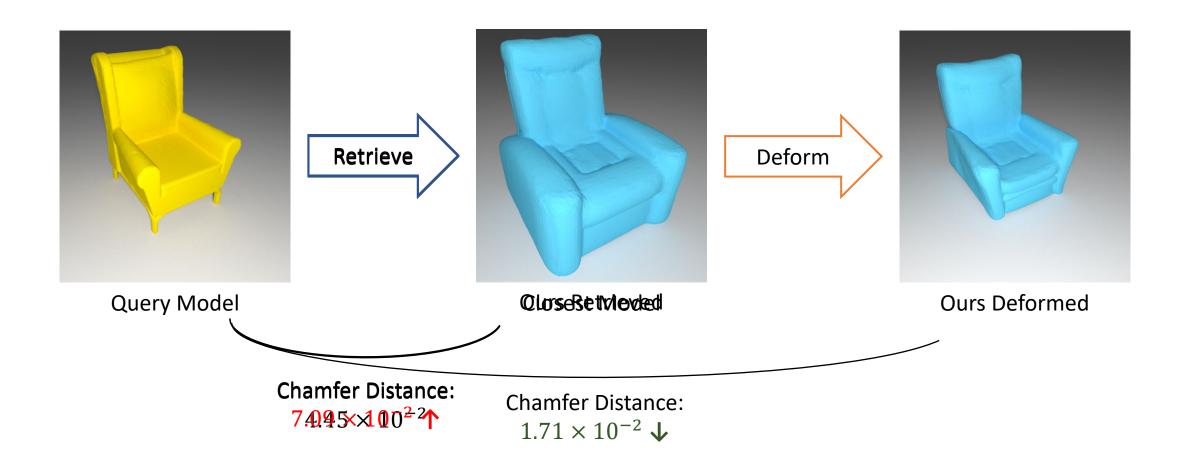
M.Uy, J. Huang, M. Sung, T. Birdal, L. Guibas (ECCV 20) M. Uy, V. Kim, M. Sung, N. Aigerman, S. Chaudhuri, L. Guibas (CVPR 21)

#### Problem

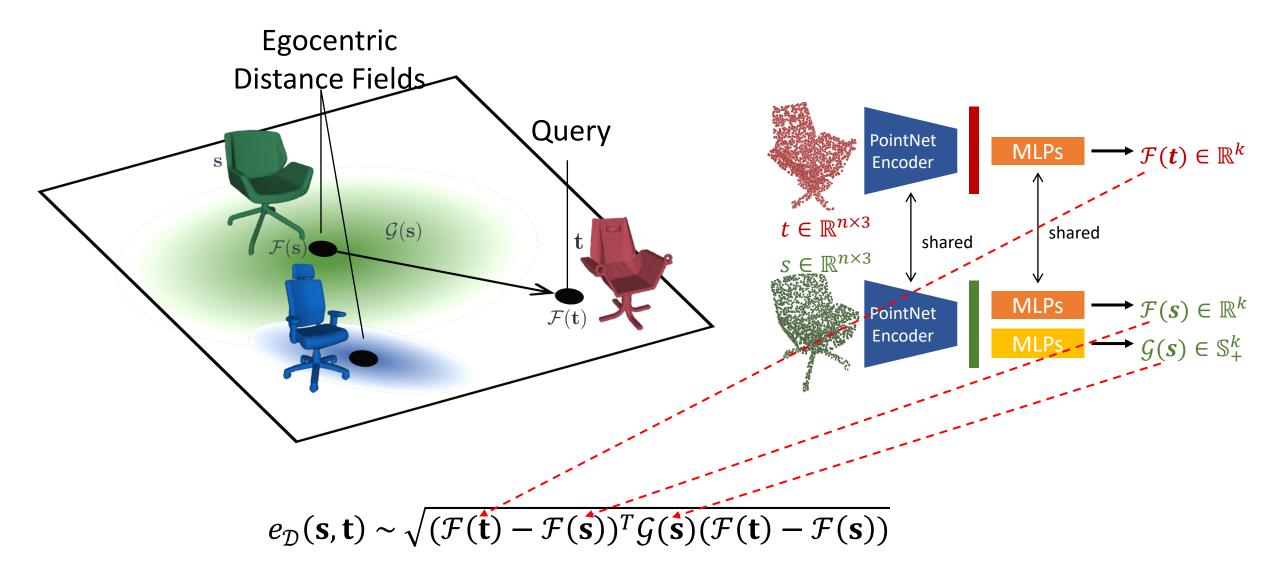


Not all shapes are "deformable" to each other!

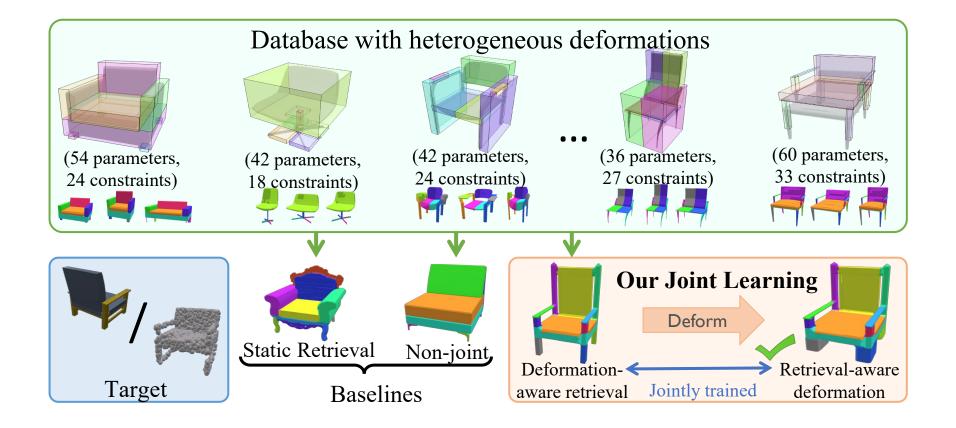
#### Key Idea



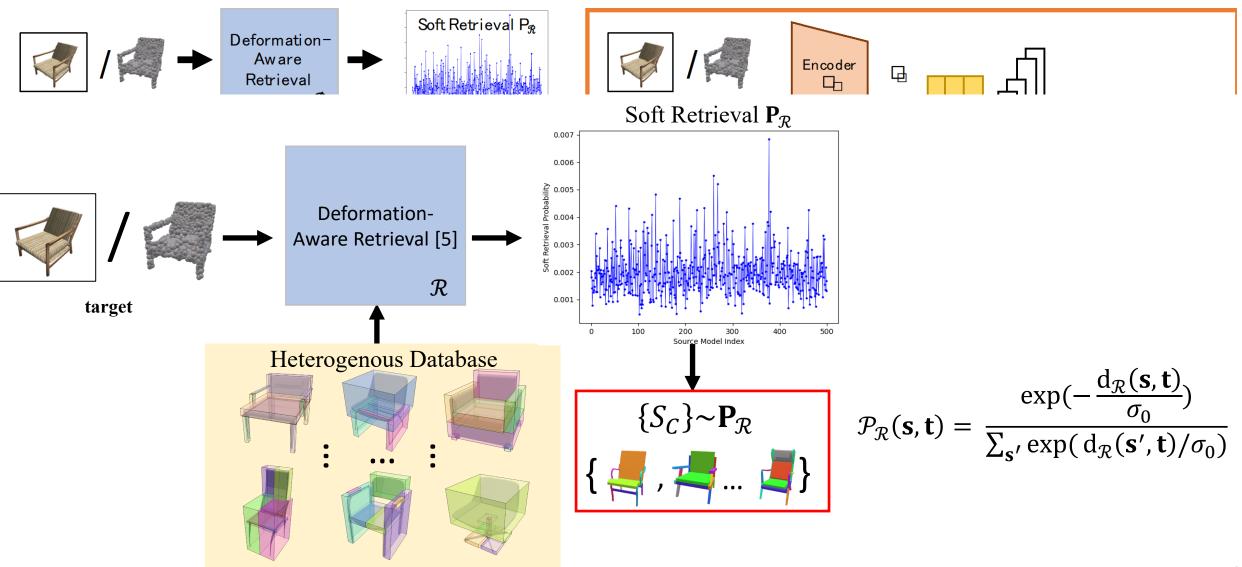
#### **Deformation-Aware Embedding**



#### Joint Learning – Retrieval-Aware Deformation



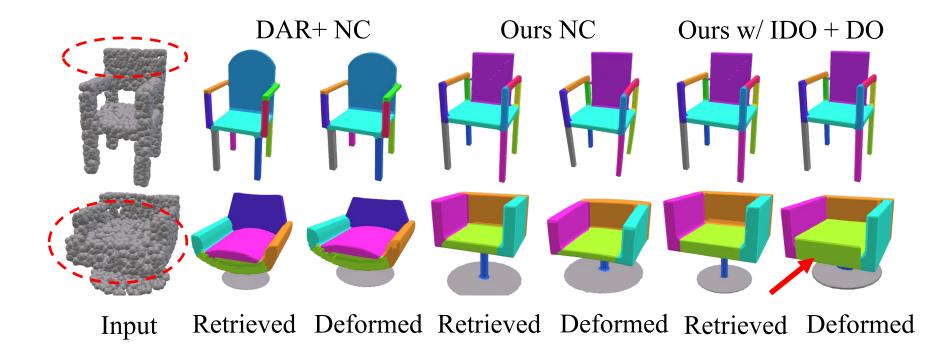
#### Joint Approach – Soft Retrieval



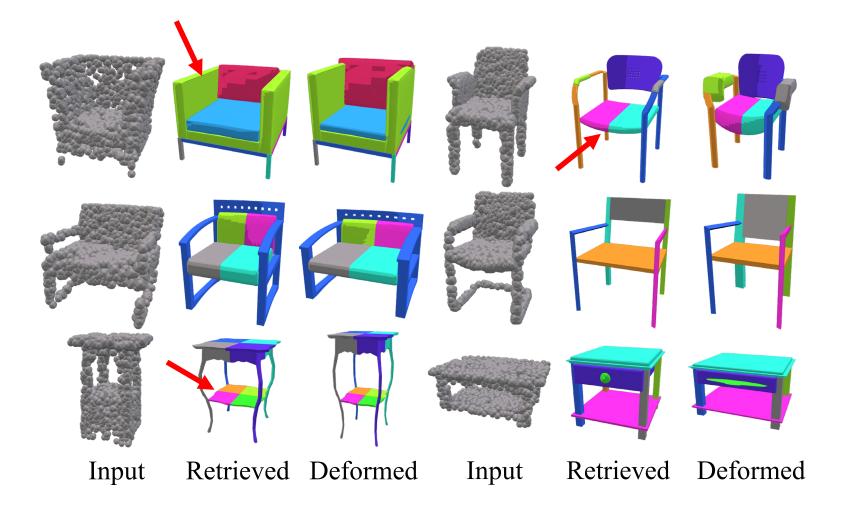
>

#### Results

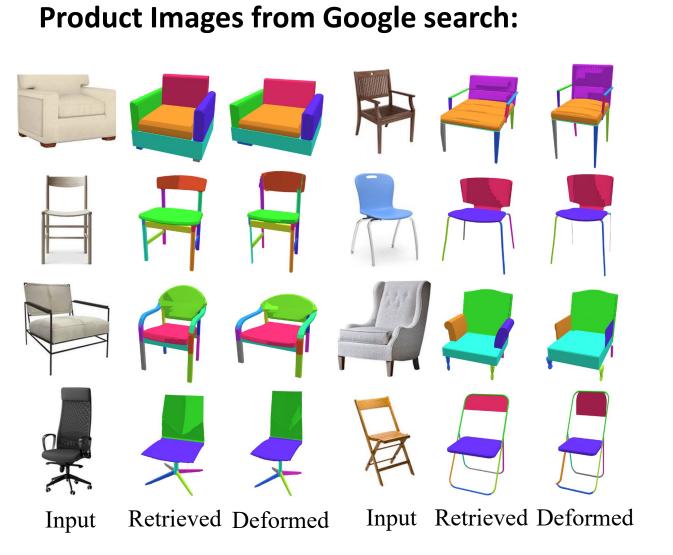
• Our joint approach on Neural Cages:



#### **Results – autosegmented dataset**



# Applications



**Real Scans:** 



Input Retrieved Deformed Input Retrieved Deformed

